

# An Interactive Exploration Tool for High-Dimensional Datasets: A Shock Physics Case Study

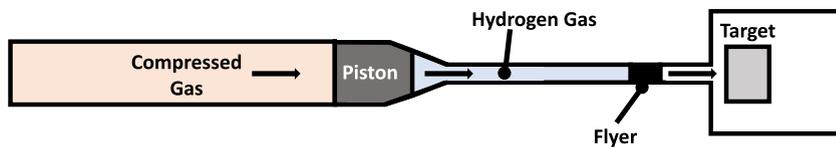
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**Abstract—Validating simulations with experimental results is a vital component of modern materials science. Existing workflows require substantial human intervention to interpret their results. We present a statistical approach to identify physically meaningful features, and we construct a visualization system that allows users to interactively and intuitively explore their datasets.**

■ **MATERIALS SCIENTISTS STUDYING** how materials respond to harsh environment involving materials failure (i.e., damage and shock) frequently work with ensemble datasets that are generated from the simulations as well as the experiments. These simulations often involve multiple input parameters (e.g., 10–20 parameters) and the

output is a one-dimensional time series. In this high-dimensional dataset, generally, there does not exist a uniquely resolved output that matches exactly with the experiments. In an effort to understand their datasets, the domain scientists have to go through the thousands of output curves manually, look for different features in these curves, and try to find the input parameter combinations for which the simulation produces similar output as the experiments. This is a tedious and time-consuming task for the domain scientists, and the existing data analysis

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**Figure 1.** Schematic of the experimental setup. Compressed gas is released, which launches a flyer down a barrel. At the end of the barrel, the flyer impacts a target and the impact causes a shock wave to travel through the target.

tools that can help them achieve their goals are mostly lacking.

Interactive visual analysis of curves has been a well-researched topic in the past. Although there exist multiple data analysis and visualization tools that provide generic solutions to scientific problems (see “RELATED TOOLS”), there are certain problems—like the one mentioned above—that require specialized tools that utilize domain-specific knowledge or operations and still be lightweight. Examples of domain-specific software and tools are CoFlaVis,<sup>1</sup> ImageVis3D,<sup>19</sup> and Seg3D.<sup>20</sup> The teams behind SCIRun and CoFlaVis have recognized and documented the usefulness of such domain-specific tools, which make for easier maintainability, smaller codebases, and less time to solution for the users.

In this work, we have developed a data analysis and visualization tool for exploring a high-dimensional dataset by closely working with the materials scientists of the shock physics domain. Given high-dimensional input and output data, our tool provides interaction capabilities to the users for feature extraction, feature correction, simulation validation, parameter importance exploration, and intuitive drawing-based feature query within a unified interface. To facilitate the exploration process, our proposed tool uses ensemble spaghetti plots for initial data visualization, principal component analysis (PCA)-based similarity analysis for validation and interactive selection, parallel coordinates plot (PCP)-based visualization for high-dimensional input parameter combination, existing sensitivity methods for understanding parameter importance, and  $k$ -nearest neighbor (KNN)-based analysis for drawing-based curve selection. We work closely with domain scientists to understand their requirements, and their feedback shows the efficacy of our proposed exploration tool.

