Non-Fermi Liquid Behavior Close to a Quantum Critical Point in a Ferromagnetic State without Local Moments

E. Svanidze, ¹ L. Liu, ² B. Frandsen, ² B. D. White, ³ T. Besara, ⁴ T. Goko, ^{2,†} T. Medina, ⁵ T. J. S. Munsie, ⁵ G. M. Luke, ⁵ D. Zheng, ⁶ C. Q. Jin, ⁶ T. Siegrist, ⁴ M. B. Maple, ³ Y. J. Uemura, ² and E. Morosan^{1,*}

¹Department of Physics and Astronomy, Rice University, Houston, Texas 77005, USA

²Department of Physics, Columbia University, New York, New York 10027, USA

³Department of Physics, University of California, San Diego, La Jolla, California 92093, USA

⁴National High Magnetic Field Laboratory, Florida State University, Tallahassee, Florida 32306, USA

⁵Department of Physics and Astronomy, McMaster University, Hamilton, Ontario L8S 4M1, Canada

⁶Institute of Physics, Chinese Academy of Sciences, Beijing 100190, China

(Received 16 July 2014; revised manuscript received 24 November 2014; published 4 March 2015; corrected 16 March 2015)

A quantum critical point (QCP) occurs upon chemical doping of the weak itinerant ferromagnet $Sc_{3.1}In$. Remarkable for a system with no local moments, the QCP is accompanied by non-Fermi liquid behavior, manifested in the logarithmic divergence of the specific heat both in the ferro-and the paramagnetic states, as well as linear temperature dependence of the low-temperature resistivity. With doping, critical scaling is observed close to the QCP, as the critical exponents δ , γ , and β have weak composition dependence, with δ nearly twice and β almost half of their respective mean-field values. The unusually large paramagnetic moment $\mu_{PM} \sim 1.3 \mu_B/F$.U. is nearly composition independent. Evidence for strong spin fluctuations, accompanying the QCP at $x_c = 0.035 \pm 0.005$, may be ascribed to the reduced dimensionality of $Sc_{3.1}In$, associated with the nearly one-dimensional Sc-In chains.

DOI: 10.1103/PhysRevX.5.011026 Subject Areas: Condensed Matter Physics

I. INTRODUCTION

Quantum critical points (QCPs) are ubiquitous features in the phase diagrams of strongly correlated electron systems, ranging from high-temperature oxide superconductors [1–3] and low-dimensional compounds [4–6], to itinerant magnets (IMs) [7–10] and heavy fermions (HFs) [11–16]. Often, non-Fermi liquid (NFL) behavior [17–21], and critical scaling [22] accompany the QCP, and such novel phenomena have been extensively studied in HFs and, in particular, in antiferromagnetically ordered systems. However, fewer ferromagnetic QCPs are known and much less is currently understood about itinerant electron magnets and their quantum critical behavior, particularly due to the limited number of existent IMs. These observations make itinerant *ferromagnets* (IFMs) particularly appealing, given the comparatively smaller number of known ferromagnetic (FM) rather than antiferromagnetic (AFM) QCPs. The QCPs recently observed in two substantively different systems, the IFM ZrZn₂ [7] and the HF ferromagnet

Published by the American Physical Society under the terms of the Creative Commons Attribution 3.0 License. Further distribution of this work must maintain attribution to the author(s) and the published article's title, journal citation, and DOI. URu₂Si₂ [23], are two such FM QCP systems. NFL behavior is associated with the quantum phase transition induced by doping in the latter compound, but not the former, reemphasizing the imperious need for a unified picture of quantum criticality and NFL behavior in IFM systems. This study of the doping-induced NFL state close to the QCP in the IFM Sc_{3.1}In provides a first connection between the two previously known ferromagnetic QCP systems, a precursor of such a unified theory.

Lu doping in Sc_{3.1}In represents the first report of NFL behavior associated with a QPT in this IFM. The critical composition x_c in $(Sc_{1-x}Lu_x)_{3,1}In$ is very small, close to 0.035. The critical scaling close to the QCP is remarkable in comparison to ZrZn₂ or URu₂Si₂: While Sc_{3.1}In is similar to the former compound as the only other known FM with no magnetic elements, its critical scaling is not mean-field-like (MF-like), akin to that in the latter system. The reduced crystallographic dimensionality of Sc_{3.1}In, associated with quasi-1D Sc-In chains (inset of Fig. 1), provides one plausible justification for the similarities with the two-dimensional URu₂Si₂, in contrast with the three-dimensional ZrZn₂. In URu₂Si₂, the Kondo effect is inherently coupled with the quantum critical behavior, but Sc_{3.1}In has no local moments, rendering its magnetism and the QCP even more striking. What makes Sc_{3.1}In even more unique is the NFL behavior, a trait so far not seen in IFMs without magnetic elements. It is therefore paramount to probe the existence of the QCP in this IFM system, and properly characterize the NFL behavior, as

^{*}Corresponding author. emorosan@rice.edu

[†]Present address: Laboratory for Muon Spin Spectroscopy, Paul Scherrer Institut, CH-5232 Villigen PSI, Switzerland.

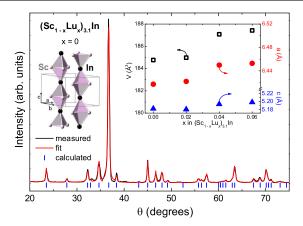


FIG. 1. Measured x-ray diffraction pattern for $(Sc_{1-x}Lu_x)_{3.1}In$ (black line), where x = 0, with calculated peak positions marked by vertical lines, based on space group P6₃/mmc and lattice parameters a = 6.42 Å and c = 5.18 Å. The crystal structure of $Sc_{3.1}In$ (left inset) exhibits quasi-1D chains of Sc-In. Right inset: Evolution of lattice parameters a and c and the unit-cell volume c with composition c.

a precursor for a unified picture of quantum criticality in IFMs. The development of such a unified theory necessitates more IFM systems, which starts with a thorough understanding of the few compounds that are already known.

