

For midterm exams, place your problem solutions and your copy of the exam inside this cover and give it to the exam proctors.

For final exams, place only your scratch notes inside this cover and place it inside the "Physics 121" box just outside the exam collection area. Hand your copy of the exam and your answer sheet to the exam proctors.

All exams closed book and notes except for the information on this cover. You may write whatever you like on it, but you are allowed only one cover for the entire semester. You may also bring the "Physics 121 Math reference" if you leave it inside this cover when you hand it in.

We presume that you have neither given nor received unauthorized assistance and that your conduct on this exam is in harmony with the BYU honor code. Please tell us if this is not the case.

Chapter 2 Outline — Motion in One Dimension

Position

Coordinates: origin, + direction

$x(t) \stackrel{\text{def}}{=} x$  at time  $t$ .

Average Speed

average speed  $\stackrel{\text{def}}{=} \frac{\text{total distance}}{\text{total time}}$ .

Displacement

$\Delta x \stackrel{\text{def}}{=} x_{\text{final}} - x_{\text{initial}}$ .

Average Velocity

$\bar{v} \stackrel{\text{def}}{=} \frac{\text{displacement}}{\text{time interval}} \stackrel{\text{def}}{=} \frac{\Delta x}{\Delta t}$   
 = slope of line between points on  $x$  vs.  $t$  curve.

Velocity

$v \stackrel{\text{def}}{=} \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} \stackrel{\text{def}}{=} \frac{dx}{dt}$  = slope of  $x$  vs.  $t$  curve  $\iff \Delta x = x_f - x_i = \int_i^f v dt$ .

Acceleration

$a \stackrel{\text{def}}{=} \lim_{\Delta t \rightarrow 0} \frac{\Delta v}{\Delta t} \stackrel{\text{def}}{=} \frac{dv}{dt}$  = slope of  $v$  vs.  $t$  curve  $\iff \Delta v = v_f - v_i = \int_i^f a dt$ .

Constant Acceleration

If (and only if) acceleration is constant:  
 $v = v_0 + at$        $x - x_0 = v_0 t + \frac{1}{2}at^2$   
 $x - x_0 = \frac{1}{2}(v + v_0)t$        $v^2 = v_0^2 + 2a(x - x_0)$

Free Fall

For free fall with no aerodynamic forces.  $a \stackrel{\text{law}}{=} -g$  for all objects, presuming that  $\uparrow$  is the positive direction.  
 $g = 9.80 \text{ m/s}^2 \approx 32 \text{ ft/s}^2$ .

Chapter 4 Outline — Motion in Two Dimensions

Definitions:

Position:  $\vec{r} \stackrel{\text{def}}{=} x\hat{i} + y\hat{j} + z\hat{k}$

Displacement:  $\Delta \vec{r} \stackrel{\text{def}}{=} \Delta x\hat{i} + \Delta y\hat{j} + \Delta z\hat{k}$

Velocity:  $\vec{v} \stackrel{\text{def}}{=} \frac{d\vec{r}}{dt} = \frac{dx}{dt}\hat{i} + \frac{dy}{dt}\hat{j} + \frac{dz}{dt}\hat{k} = v_x\hat{i} + v_y\hat{j} + v_z\hat{k}$

Acceleration:  $\vec{a} \stackrel{\text{def}}{=} \frac{d\vec{v}}{dt} = \frac{dv_x}{dt}\hat{i} + \frac{dv_y}{dt}\hat{j} + \frac{dv_z}{dt}\hat{k} = a_x\hat{i} + a_y\hat{j} + a_z\hat{k}$

For constant acceleration (vector form):  $\vec{v} = \vec{v}_0 + \vec{a}t$  and  $\vec{r} - \vec{r}_0 = \vec{v}_0 t + \frac{1}{2}\vec{a}t^2$

For free fall with  $\vec{a} \stackrel{\text{law}}{=} a \text{ constant} = -jg$ ,

$$\begin{matrix} v_{x0} = v_0 \cos \theta_0 & a_x = 0 & v_x = v_{x0} & x - x_0 = v_{x0}t \\ v_{y0} = v_0 \sin \theta_0 & a_y = -g & v_y = v_{y0} - gt & y - y_0 = v_{y0}t - \frac{1}{2}gt^2 \end{matrix}$$

Derived Free-fall results: (Be very careful! — These are for very specific situations.)