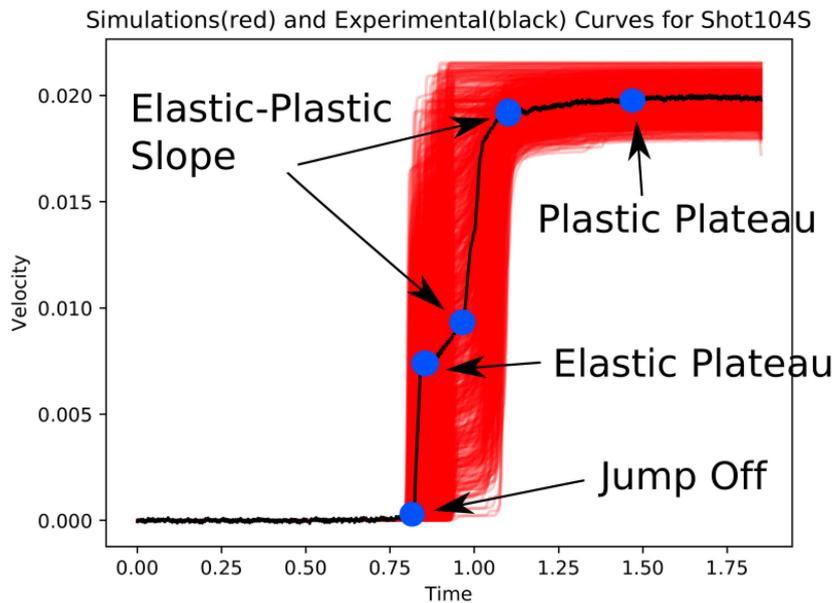
## RELATED TOOLS

For general data analysis and visualization, there are different tools and software available. Visualization Tool Kit or VTK<sup>13</sup> is a popular open-source software with multiple functionalities for data visualization such as isocontours, streamlines, and volume rendering. ParaView<sup>14</sup> is built on the top of the VTK to provide a graphical interface for ease of use. Another open-source tool that can provide effective data visualization is VisIt.<sup>15</sup> MATLAB is a multiparadigm numerical computing environment that is popular for basic data analysis and visualizations. Tools developed in Python<sup>16</sup> are now becoming popular open-source alternatives to MATLAB scripts. MayaVi<sup>17</sup> is a Python-based tool that uses VTK to provide effective data visualization. Amira 3D Software for Life Sciences<sup>18</sup> is another product that provides 3-D and 4-D visualizations for life science, CFD, and materials science datasets. CoFlaVis,<sup>1</sup> ImageVis3D,<sup>19</sup> and Seg3D<sup>20</sup> provide more domain-specific solutions for a set of targeted users. Our proposed tool is Python-based due to its popularity and cross-platform support.

## DATA DESCRIPTION

### Shock Physics Experiments and Simulations

In this work, the material properties of wrought aluminum alloy Al-5083 have been analyzed using experimental results and corresponding simulation outputs. The experiments are described by Boteler and Dandekar.<sup>2</sup> They are performed with a gas gun, which uses compressed gas to accelerate a flyer made of one material into a target made of another (or the same) material.<sup>2</sup> A schematic of this experimental setup is shown in Figure 1. The impact has enough energy to generate a shock wave within the target material whose characteristics are governed by the material and the nature of the impact. If the impact is characterized well, then velocity measurements using optical interferometry<sup>4</sup> are translated into information



**Figure 2.** Velocity profile from one experimental setup (black) and an ensemble of simulated velocity profiles generated using the FLAG hydrodynamics simulation (red). The blue dots on the experimental curve represent the different features on the velocimetry curve.

about the internal state of the material, such as stress, strain, pressure, and temperature using constitutive models for the elastic response<sup>5</sup> (reversible deformation) and plastic response<sup>3,6</sup> (irreversible deformation). In this work, there are three experiments under study that are labeled as shot 104S, shot 105S, and shot 106S, and output of shot 104S is shown in Figure 2 (in black).

Numerical hydrodynamic simulations of materials under intense thermodynamic conditions offer an alternative to shock physics experiments, which require considerable infrastructure, time, and financial support. Simulations can provide a quick indication of whether a material is unsuitable for a particular application due to its plasticity. Hydrodynamic simulations are validated by comparing their output to experimental results. In this simulation, there are total 11 tunable input parameters: five of these are the popular Johnson-Cook strength model<sup>6</sup> parameters ( $A$ ,  $B$ ,  $C$ ,  $X_n$ , and  $X_m$ ), three from varying the shear modulus ( $G_1$ ,  $\delta_2$ , and  $\delta_3$ ) for the three experiments, and the three corresponding impact velocities ( $v_1$ ,  $v_2$ , and  $v_3$ ). Simulations of velocity profiles from the impact of two Al-5083 plates were conducted using the FLAG hydrodynamics code<sup>7</sup> on the Los Alamos National Laboratory supercomputing platform Moonlight (308 Intel Xeon E5-267 nodes

and 4928 CPU cores). The ensemble of simulated velocity profiles that were analyzed for shot 104S is shown in Figure 2 (in red).

#### Features as Material Properties

Features in the velocity profiles are related to physical properties of the material, and accurate identification of these features is of great importance to the scientists. There are primarily four features used to measure these properties and validate simulations against experimental results. An example of these features is shown in Figure 2. Here, we provide a brief explanation of how each feature relates to the properties of the material.