IFMs lack the complexity associated with the interplay between the local and itinerant character of the electrons observed in HFs [15,24]. Of the two known IFMs with no magnetic elements, ZrZn₂ and Sc₃In, the latter presents the advantage, from the quantum criticality perspective, of a much lower magnetic ordering temperature $T_C \le 7.5 \text{ K}$ [25–29] in Sc₃In. This would likely facilitate the suppression of magnetic order towards a QCP but has proven difficult by the application of pressure [29] or a magnetic field [27]. Here, we show that the QCP in Sc_{3.1}In can indeed be reached by Lu doping, where the dopant ion is comparable in size $(r[Lu^{3+}] = 0.861 \text{ Å})$ with the host ion Sc that it substitutes for $(r[Sc^{3+}] = 0.745 \text{ Å})$ [30]. Therefore, the effects of chemical substitution can be deconvoluted from those of chemical pressure, which is important given that pressure was shown to enhance the ordering temperature [29]. The systematic analysis of the magnetization isotherms M(H), temperature-dependent magnetization M(T) at low fields, and H=0 specific heat data, for $0 \le x \le 0.10$, indicate that the magnetic ground state is suppressed in $(Sc_{1-x}Lu_x)_{3,1}$ In towards a QCP close to $x_c \approx 0.035$. Remarkably, the logarithmic divergence of the specific heat and the low-temperature resistivity linear in T close to x_c are evidence of the NFL behavior in both the ferromagnetic and the paramagnetic states. Additionally, the reduced crystallographic dimensionality, associated with quasi-1D Sc-In chains, may be linked to the NFL behavior and the non-MF critical scaling, similar to that in the more 2D FM, albeit with substantively different critical exponents.

II. EXPERIMENTAL METHODS

The hexagonal $Sc_{3.1}$ In compound has a Ni_3Sn -type structure, with space group $P6_3$ /mmc and lattice parameters a=6.42 Å and c=5.18 Å [31]. The reported crystal structure for Sc_3 In is shown in the left inset of Fig. 1. Highlighted are the Sc-In bipyramids which form nearly one-dimensional chains along the hexagonal c axis. In addition to the nearly one-dimensional crystal structure, band-structure calculations [32] also suggest possible reduced electronic dimensionality. These observations will be discussed in the context of the dimensionality of other IFM systems close to quantum criticality.

It had already been established [25] that Sc_3In forms nonstoichiometrically around the ionic ratio Sc:In = 3:1. In the current study, we have determined that the optimal composition, which yielded the highest Curie temperature T_C and paramagnetic moment μ_{PM} , was Sc:In = 3.1:1. Polycrystalline samples of $(Sc_{1-x}Lu_x)_{3.1}In$ ($0 \le x \le 0.10$) were prepared by arcmelting Sc (Ames Laboratory, 99.999%), Lu (Ames Laboratory, 99.999%) and In (Alfa Aesar, 99.9995%), with mass losses of no more than 0.5%. The arcmelted buttons were subsequently wrapped in Ta foil, sealed in quartz tubes under a partial Ar atmosphere, and annealed over two weeks at temperatures between 700 °C and 800 °C.

Both annealed and nonannealed samples exhibit extreme hardness, comparable to that of high carbon steel [33], which made it very difficult to perform powder x-ray diffraction measurements. However, it was feasible to x ray a polished surface of the arcmelted buttons. The arcmelted samples with a radius of about 3 mm were cut, and the flat surface was scanned for 12 hours in a Rigaku D/Max diffractometer with $CuK\alpha$ radiation and a graphite monochromator. An example of a diffraction pattern is shown in Fig. 1 for $(Sc_{1-x}Lu_x)_{3.1}In$ with x=0. All observed peaks can be indexed with the space group $P6_3/mmc$. As shown in the right inset of Fig. 1, both a (right axis, circles) and c (right axis, triangles) lattice parameters, along with the unit-cell volume V (left axis, squares) for $(Sc_{1-x}Lu_x)_{3.1}In$ for $0 \le x \le 0.10$, increase nearly linearly with x.

The dc magnetization measurements on the annealed samples were performed in a Quantum Design (QD) Magnetic Property Measurement System for temperatures between 1.8 K and 300 K, and for applied magnetic fields up to 5.5 T. Specific heat was measured from 0.4 K to 20 K in a QD Physical Property Measurement System.

Measurements of ac magnetic susceptibility were performed in a ⁴He dewar down to about 1.17 K, with temperatures below 4.2 K achieved by pumping on the He⁴ bath with a Stokes pump. The ac magnetic susceptibility coils were positioned in the thermal gradient above the ⁴He bath by manually adjusting the vertical position of

the probe. An ac current was driven on the primary coils with a frequency of 15.9 Hz using a linear research LR700 ac resistance bridge, which produces an ac magnetic field with a magnitude of around 0.3 Oe. This bridge was also used to measure the in- and out-of-phase components of the signal induced in the secondary pickup coils. The secondary coils are balanced by counterwinding the wire to cancel background signals induced by the oscillating ac magnetic field. A small offset in the measured signal due to minor imbalances in the homebuilt ac susceptibility coils was subtracted from the data. The data were then scaled so that their arbitrary units are proportional to emu/mol.

Muon-spin relaxation (μ SR) measurements were performed at TRIUMF using a He gas flow cryostat at the M20 beam line for Sc_{3.1}In and another spectrometer with a dilution cryostat at the M15 beam line for x = 0.01 and x = 0.025 (Sc_{1-x}Lu_x)_{3.1}In samples. Details of the μ SR technique can be found elsewhere [34–38].