The trajectory:  $y = (\tan \theta_0)x - \left(\frac{g}{2v_0^2 \cos^2 \theta_0}\right)x^2$ , ( $\hat{a}$  parabola)

The horizontal range and maximum height:  $R = \frac{v_0^2}{g} \sin 2\theta_0$ ,  $h = \frac{v_0^2 \sin^2 \theta_0}{2g}$ .

Speed  $v$  as a function of time:  $v^2 = v_x^2 + v_y^2 = v_{x0}^2 + (v_{y0} - gt)^2$

Speed  $v$  as a function of  $y$  and  $x$ :  $v^2 = v_0^2 - 2g(y - y_0)$

Acceleration in Uniform Circular Motion:

$a_r = \frac{v^2}{r}$ , directed toward the center of the circle.

Tangential and Radial Acceleration:

$\vec{a} = \vec{a}_r + \vec{a}_t$ , with

$a_r = \frac{v^2}{r}$ , directed toward the center of the circle.

$a_t = \frac{dv}{dt}$ , directed toward the direction of motion.

Relative Motion:

Relative velocity:  $\vec{v}_{BA} = \vec{v}_{BC} + \vec{v}_{CA}$

Relative acceleration  $\vec{a}_{BA} = \vec{a}_{BC}$  if  $\vec{a}_{CA} = 0$

Vector Differentiation

Rectangular form:  $\frac{d\vec{V}}{dt} = \frac{dV_x}{dt}\hat{i} + \frac{dV_y}{dt}\hat{j} + \frac{dV_z}{dt}\hat{k}$ .

Polar form: with  $\vec{V} = (V, \theta)$ ,  $\frac{d\vec{V}}{dt} = \frac{dV}{dt}\hat{u}_R + V\frac{d\theta}{dt}\hat{u}_\perp$ .

Chapters 5 and 6 Outline — The Laws of Motion

I. Newton's First Law — The First Law of Motion

A free object moves with  $\vec{a} \stackrel{\text{law}}{=} 0$  ( $\vec{v} \stackrel{\text{law}}{=} \text{constant}$ ).  
 If at rest, it remains at rest.  
 If moving, it continues to move in a straight line with constant speed.  
 The first law is a statement specifying an inertial reference frame.

II. Some Definitions

Acceleration:  $\vec{a} \stackrel{\text{def}}{=} \frac{d\vec{v}}{dt}$

Force ( $\vec{F}$ )  
 Push or pull  
 Whatever can cause acceleration  
 Measured in newtons (N) or pounds (lb)  
 A vector quantity

For the same object,  $\vec{F}_a \stackrel{\text{def}}{=} \frac{\vec{a}_a}{a_a} F_a$ .  
 (Defines an unknown force in terms of a standard force)

Inertial Mass ( $m$ )

A measure of how an object accelerates in response to force.  
 Measured in kilograms (kg) or slugs  
 A scalar quantity  
 For the same force acting,  $m_a \stackrel{\text{def}}{=} \frac{a_a}{a_s} m_s$ .  
 (Defines the mass of an unknown object in terms of a standard mass.)

III. Newton's Second Law — The Second Law of Motion

In an inertial reference frame:  
 1. Accelerations are caused by forces.  
 2.  $\vec{a} = \vec{F}/m$ , or  $\vec{F} = m\vec{a}$  (for consistent units)  
 3.  $\vec{a}$  is in the same direction as  $\vec{F}$ .  
 4. The  $\vec{F}$  in (2) is the vector sum  $\Sigma \vec{F}$  of all the forces acting on the object;  
 the second law in its full glory is  
 In an inertial frame,  $\vec{a} \stackrel{\text{law}}{=} \frac{\Sigma \vec{F}}{m}$  or  $\Sigma \vec{F} \stackrel{\text{law}}{=} m\vec{a}$ .