- 1) *Jump off*: The jump-off is the time when the elastic wave reaches the rear surface of the target material. This time depends on the propagation of the elastic wave through the material, which is parameterized by the thickness, density, and speed of sound through the material.
- 2) *Elastic plateau*: Plastic deformation waves travel slower than elastic deformation waves. Following the impulse of acceleration from the elastic wave, the rear surface of the target material accelerates little until the arrival of the plastic wave; this is represented as a plateau in Figure 2. Materials with a higher yield stress will be able to convert more of the

impact energy into elastic deformation resulting in a higher elastic plateau.

- 3) *Elastic-plastic slope*: The slope at the arrival of the plastic wave is related to characteristics of the material's plastic deformation (e.g., strain hardening/softening, strain rate effects, temperature effects, etc.). Generally, a smaller slope indicates that the plastically deforming material is much less stiff than the elastically deforming portion.
- 4) *Plastic plateau*: The velocities at the elastic and plastic plateaus can be used to determine the velocity of the shock wave in the material. The speed of the shock wave in combination with equations for the conservation of mass and momentum can be used to estimate the internal state of the material to help determine under what conditions the material begins to plastically (irreversibly) deform.

Although these four features can be easily pointed out in a regularly shaped curve, it is possible for the simulation and experiment to generate curves that are very irregularly shaped and where the feature locations overlap. Due to this, feature extraction from these curves becomes challenging and uncertain.

## PROBLEM OVERVIEW AND SYSTEM REQUIREMENTS

Hydrodynamic modelers typically visually inspect an ensemble of velocity profiles, record the features for each velocity profile, perform validation against the experimental data, and analyze the input parameters to understand their effect on the output for tuning their values. This existing workflow can take up from days to weeks for each of the ensemble runs with moderate number of simulation runs (e.g., 1000 runs). A data analysis and visualization system that can enable the materials scientists to explore and understand these different aspects of their data is mostly lacking. To create a visualization system that can help answer the domain-specific questions, we first discussed with the domain experts regarding their existing data visualization needs and requirements. As noted from these discussions, the primary requirements of the intended system are as follows.

- 1) Accurate and automated identification of the features of the ensemble curves.

- 2) Importance (i.e., sensitivity) analysis of the input parameters such that more important parameters can be tuned earlier.
- 3) Exploration of simulated output to identify the suitable parameter combinations that produce data similar to the experiments.
- 4) Fast and easy query mechanism of the features/curves.

## SYSTEM OVERVIEW

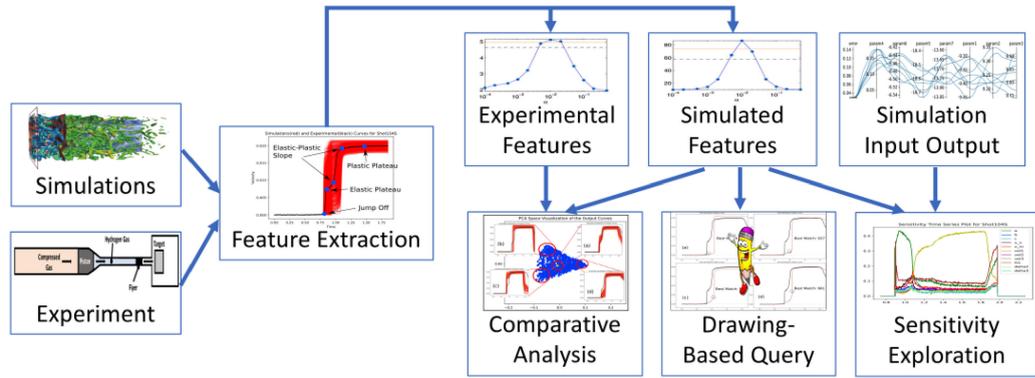
A schematic of our proposed workflow is shown in Figure 3. Given an ensemble of simulations and their corresponding experiments, we apply a feature detection algorithm to extract the material properties from the velocity profiles. Since these features are uncertain, we devise a statistical Gaussian mixture model (GMM)-based method for fast and accurate identification of the features. Since there exist multiple uncertain features, a comparison of different simulation runs with their experimental data requires a nontrivial feature comparison step. We employ PCA to reduce the dimensionality of the velocimetry time-series data and provide a 2-D view of the simulations and the experiments for interactive exploration. With the extracted features and simulation input parameters, we now apply detailed sensitivity analysis within and across the range of input parameters and extracted features. PCPs and an interactive drawing-based query mechanism aid in the exploration process. The use of innovative, yet simple, visualization and analysis tools helps in guiding the exploration of the high-dimensional shock physics datasets.