III. RESULTS AND ANALYSIS

A. Temperature-dependent magnetization measurements

For weak IFMs, the low-field susceptibility is expected to follow a T^{-1} behavior [39]:

$$\frac{\chi_0}{\chi(T)} = 1 - \alpha + \lambda(T),\tag{1}$$

where the coefficient λ encompasses the dependence on the local amplitude of spin fluctuations and is linear in temperature $\lambda \sim T/T_C^*$, and $\alpha = I\rho(E_F)$, where I is the coupling constant and $\rho(E_F)$ is the density of states at the Fermi level. When $T^* \gg T_C^*$, $\alpha \sim (T/T^*)^2$ usually has only a weak T^2 dependence. However, the magnetic susceptibility $\chi(T)$ in $\mathrm{Sc}_{3.1}\mathrm{In}$ follows a modified Curie-Weiss-like law:

$$\chi(T) = \frac{C}{T^*} + \frac{C}{(T - T_C^*)},\tag{2}$$

as illustrated in Fig. 2(a). Such a temperature dependence can possibly be understood when considering strong spin fluctuations, associated with the low-dimensional Fermi surface of Sc₃In [32]: If $T^* > T_C^*$ (but not $\gg T_C^*$), then the temperature dependence of α is not negligible compared to that of λ . In weak IFMs, the Curie-Weiss-like temperature T_C^* , determined from linear fits of the inverse susceptibility after the temperature-independent term C/T^* was subtracted, coincides with the Curie temperature T_C . As shown below, this is not the case in $(\mathrm{Sc}_{1-x}\mathrm{Lu}_x)_{3.1}\mathrm{In}$, even though T_C and T_C^* are both continuously suppressed to 0 K with x.

A local minimum in the derivative dM/dT [Fig. 2(b), left axis] corresponds to the Curie temperature T_C in $\mathrm{Sc}_{3.1}\mathrm{In}$. Moreover, the specific heat data for x=0, plotted as C_p/T [right axis, Fig. 2(b)], also displays a broad maximum at T_C . This is remarkable, given that such transitions are often difficult to identify in the field-independent properties of IFMs, even in single crystalline samples [23]. In $\mathrm{Sc}_{3.1}\mathrm{In}$, the susceptibility derivatives and specific heat data provide evidence that the ferromagnetic ordering occurs below $T_C \sim 4.5$ K, as also demonstrated by the field-dependent data shown below. The different measurements consistently indicate that T_C is significantly lower than the older estimates from Arrott isotherms alone [26,28,29], when $\mathrm{Sc}_3\mathrm{In}$ was erroneously assumed to be a MF ferromagnet.

In $(\mathrm{Sc_{1-x}Lu_x})_{3.1}$ In, T_C is continuously suppressed by Lu doping above x=0.02 to values below those accessible by the QD MPMS system. Further data below T=2 K were collected from ⁴He ac susceptibility measurements shown in Fig. 2(c). Lack of data around the 4.2 K ⁴He transition precludes a T_C estimate for x=0 and x=0.005, when the transition falls close to this temperature interval. However, for all other compositions up to x=0.04, the peak corresponding to T_C [illustrated by the solid line fit in Fig. 2(c)] is continuously reduced to temperatures below T=1.17 K, as shown in Fig. 2(c). This agrees with the critical composition $x_C=0.035\pm0.005$, as determined from the analysis below.

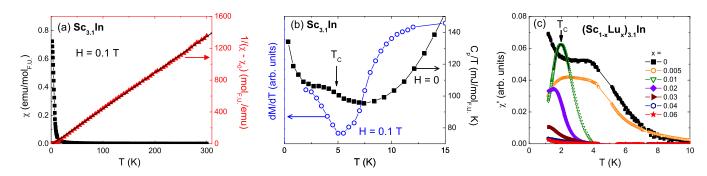


FIG. 2. (a) $Sc_{3.1}In$ susceptibility (left) and inverse susceptibility $1/(\chi - \chi_0)$ (right) for H = 0.1 T, where $\chi_0 = C/T^*$ (see text). (b) The magnetization derivative dM/dT (left) and specific heat C_p/T (right) for $Sc_{3.1}In$ with the vertical arrow marking the Curie temperature T_C . (c) $(Sc_{1-x}Lu_x)_{3.1}In$ ac susceptibility $\chi'(T)$. The Curie temperature T_C is estimated from the peak position (solid line), indicated by the vertical arrow.

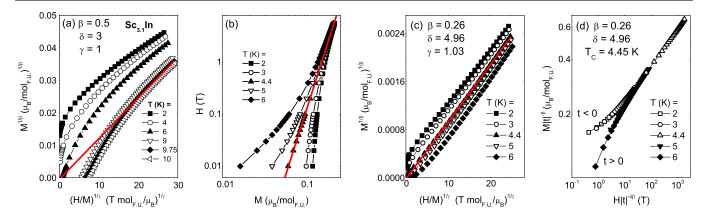


FIG. 3. $M^{1/\beta}$ vs $(H/M)^{1/\gamma}$ isotherms for $Sc_{3.1}$ In with (a) MF exponents $\beta = \beta_{\rm MF} = 0.5$ and $\gamma = \gamma_{\rm MF} = 1$, $T_C = 9.75$ K (solid line) and (c) non-MF exponents $\beta = 0.26$ and $\gamma = 1.03$, $T_C = 4.45$ K (solid line). (b) Log-log plot of $Sc_{3.1}$ In M(H) isotherms, with the straight line representing the fit for the critical isotherm. (d) Arrott-Noakes scaling plots $M|t|^{-\beta}$ vs $H|t|^{-\delta\beta}$. The scaled M(H) data collapse onto two diverging branches, one below T_C (t < 0, open symbols) and one above T_C (t > 0, full symbols).