IV. Newton's Third Law — The Third Law of Motion

(A law describing forces)

- All forces result from interactions between pairs of objects.
- In every interaction there are two forces, ONE ON EACH OBJECT.
- $\vec{F}_{12} \stackrel{\text{law}}{=} -\vec{F}_{21}$ .  
 (The two forces have equal strength and act in opposite directions.)

V. Finding Forces

- Long-range interactions  
 gravity, electromagnetic.  
 ( $\vec{w} \stackrel{\text{def}}{=} m\vec{g} = -mg\hat{j}$  near Earth's surface.)
- Contact interactions  
 electromagnetic, nuclear  
 (tension, friction, 'normal' forces, springs, all other forces)  
 For a "Hooke's law" spring,  $F_{\text{spring}} \stackrel{\text{law}}{=} -kx$ .  
 For friction,  $f_s \leq \mu_s n$  and  $f_k \stackrel{\text{law}}{=} \mu_k n$ .  
 The buoyant force:  $\vec{B} = m_f(\vec{a}_f - \vec{g})$   
 For viscous drag at low speed:  $\vec{R} \stackrel{\text{law}}{=} -b\vec{v}$ ; at higher speeds:  $\vec{R} \stackrel{\text{law}}{=} \frac{1}{2} D \rho A v^2 (-\hat{v})$ .

In most cases tension  $T$  and the 'normal' component  $n$  of a contact force can be found only by using the 2nd law of motion. The same is true of static friction unless you know that  $f_s = \mu_s n$ .

Chapter 7 Outline — Work and Energy

The work-kinetic energy theorem:

For any object,  
 $\Delta K \stackrel{\text{law}}{=} \Sigma W \stackrel{\text{def}}{=} W_{\text{net}}$

Definitions:

$$\Delta K \stackrel{\text{def}}{=} K_{\text{final}} - K_{\text{initial}} \stackrel{\text{def}}{=} \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$$

$$W \stackrel{\text{def}}{=} \int_{\text{initial}}^{\text{final}} \vec{F}_s \cdot d\vec{s} \stackrel{\text{def}}{=} \int_i^f \vec{F}_s \cdot d\vec{s} \stackrel{\text{def}}{=} \lim_{\Delta s \rightarrow 0} \sum \vec{F}_s \cdot \Delta \vec{s}$$

Special Cases:

- $F = \text{constant}$ :  $W = \vec{F} \cdot \vec{d} = F \cdot \Delta r$   
 e.g.:  $W_g = -mg(y_f - y_i)$  for  $\vec{F}_g = -mg\hat{j}$
- 1-dimensional motion:  
 $W = \lim_{\Delta x \rightarrow 0} \sum F_x \Delta x \stackrel{\text{def}}{=} \int_i^f F_x dx$   
 e.g.:  $W_H = -\frac{1}{2} k(x_f^2 - x_i^2)$  for  $\vec{F}_H = -kx\hat{i}$ . (Hooke's law spring)
- $W = 0$  if  $\vec{F} \perp d\vec{s}$

The Scalar Product:

$$\vec{A} \cdot \vec{B} \stackrel{\text{def}}{=} A_x B_x + A_y B_y + A_z B_z$$

$$= AB \cos \theta = AB_{\parallel} = A_{\parallel} B$$

$$A^2 = \vec{A} \cdot \vec{A} = A_x A_x + A_y A_y + A_z A_z$$

Power:

$$P \stackrel{\text{def}}{=} \lim_{\Delta t \rightarrow 0} \frac{\Delta W}{\Delta t} = \vec{F} \cdot \vec{v}$$