## UNCERTAIN FEATURE DETECTION

Velocity profiles are important to materials scientists since the location of features in this time series stands for the different properties of the material. There is no generally accepted method for finding features that will work for all cases, though there is some research in that direction.<sup>8</sup> In this work, we propose a GMM algorithm to solve our domain-specific problem. Next, we briefly describe our novel GMM-based automated method to identify these features.

### Feature Finding Method

We have developed a statistical approach to detect these four features. In our proposed

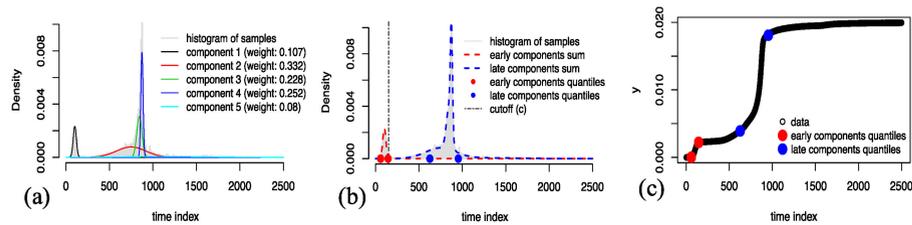


**Figure 3.** Overview of the proposed system. In this work flow, simulations and experimental datasets are used for initial feature extraction using our GMM-based approach, which is then further analyzed for understanding its sensitivity toward the input parameters. Our system also allows the users to query for features and hand-drawn curves in real time using PCA- and KNN-based approaches. PCP is used for high-dimensional visualization of the input space.

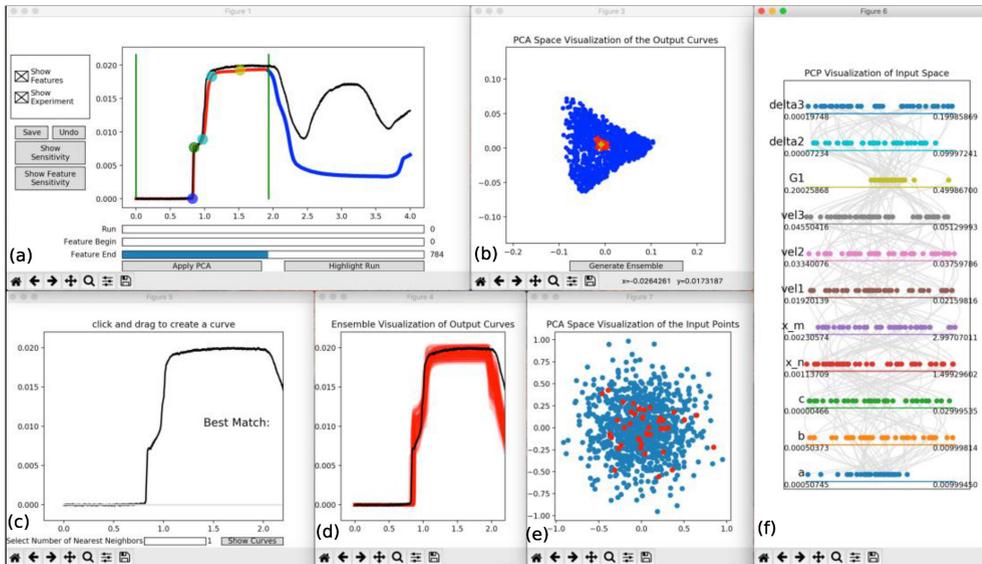
method, the  $N$  velocity profiles  $y_i(t)$ ,  $i \in 0, \dots, N$  are treated as cumulative density functions (CDFs), and we treat their derivatives  $y'_i(t)$  as probability density functions (PDFs). The PDFs are then modeled as a mixture of Gaussians. While it may appear that two mixture components would be sufficient after a visual inspection in Figure 4, we use more mixture components in order to 1) capture tail behavior, and 2) accurately model the CDF when there are clearly more than two jumps in  $y(t)$ . Figure 4(a) shows five mixture components for one velocity profile. The four features that describe the deformation properties of a material on a curve  $y_i(t)$  are obtained by finding certain quantiles from groups of mixture components. We use quantiles in the tails of the components instead of means because they correspond to places where  $y'_i(t)$  is nearing zero, and hence,  $y_i(t)$  is flattening out. These are the points of interest to the domain scientists.