B. Arrott and Arrott-Noakes analysis

Strong spin fluctuations in Sc_{3.1}In result in deviations from linearity in the inverse susceptibility around T_C^* which precludes the accurate determination of the Curie temperature T_C from the $\chi(T)$ data. Alternatively, Arrott isotherms M^2 vs H/M [40] had previously been employed to determine T_C in Sc_3 In. Existing reports estimate this value as less than 7.5 K [25–29]. If the Arrott plot technique were used for Sc_{3.1}In [Fig. 3(a)], it would appear that ferromagnetic order occurred close to 9.75 K. This implies that the Sc-In ratio used for the current study is closest to the optimal one [25], compared to all previous reports. However, the Arrott isotherms deviate strongly from linearity at high H values [26,28,29]. This is a compelling indication that the mean-field theory cannot accurately describe the weak ferromagnetism in Sc_{3.1}In, in contrast with, for example, ZrZn₂ [7]. The more generalized Arrott and Noakes method [41] was successfully employed to characterize the critical scaling in the HF ferromagnet URu₂Si₂ doped by Re [23]. In the current work, this generalized critical scaling is applied to a different type of QCP, in the weak IFM Sc_{3.1}In which has no local-moment elements. It would appear that the NFL behavior results from the non-MF character of the magnetism in these IFMs.

The Arrott-Noakes scaling represents a generalization of the MF scaling of the magnetization M, magnetic field H and the reduced temperature $t = (T/T_C - 1)$:

$$M \propto t^{\beta}$$
 for $t < 0$, (3)

$$M \propto H^{1/\delta}$$
 at $t = 0$, (4)

$$\chi \propto t^{-\gamma} \quad \text{for } t > 0.$$
(5)

This yields generalized critical exponents β , δ , and γ with the constraint that $1 + \gamma/\beta - \delta = 0$. In the case of $(\mathrm{Sc}_{1-x}\mathrm{Lu}_x)_{3.1}\mathrm{In}$, the Curie temperature T_C and exponent δ are first determined from log-log M(H) plots for each composition, as shown in Fig. 3(b) for x=0 and in Figs. 4(a)–4(c) for x=0.005, 0.008, and x=0.01. At T_C , critical scaling requires that the isotherm be linear, with a slope equal to the critical exponent δ . The T=1.8 K isotherm for x=0.02 is nearly linear all the way down to H=0 T [Fig. 4(d)], indicating that T_C for x=0.02 is finite

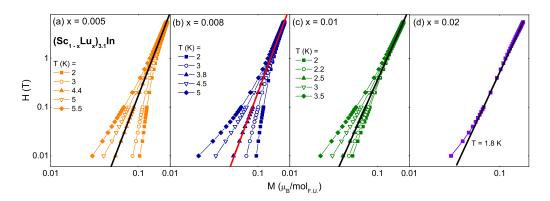


FIG. 4. Log-log $(Sc_{1-x}Lu_x)_{3.1}$ In M(H) isotherms for (a) x = 0.005, (b) x = 0.008, and (c) x = 0.01 with linear fits (solid lines) at the critical $(T = T_C)$ isotherm. (d) Log-log M(H) curve for x = 0.02 and T = 1.8 K, with a linear fit above H = 0.05 T.

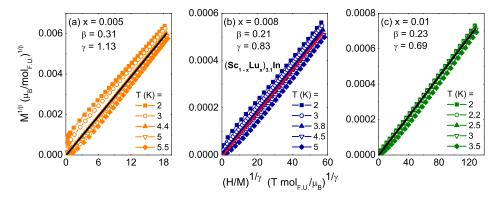


FIG. 5. $(Sc_{1-x}Lu_x)_{3.1}$ In Arrott-Noakes $M^{1/\beta}$ vs $(H/M)^{1/\gamma}$ isotherms for (a) x = 0.005, (b) x = 0.008, and (c) x = 0.01 with linear fits (solid lines) at T_C .

and smaller than 1.8 K. For all other FM compositions [Figs. 4(a)–4(c)], nonlinear isotherms occur within 20% of T_C . Therefore, in the absence of M(H) measurements below 1.8 K, the nearly linear log-log M(H; 1.8 K) isotherm for x=0.02 is a good indication that the T_C value estimate for this composition is within 20% of T_C , which yields $T_C(x=0.02)=1.5\pm0.3 \text{ K}$. This value agrees well with the ac susceptibility estimate, where $T_C=1.62 \text{ K}$.

Next, the critical exponents β and γ are determined from the expected linear dependence of $M^{1/\beta}$ vs $(H/M)^{1/\gamma}$. A subset of the resulting isotherms is shown in Figs. 3(c) (x=0) and 5(a)-5(c) (x=0.005,0.008 and 0.01). The extrapolations of the linearized isotherms in the ferromagnetic state yield the spontaneous magnetization M_0 from the vertical axes intercepts. As expected, M_0 scales with $|t|^{\beta}$, as shown in Fig. 6 for $(Sc_{1-x}Lu_x)_{3.1}In$, where $0 \le x \le 0.02$. In contrast with $URu_{2-x}Re_xSi_2$ [23], M_0 for $(Sc_{1-x}Lu_x)_{3.1}In$ (Fig. 6) grows faster in the ordered state, as the critical exponent β for the former, $\beta = 0.26 \pm 0.05$, is less than half of the respective value in the latter system [23]. However, the β values in $(Sc_{1-x}Lu_x)_{3.1}In$ are unusually small, which implies that the ordered moment in this weak IFM is more readily

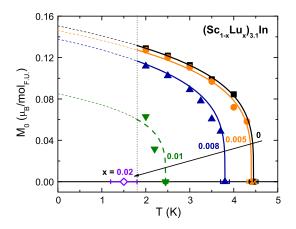


FIG. 6. Spontaneous magnetization $M_0(T)$ for $(Sc_{1-x}Lu_x)_{3.1}In$ where $0 \le x \le 0.02$.

destabilized by fluctuations close to T_C . This might indicate a fragile magnetism in a nearly 1D electron system [32], which is immediately suppressed to 0 K by doping and the attendant disorder.