We split the five mixture components into two groups, which we call the early and late

groups. If  $\mu_j + 2\sigma_j < c$  (where  $\mu_j$  is the mean, and  $\sigma_j$  is the standard deviation of the  $j$ th Gaussian component), component  $j$  is assigned to the early group, indicating that most of the mass of the component occurs before  $c$ . The cutoff  $c$  is recognized visually when all the data are plotted together (a time point between the elastic plateau and the first elastic-plastic slope features). The jump-off and elastic plateau features are the 0.01 and 0.99 quantiles of the early components. These quantiles can be obtained by rescaling the early components so that the weights add up to one, integrating the summed components to get a CDF and then inverting that CDF. The slope features are the 0.1 and 0.9 quantiles of the late components. An example of early and late groupings, as well as the corresponding feature locations, is shown in Figure 4(b). The plastic plateau is the 0.995 percentile of the original CDF  $y(t)$ . The corresponding detected feature points are shown in Figure 4(c).



**Figure 4.** (a) We approximate the density function with a mixture of Gaussians. (b) We use a five-component mixture and separate the components into two groups—early and late components. Features correspond to certain quantiles from the groups. (c) Identified features on the top of the original data.



**Figure 5.** Overview of the proposed system: (a) initial simulation/experiment explorer window, (b) output principal component analysis (PCA) space where proximity represents similarity in the velocimetry curves, (c) users can draw free-form curves for flexibly querying different velocimetry curves, (d) this window shows the output of the queries made in the window(c) by drawing, (e) PCA space showing the input parameter combinations, and (f) visualization of input parameter combinations using the parallel coordinates plot (PCP) for interparameter relationship exploration.

### Feature Visualization, Refinement, and Validation

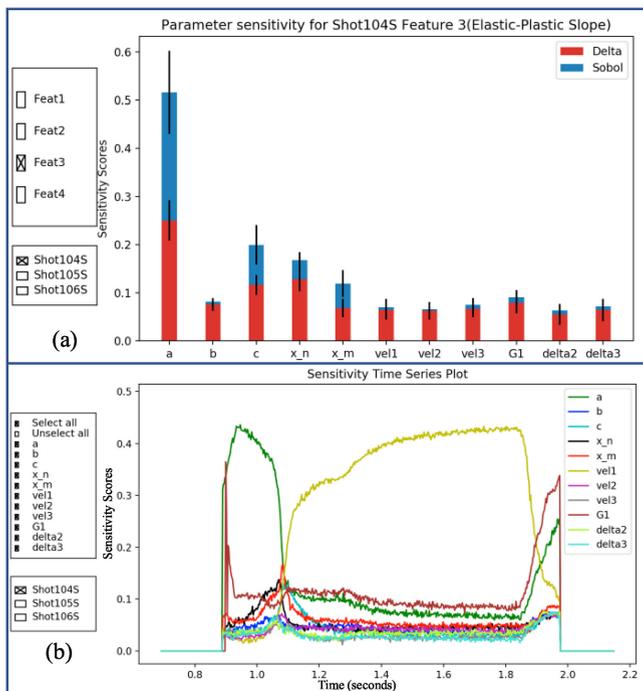
Following the previously mentioned method, features are extracted from the ensemble of simulation and experimental velocity profiles and presented to the user, as shown in Figure 5(a). The blue point is the jump off, green is the elastic plateau, the cyan points are the two end points for the elastic-plastic slope calculation, and the yellow point is the plastic plateau. Using our interface, users can choose to observe all these feature locations for different simulations and experiments by clicking buttons and cycling through the simulation runs. Since feature finding has uncertainty, we provide the option for users of this system to refine each feature. Users can zoom into the feature locations, drag the feature points to the desired locations, undo the last drag, and save the features to a file on the disk. Using this input from materials scientists as the ground truth, we compared our proposed feature extraction method with simpler automated methods (such as trying to find the feature locations following the feature definitions) and our proposed method has consistently showed higher accuracy, specifically in handling the irregularly shaped curves.

### EXPLORATION OF PARAMETER IMPORTANCE

#### Feature Sensitivity

We would like to understand the importance of each input parameter on the set of features we extract from the simulated velocity profiles. Sensitivity studies are a popular method for quantifying the uncertainty of the output due to each input parameter. Here, we use two popular global sensitivity methods: Delta<sup>10</sup> and Sobol.<sup>11</sup> For both of these methods, a higher value represents higher importance for the corresponding parameter in deciding the underlying feature. Knowing the sensitivity values, it becomes easier for the scientists to identify and tune the more important parameters, thus saving valuable time.