The Arrott-Noakes critical exponents δ (triangles), γ (squares), and β (circles), scaled by their MF values, are presented in Fig. 7 as a function of composition. Most strikingly, δ is nearly twice as large as its MF value $\delta_{\rm MF}$, while β is nearly half of $\beta_{\rm MF}$, leaving γ nearly identical to its MF value $\gamma_{\rm MF}$. δ is a measure of the curvature of M(H) at T_C , with larger values signaling faster saturation. A comparison between $(Sc_{1-x}Lu_x)_{3,1}In$ and $URu_{2-r}Re_rSi_2$ [23] shows that larger δ values for the former compound are also associated with a larger relative magnetization $M(5.5T; 1.8 \text{ K}) \approx 0.2 \mu_B$. This value at t = 0.6is nearly 15% of the paramagnetic moment $\mu_{PM} \approx 1.3 \mu_B$ for the composition x = 0 with maximum T_C . The corresponding value for $URu_{2-x}Re_xSi_2$ is $M(5.5T; 1.8K)/\mu_{PM} \approx$ $(0.4\mu_B)/(3.8\mu_B) \approx 10\%$ (for which $T_{C,\text{max}} = 27 \text{ K}$ is obtained for x = 0.6), nearly one-third less at a comparable relative temperature t (Fig. 1, bottom panel, in Ref. [24]).

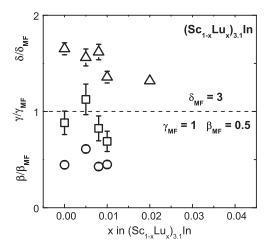


FIG. 7. The critical exponents scaled by their MF values $\delta/\delta_{\rm MF}$ (triangles), $\gamma/\gamma_{\rm MF}$ (squares), and $\beta/\beta_{\rm MF}$ (circles) as a function of composition x.

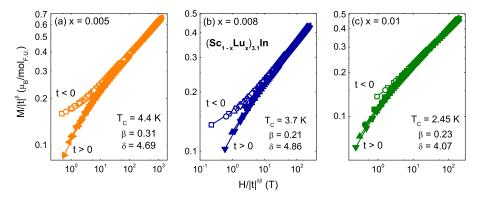


FIG. 8. Scaling plots $M|t|^{-\beta}$ vs $H|t|^{-\delta\beta}$ for (a) x = 0.005, (b) x = 0.08, and (c) x = 0.01 in $(Sc_{1-x}Lu_x)_{3,1}In$.

The scaling collapse of $M|t|^{-\beta}$ vs $H|t|^{-\delta\beta}$, shown in Figs. 3(d) and 8(a)–8(c), exemplifies how the $M|t|^{-\beta}$ vs $H|t|^{-\delta\beta}$ curves collapse onto two diverging branches, for t<0 (open symbols) and t>0 (full symbols). This collapse is similar to that observed for the HF URu_{2-x}Re_xSi₂ [23], which is remarkable, given the lack of formal local moments in the constituent elements of $(Sc_{1-x}Lu_x)_{3,1}In$.

C. Non-Fermi liquid behavior

Independent and compelling evidence for the QCP in the doped $Sc_{3,1}$ In system is the NFL behavior below x = 0.04. One signature of NFL behavior is the logarithmic temperature dependence of the specific heat C_p/T [Fig. 9(a)], which occurs over a decade in temperature. The TlnT specific heat, shown in Fig. 9(a), may, in principle, have two possible origins: NFL behavior or Schottky anomaly. For a Schottky anomaly, a low-T peak in the specific heat would move up in temperature with increasing H. However, the decrease of the low-temperature C_p/T with increasing H [inset, Fig. 9(a)] invalidates the Schottky anomaly scenario, not surprisingly, since this would be associated with low-lying energy states (which is not the case for a system with no formal local moments). The NFL scenario is therefore more plausible in $(Sc_{1-x}Lu_x)_{3,1}In$ for $0 \le x \le 0.04$. More interestingly, the NFL behavior coexists with the ferromagnetic state. This coexistence has been explained based on magnetic cluster formation as a result of competition between Ruderman-Kittel-Kasuya-Yosida (RKKY) coupling and the Kondo effect [42,43]. However, this is the *first* observation of NFL behavior within the ferromagnetic state in a weak IFM without magnetic elements. The implication is that a new model would be required to describe the ground state in Sc_{3.1}In, or that the Griffiths-McCoy model [44] may still be appropriate if evidence for the Kondo effect emerges for this compound.

Besides the TlnT behavior in the specific heat, $(Sc_{1-x}Lu_x)_{3.1}$ In displays linear resistivity at the lowest temperatures $\rho(T) = \rho_0 + AT^n$ (n = 1), as shown in Fig. 9(b). A detailed study of the $(Sc_{1-x}Lu_x)_{3.1}$ In resistivity and NFL

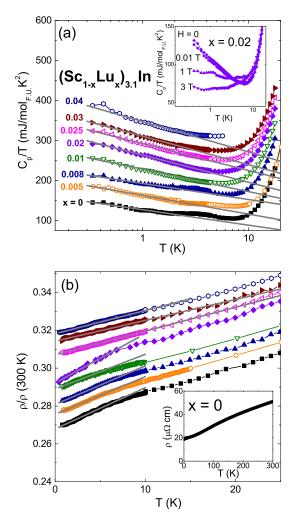


FIG. 9. (a) Semilog plot of the specific heat C_p/T (symbols) and the linear fits (lines) at low temperatures. The data for x>0 are shifted vertically for clarity by 30 mJ/mol_{F.U.} K². Inset: Specific heat for $(Sc_{0.98}Lu_{0.02})_{3.1}$ In in various magnetic fields: H=0, 0.01, 1, and 3 T. (b) Temperature-dependent resistivity for $(Sc_{1-x}Lu_x)_{3.1}$ In $(0 \le x \le 0.04)$. The data are shifted vertically for clarity. Inset: The whole range of $\rho(T)$ from which residual resistivity ratios (RRR) are determined.

TABLE I. Resistivity parameters summary.

x	ρ (0.8 K) (μ Ωcm)	RRR
0	19.0	2.7
0.005	14.7	3.5
0.008	12.6	3.0
0.010	15.1	2.8
0.020	14.6	3.1
0.025	18.0	3.1
0.030	15.8	2.7
0.040	24.1	2.7

behavior as a function on both T and x is underway [45], revealing that the resistivity exponent remains n = 1 well beyond T_C , substantively different from the marginal FL exponent n = 5/3 of $ZrZn_2$ [46]. Moreover, the specific heat data for ZrZn₂ are FL-like [47], with no TlnT dependence like that reported here for $(Sc_{1-x}Lu_x)_{3,1}In$. As illustrated by the inset in Fig. 9(b) for x = 0, all polycrystalline $(Sc_{1-x}Lu_x)_{3,1}$ In samples have comparable $\rho(T)$ values for $0 \le x \le 0.10$. It should be remarked that the absolute residual resistivity values ρ_0 and the residual resistivity ratios RRR = $\rho(300 \text{ K})/\rho_0$ (Table I) for $(Sc_{1-x}Lu_x)_{3,1}In$ are of the order of $\rho_0 \sim \mu\Omega$ cm and RRR around 3-4, values characteristic of good metals, comparable even with those of ZrZn₂ single crystals [46]. These are arguments suggesting minimal disorder effects on the quantum critical behavior of the doped Sc_{3.1}In. Even more important for the question of disorder, the resistivity change $\Delta \rho$ in the range of linearity [Fig. 9(b)] is also comparable to the residual resistivity values ρ_0 , whereas strong disorder effects would result in $\Delta \rho \ll \rho_0$. Therefore, the resistivity exponent itself, n = 1, and the TlnT specific heat in $(Sc_{1-x}Lu_x)_{3,1}$ In speak in favor of small disorder effects, in contrast with, for example, doped Ni_xPd_{1-x} [48]. In the latter compound, disorder was considered to change the temperature dependence of the specific heat from the expected NFL TlnT in the quantum critical region to $T^{3/2}$ slightly away from the QCP. Even for the pressure-induced QCP in MnSi [47], the resistivity exponent is found to be n = 3/2, a value attributed to frozen-in disorder even in very high purity systems.

D. Muon-spin relaxation measurements

The small saturation moments of itinerant systems preclude the accurate determination of the small ordered moment from neutron diffraction investigations, similar to the case of $ZrZn_2$ [49]. On the contrary, the muon-spin relaxation (μ SR) technique is extremely sensitive to local magnetic fields and has been used to investigate multiple itinerant systems [50–54]. Figure 10 shows the time spectra observed in the zero field (ZF) and longitudinal field (LF) at the lowest temperature. The fast relaxation in the early time region in ZF is eliminated by the decoupling effect in LF, which indicates that the observed relaxation

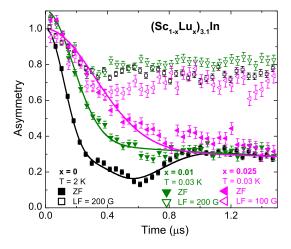


FIG. 10. Time spectra of ZF and LF μ SR of $(Sc_{1-x}Lu_x)_{3.1}In$, where x=0 (squares), 0.01 (downward-facing triangles), and 0.025 (leftward-facing triangles). The background sample holder contribution in the two Lu-doped samples was subtracted. The solid lines represent fits to Eqs. (6) and (7).

is due to a static field, generated by the static magnetic order in both the undoped and doped systems. For the ZF Sc_{3.1}In spectrum, two precession frequencies at low temperatures can be seen, as shown in Fig. 11(a). The ZF time spectra were analyzed by assuming a functional form of

$$G(t) = [A_1 \cos(2\pi\nu_1 t)e^{[-\Lambda_1^2(t^2/2)]} + A_2 \cos(2\pi\nu_2 t)e^{[-\Lambda_2^2(t^2/2)]} + (A_{1Z} + A_{2Z})e^{[-(t/T_1)]}]V_M + \frac{(1 - V_M)[G_{KT}(t, \Delta_{KT1}) + G_{KT}(t, \Delta_{KT2})]}{2},$$
 (6)

where $G_{KT}(t)$ is the Kubo-Toyabe function [55] for random nuclear dipolar fields, and A_{1Z} and A_{2Z} are assumed to be half of A_1 and A_2 , respectively, as expected for polycrystalline specimens. A very good fit was obtained by assuming $A_1 = A_2$, presumably due to two magnetically nonequivalent muon sites populated with equal probabilities. For the longitudinal relaxation rate $1/T_1$, two values for the two different sites could not be resolved. So, one value of T_1 was used in the fit. The temperature dependence of the two frequencies ν_1 and ν_2 is shown in Fig. 11(a). The volume fraction V_M of the magnetically ordered region, shown in Fig. 11(b), was determined from the amplitudes of the precession signals. The volume fraction V_M decreases gradually with increasing temperature, indicating coexistence of volumes (or regions) with and without static magnetic order. Although the precession signal disappears around T = 5.5 K, a small V_M remains above this temperature up to $T \approx 8$ K. This is due to a nonprecessing but relaxing signal with a small amplitude, caused by static random fields from the electron system remaining in a small volume fraction.