If we assume each time step of the velocity profile is an independent feature, then we can compute the sensitivity of the output due to each parameter at that time. Since analysts have a general idea where each feature occurs in time, this can be thought of as an implicit method to understand which parameters influence a particular feature the most. For each shot, we compute the sensitivity at each feature [see Figure 6(a)]



**Figure 6.** (a) This figure shows the sensitivity information based on feature 3 (elastic–plastic slope). Here, it is shown that parameter “a” (strength model parameter from the Johnson–Cook strength model) is the most important in deciding the elastic–plastic slope of the simulations velocimetry curves. (b) This figure shows the time-varying sensitivity information as a generalized version of plot (a). The higher sensitivity scores here indicate that the corresponding input variables become important in deciding the velocity values of the velocimetry curves at the varying time steps. This agrees with the results from (a) and also shows that the impact velocity (vel1) has a strong impact on the plastic plateau. Users can interact with plots of (a) and (b) using the toolbars on the left panel for more detailed exploration.

as well as the sensitivity as a function of time [see Figure 6(b)]. For feature-based sensitivity, we have employed the popular stacked bar charts for its widespread popularity and ease of interpretation when comparing multiple quantities. For time-varying sensitivity, we use time-series sensitivity plots. Figure 6(a) and (b) show examples of this sensitivity analysis using simulations of shot 104S. Our interface allows the user to interactively display this sensitivity information for each shot. This enables the user to comparatively explore the importance of each parameter and across multiple shots, and as shown in Figure 6(b), the importance of each parameter is time dependent.

## Interactive Exploration

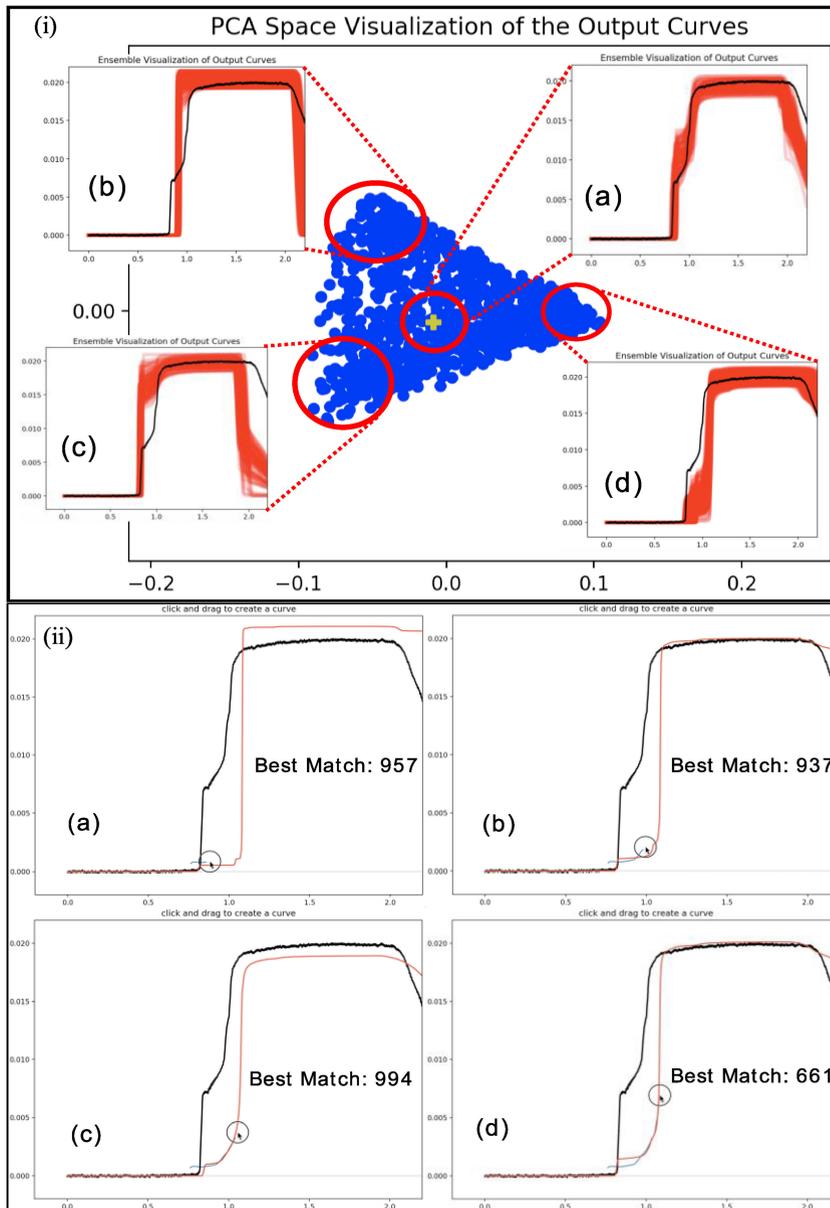
Using our visualization tool, users are able to interactively explore the different aspects of parameter importance via the sensitivity study. We provide simple selection tools [as shown in the left panel in Figure 6(a) and (b)] to facilitate the comparison across multiple shots, features [see Figure 6(a)], and input parameters [see Figure 6(b)] for comparative analysis. Users can choose to explore the time series or the feature-based sensitivity values in order to gain insight into the importance of the input parameters across the different shots and parameters. For example, using toolbars in Figure 6(b), users may wish to select the shots 104S and 105S and the parameters  $a$  and  $v_1$  to explore their sensitivity across the two different shots. It should be noted that different parameters show varying trends across time for different shots. Simple and intuitive interactions allow materials scientists to thoroughly explore this varying sensitivity information.