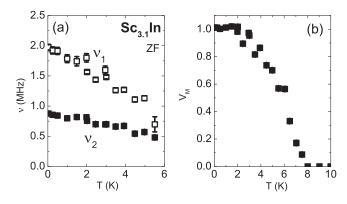


FIG. 11. (a) The muon-spin precession frequencies ν_1 (full squares) and ν_2 (open squares), and (b) the volume fraction V_M of the magnetically ordered regions, obtained from ZF μ SR of Sc_{3.1}In.

The Lu-doped samples show a relaxing signal without precession at low temperatures, indicating a more random internal field, as compared with the undoped Sc_{3.1}In. In order to reproduce the observed line shape, the ZF time spectra of the Lu-doped samples have been analyzed by assuming the following functional form:

$$G(t) = A_1(1 - p\sigma^2)e^{-\frac{1}{2}\sigma^2t^2} + \frac{A_1}{2}e^{[-(t/T_1)]} + A_{\text{bg}}, \quad (7)$$

where the first term represents the transverse relaxation, the second term is the longitudinal $1/T_1$ component, and the third term is a background signal from the sample holder. From independent measurements in a weak transverse field at low temperatures, the values of the nonrelaxing background signal from a silver sample holder A_{ba} were estimated to be 0.36 and 0.55 for x = 0.01 and 0.025 samples, respectively. These values are consistent with the known background level from the cryostat and sample holder, and a rather small sample size. However, it is not possible to eliminate the possibility that a signal from a small paramagnetic volume in the specimen, persisting to T=0 K, is included in the background signal. Because of the difficulty in separating the effects of slow relaxation and partial volume fraction, the amplitude A_1 was fixed to be temperature independent, allowing us to extract the relaxation rate σ . A phenomenological "dip" parameter p(p = 1) for the Kubo-Toyabe function was introduced, while smaller p values would fit line shapes with a shallower dip, which are often observed in real materials, including the present case of Lu-doped systems. Although the fit is not perfect, as shown by the lines in Fig. 10, the functional form of Eq. (7) was used to compare the relaxation rates in different specimens without introducing additional free parameters. Figure 12(a) shows the temperature dependence of σ in the two Lu-doped specimens. To compare the relaxation rates σ with the static field measured in undoped Sc_{3.1}In, the spatially averaged value of the static local field was determined as

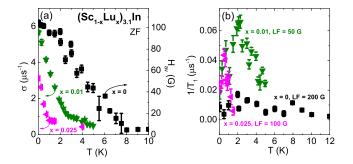


FIG. 12. (a) Muon-spin relaxation rate σ for x=0.01 (downward-facing triangles) and x=0.025 (leftward-facing triangles) for $(Sc_{1-x}Lu_x)_{3.1}In$ (left axis), along with the average static internal field $H_{\rm av}$ for x=0 (right axis), obtained from the fits of ZF μ SR measurements. The vertical axes are scaled with γ_{μ} , the gyromagnetic ratio of a positive muon. (b) The longitudinal relaxation rate $1/T_1$, obtained from the LF μ SR measurements.

$$H_{\text{av}} = V_M \frac{A_1 \nu_1 + A_2 \nu_2}{A_1 + A_2} + \frac{(1 - V_M)(\Delta_{\text{KT1}} + \Delta_{\text{KT2}})}{2\gamma_\mu}, \quad (8)$$

where γ_{μ} represents the gyromagnetic ratio of a positive muon and $\Delta_{\rm KT}$ are the widths of the Kubo-Toyabe function for nuclear dipolar fields. We plot $H_{\rm av}$ in Fig. 12(a) with the relaxation rate (left axis) and the average field (right axis), scaled with γ_{μ} . Since the static internal field is expected to be proportional to the local static spin polarization, Fig. 12(a) demonstrates the development of the spatially averaged magnetic order parameter which can be compared to the spontaneous magnetization M_0 , shown in Fig. 6.

Measurements of the spin-lattice relaxation rate $1/T_1$ were performed in an applied LF. Figure 12(b) shows the temperature dependence of $1/T_1$ for $(\mathrm{Sc}_{1-x}\mathrm{Lu}_x)_{3.1}\mathrm{In}$ with x=0,0.01,0025. There is no divergent behavior in $\mathrm{Sc}_{3.1}\mathrm{In}$, while the Lu-doped samples exhibit a peak in $1/T_1$ at the ordering temperature. In either case, the absolute values of $1/T_1$ are less than $0.1/\mu\mathrm{s}$, which implies that the relaxation rate measured in the zero field [Fig. 12(a)] is predominantly due to a static field, even at temperatures very close to the ordering temperature. In Fig. 12(a), a finite relaxation rate or average field persists up to high temperatures for all three systems. This is attributed to the nuclear dipolar field, as Sc has a very large nuclear moment.

The absence of dynamic critical behavior and the gradual change of the volume fraction V_M , observed in undoped $Sc_{3.1}In$, indicate a first-order transition at the magnetic order. It is interesting to note that a weak "second-order" feature is observed for Lu-doped samples. However, further experimental data are needed given the fact that the order parameter [Fig. 12(a)] exhibits a nonlinear dependence on the Curie temperature T_C , suggesting a remaining effect of first-order quantum evolution. Additionally, the difficulty in separating the effects of moment sizes and volume fraction at very small relaxation rates, as well as the

uncertainty in estimating the background level, prevents a reliable determination of V_M for the Lu-doped samples.

IV. DISCUSSION

The paramagnetic moment μ_{PM} [diamonds, Fig. 13(a)], determined by the Curie-Weiss-like law, is nearly composition-independent $\mu_{PM} \sim 1.3 \mu_B/F.U.$ Moreover, the Weiss-like temperature T_C^* decreases nearly linearly with x for $x \le 0.10$, after an initial jump between x = 0and 0.005 [squares, Fig. 13(a)]. Considering that Curie-Weiss-like behavior in the itinerant scenario arises from the temperature dependence of the amplitude of spin fluctuations [39], this sudden increase in the corresponding T_C^* signals enhanced spin fluctuations due to the disorder brought on by Lu doping. Between x = 0.02 and x = 0.04, T_C^* changes sign in a continuous manner, suggesting the presence of a (second-order) doping-induced QCP in this composition range near $x_c = 0.035 \pm 0.005$. Moreover, T_C determined either from $\chi'(T)$ or M(H) data [Figs. 2(c) and 5] moves down continuously in temperature below 1.17 K for the doping amounts above 0.03, indicating that the QCP is close to this composition.

The determination of the critical composition x_c at the QCP requires consistency between the M(T) and $\chi'(T)$ data, the critical scaling analysis of the M(H) measurements as well as the μ SR results. Indeed, the critical composition $x_c = 0.035 \pm 0.005$ is determined from (i) the T_C (circles and triangles) and T_C^* (squares) values [Fig. 13(b)] approaching 0 K at the QCP and (ii) the critical scaling rendering the Arrott-Noakes plots $M^{1/\beta}$ vs $(H/M)^{1/\gamma}$ as parallel isotherms, equally spaced in t [Figs. 3(c) and 5(a)–5(c)]. Moreover, the μ SR results confirm the development of static magnetic order with a nearly full volume fraction at low temperatures and a diminishing moment size as a function of decreasing

ordering temperature. Moreover, the continuous variation of T_C^* and T_C with x and the μ SR evidence for a second-order phase transition in the Lu-doped samples are also evidence for the QPT induced by Lu doping.

Doping in Sc_{3.1}In reveals intriguing traits associated with quantum criticality in general and with weak IFM systems in particular: The paramagnetic moment μ_{PM} is surprisingly large in $(Sc_{1-x}Lu_x)_{3,1}$ In and nearly independent of x, even as the system goes through the QPT at $x_c = 0.035 \pm 0.005$. Not surprisingly then, the critical exponent β is unchanged through the ferromagnetic state, although its value $\beta = 0.26 \pm 0.05$ is smaller than that in any other known quantum critical system. The minute critical composition and small β value, together with the jump in T_C^* as x > 0[Fig. 13(b), squares], point to a weak IFM ground state, easily perturbed by doping. This may seem unusual in light of the stark differences between Sc_{3 1}In and the related IFM system ZrZn₂ [7], with MF specific heat and marginal FL resistivity behavior, or the similarities with the extraordinary critical scaling in the HF FM URu_{2-r}Re_rSi₂ [23], close to these systems' respective doping-induced QCPs. However, these observations may be reconciled from crystallographic and electronic property considerations: As a nearly 1D structure is formed by bipyramidal Sc-In chains (inset of Fig. 1), the reduced dimensionality in Sc_{3.1}In renders it more similar to the layered (2D) URu₂Si₂ compound than the cubic (3D) ZrZn₂. It appears that the NFL behavior in the ferromagnetic state may also be correlated with the non-MF scaling and, more importantly, that this correlation is independent of the presence of hybridized f electrons. Consequently, the universality of the quantum critical behavior common to the former two compounds may be ascribed to spin fluctuations, associated with reduced crystallographic dimensionality. More IFM systems are needed to probe this universality. Equally important is the synthesis of single crystals of Sc_{3.1}In,

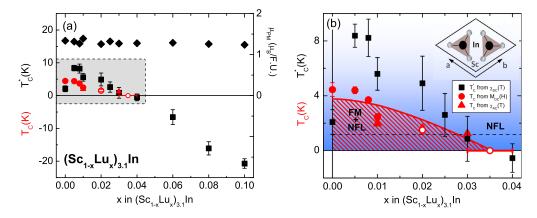


FIG. 13. (a) T-x phase diagram for $(Sc_{1-x}Lu_x)_{3,1}In$ for $0 \le x \le 0.10$, with the Weiss-like temperature T_C^* (squares, left axis), the Curie temperature T_C (circles, left axis) and paramagnetic moment μ_{PM} (diamonds, right axis). (b) Enlarged T-x phase diagram for $x \le 0.04$ [shaded area in (a)], with the ab plane projection of the $Sc_{3,1}In$ unit cell shown in the inset. The horizontal line at T=1.17 K denotes the minimum experimental temperature, with the open symbols representing T_C estimates extrapolated from accessible measurements.

which would enable further characterization of the implications of dimensionality on the QCP, as well as to probe the potential NFL behavior at the QCP and in the ferromagnetic state. These experiments are currently underway.

ACKNOWLEDGMENTS

We thank L. L. Zhao for help with figure edits, P. C. Canfield for providing some of the rare-earth metals, and Q. Si and M. C. Aronson for useful discussions. The work at Rice University was supported by National Science Foundation Grant No. DMR 0847681. Measurements of the AC magnetic susceptibility were performed at UCSD with support from the National Science Foundation under Grant No. DMR-1206553. Work at Columbia and TRIUMF (L. L., B. F., and Y. J. U.) was supported by NSF Grant No. DMR-1105961, DMREF Project No. NSF-DMR-1436095, and Grant No. OISE-0968226 (PIRE), a REIMEI project from JAEA, Japan, and the Friends of Todai Inc. Foundation. Work at IOPCAS was supported by NSF and MOST of China through research projects. T.B. and T.S. acknowledge support by the Department of Energy, Basic Energy Science, Division of Materials Science under award DE-SC0008832, and the National High Magnetic Field Laboratory, which is supported by National Science Foundation Cooperative Agreement No. DMR-1157490 and the State of Florida.

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