## COMPARATIVE EXPLORATION AND SYSTEM INTEGRATION

### PCA- and PCP-Based Exploration

PCA<sup>12</sup> is a popular method for high-dimensional data reduction and visualization, and it has been widely used for feature extraction, face recognition, variance analysis, and machine learning. If a set of high-dimensional data points are similar or have a small distance in the higher dimension, then this relative distance is often preserved in the lower dimensional PCA space. We use PCA in our system to enable the users to compare and validate the experimental output with the simulated output in an interactive way.

In our system, each velocity profile  $y_i(t)$  is a high-dimensional vector of size  $M$ . So, each velocity profile can be thought of as a point in the  $M$ -dimensional vector space. For validation purposes, we take all the simulation and the experimental outputs together in a matrix of  $(N + k) \times M$  dimensions where there are  $N$  simulations and  $k$  experiments. Then, we apply the PCA-based dimensionality reduction on this data matrix and project them down to two dimensions to present the results to the users and facilitate user interaction. In this PCA-based dimensionality reduction, the two principal PCA dimensions retain more



**Figure 7.** Different exploration and validation methods: (i) PCA space exploration for similarity based validation and analysis. Using this tool, users can quickly identify which simulated velocimetry curves are similar/dissimilar to the experimental output (physical reference experiment shown as the yellow cross) and find out their corresponding input parameters. (ii) User drawing for querying velocimetry curves with desired features. In this example, the user is looking for the curves with a low elastic plateau.

than 95% of the original information as found by computing the PCA\_explained\_variance, and this produces a good quality visualization for comparison purposes.

An example of this is presented in Figure 7(i). In this case, we have  $N = 1000$  simulations (shown by blue dots) and  $k = 1$  experiment (shown by the yellow plus) with  $M = 1600$  points

on each velocity profile  $y_i(t)$ . If the users want to select the curves that are similar to the experiment, then using a mouse they can select the points near the yellow plus; as shown in window (a) in Figure 7(i), all the curves similar to the experiment can be selected. On further inspection, since proximity in the PCA space suggests similarity, users can also select the curves that

are similar to each other but different from the experiment, e.g., as shown in windows (b), (c), and (d). For example, all the curves with a low elastic plateau are found in window (d), and the combination of the input parameters that generate these curves can be easily highlighted in a PCP. Similarly, velocity profiles with higher elastic plateau can also be quickly found from this visualization, as shown in windows (b) and (c).

The full system view is shown in Figure 5. In Figure 5(a), users can interactively select their region of interest for the curves. Then, the PCA method can be used to interactively compare the selected regions of the simulated curves with the experimental curve. Users can move the green vertical lines in Figure 5(a) to select a timespan and apply the PCA method to observe the output in the window shown in Figure 5(b). When the user selects a set of points using a lasso-based selector in this window [see Figure 5(b)], then those selected points are highlighted in red. After performing this selection, users can click on “Generate Ensemble” to visualize the collection of velocity profiles that correspond to their selected points in window (d). The input parameter combinations of the selected outputs can be visualized in windows (e) and (f) in Figure 5. Window (e) provides the PCA-reduced visualization of the input parameters such that users can explore which subspaces produce the desired velocity profiles. Window (f) is the PCP for the corresponding input parameters. In this window, users can have a detailed view of all the parameter values that produced the user-selected curves, and they can further interactively select subsets of the different parameter values to explore any hidden relationships.

#### Exploration Through User Drawing

Apart from using the PCA-based curve selection process and validation, our proposed system allows direct user input via free-hand drawing. Sketch-based image and shape retrieval has gained much popularity in the recent years.<sup>12</sup> In this work, we take up a similar idea to aid the users of our proposed system in finding velocimetry curves with user-defined features from the simulation ensemble output curves. The domain experts often need to query for a certain kind of velocity profile (e.g., low/high elastic/plastic slope). Using a free-hand drawing-based query system allows

free-form and easy feature description. This facilitates identification of the expected and the unexpected velocity profiles from the simulations and understanding the input parameter combinations that generate such velocity profiles.

In window (c) in Figure 5, users can use their finger (on a touch-enabled device) or computer mouse to draw the shape of the curve they would like to see in the simulations. At each stroke, our system finds the closest matching curves from the simulations database and displays them overlapped with the users drawing. In order to achieve this functionality, we use a KNN algorithm to find the best match (i.e., setting  $k = 1$ ). A more detailed example of this is shown in Figure 7(ii). In the windows (a–d) in Figure 7(ii), it is shown how the system-generated prediction (shown in red) changes in real time as the user draws more portions of the curve (shown in blue). The run number is also highlighted in the process. To enable more precise feature query, the time axis and the experimental curve (shown in black) are shown in the drawing window.

To implement drawing-based queries, we apply the Euclidean-distance-based similarity scheme for only the timescale where the user has provided the drawn input. We retrain the KNN algorithm at each stroke and find the closest neighbor to the user’s input. After the users have drawn the curve of their interest, they can also query for a collection of similar looking simulation curves by setting the slider “Number of Nearest Neighbors.” The ensemble of these  $k$  matches will be shown in window (d) in Figure 5 in red. In both the windows (c) and (d), the experimental curve is always displayed in black.

#### EXPERT FEEDBACK

We received a very positive feedback from the users of this tool (the domain experts). According to them, previous attempts to parameterize the shock physics simulations of this study prior to using this new data visualization tool involved individually changing one parameter at a time. This process was time consuming since each change to a parameter involved rerunning the simulation and postprocessing the data. This produced a new curve approximately every 10 min. This process would be repeated for each tunable parameter until a qualitatively good fit to the

experimental data was achieved. The process may take only a few iterations for completely decoupled parameters. In this case, parameters had coupled effects, which required readjustment of previously optimized parameters. For this model, with only five tunable parameters, the entire process consumed 10–20 h of effort.

The new process takes the same amount of time to setup the initial input deck to the simulations. However, hundreds or thousands of simulations with varied input parameters could be run simultaneously. Running multiple simulations in parallel can take the same time as before, but the real gain is that there is no human interaction required between individual simulations. The old method required constant interaction with the simulations and their outputs. The new tool presents all of the simulation results together in a dynamic, interactive environment. Here, the effects of individual and coupled parameters on the resulting output can be easily explored. Finding the best match of input parameters to a desired output (through PCA-based visualization or using hand-drawn target curves) takes minutes or less. Sensitivities of individual parameters could also be quickly deduced: something that would be difficult or impossible to do using static images of the results. Additionally, parameter optimization would become intractable with more complex models involving perhaps dozens of input variables. Furthermore, the previous manual feature finding endeavors required intimate knowledge of the data and used to cost in the order of minutes for each output curve. Our proposed feature finding method enabled a more precise material property extraction even in the case of the very complicated velocity profiles, taking only order of seconds for a set of thousand curves.

## CONCLUSION

In this paper, we presented a workflow for analyzing the shock physics datasets for assisting materials scientists. Over multiple discussions with the scientists, we formulated the requirements of the workflow and designed a system for them. We enabled the extraction of the material properties as the uncertain features from the velocity profiles. We employed the sensitivity methods to compare the importance of the input parameters of shock physics simulations for

multiple features as well as a function of time. We incorporated the PCA-based analysis for the validation of the simulations against the corresponding experiments. In our system, we enable the users to query for the features of interest via intuitive drawing using touch-screen-enabled devices. We worked closely with materials scientists throughout the project and gathered their feedback regarding our proposed system that shows its efficacy.

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