Conservation of Momentum:

for an isolated system. ( $\vec{F}_{\text{ext}} = 0$ )  
 $\vec{p}_f \stackrel{\text{law}}{=} \vec{p}_i$  or  $\Delta \vec{p} \stackrel{\text{law}}{=} 0$  or  $\frac{d\vec{p}}{dt} \stackrel{\text{law}}{=} 0$

Definition of momentum:

for a particle  $\vec{p} \stackrel{\text{def}}{=} m\vec{v} \iff K \stackrel{\text{def}}{=} \frac{p^2}{2m}$

For a system  $\vec{P} \stackrel{\text{def}}{=} \sum_{k=1}^N \vec{p}_k \stackrel{\text{def}}{=} \vec{p}_{\text{tot}} \stackrel{\text{def}}{=} M\vec{v}_{\text{cm}}$ .  
 (Warning:  $K_{\text{total}}$  is not always equal to  $\frac{P^2}{2M}$ .)

2nd Law of Motion and the Impulse-Momentum Theorem:

particle:  $\frac{d\vec{p}}{dt} \stackrel{\text{law}}{=} \Sigma \vec{F} \iff \Delta \vec{p} \stackrel{\text{law}}{=} \Sigma \int \vec{F} dt \stackrel{\text{def}}{=} \Sigma \vec{I}$   
 system:  $\frac{d\vec{P}}{dt} = M\vec{a}_{\text{cm}} \stackrel{\text{law}}{=} \Sigma \vec{F}_{\text{ext}} \iff \Delta \vec{P} \stackrel{\text{law}}{=} \Sigma \int \vec{F}_{\text{ext}} dt \stackrel{\text{def}}{=} \Sigma \vec{I}_{\text{ext}}$

The integral forms of these equations are the impulse-momentum theorems.

Center of mass:

$M\vec{r}_{\text{cm}} \stackrel{\text{def}}{=} \sum_{k=1}^N m_k \vec{r}_k$  for discrete particles.  
 $M\vec{r}_{\text{cm}} \stackrel{\text{def}}{=} \int \vec{r} dm$  for continuous systems

Chapter 8 Outline — Conservation of Energy

If a Physical Quantity  $X$  is conserved for an isolated system

$$\Delta X \stackrel{\text{law}}{=} 0 \text{ or } X_{\text{final}} \stackrel{\text{law}}{=} X_{\text{initial}} \text{ or } X \stackrel{\text{law}}{=} \text{constant} \text{ or } \frac{dX}{dt} \stackrel{\text{law}}{=} 0$$

Conservation of Energy:

For an isolated system,  
 $\Delta E \stackrel{\text{law}}{=} 0$  or  $E_{\text{final}} \stackrel{\text{law}}{=} E_{\text{initial}}$  or  $\frac{dE}{dt} \stackrel{\text{law}}{=} 0$ .

Definitions:

$E \stackrel{\text{def}}{=} \Sigma K + \Sigma U + \Sigma U_{\text{int}} \stackrel{\text{def}}{=} \text{kinetic energy} + \text{potential energy} + \text{internal energy}$   
 $K \stackrel{\text{def}}{=} \frac{1}{2} m v^2 = \frac{1}{2} m \vec{v} \cdot \vec{v}$   
 $U_{\text{int}} \stackrel{\text{law}}{=} mc^2 = \text{A function of temperature, physical state, chemical state and nuclear structure.}$

Conservative Force: One which does not change internal energy. A force is conservative if the work it does on a particle depends only on the initial and final points of the motion, or, equivalently, if the work it does through every closed path is zero.

Potential Energy:

$U_g \stackrel{\text{def}}{=} mgy$  for  $\vec{F} = -mg\hat{j}$ . (near-Earth gravity)  
 $U_H \stackrel{\text{def}}{=} \frac{1}{2} kx^2$  for  $\vec{F}_H = -kx\hat{i}$  (Hooke's-law spring)  
 $U \stackrel{\text{def}}{=} -\frac{k}{r}$  for  $\vec{F} = -\frac{k}{r^2} \hat{r}$  (long-range attractive gravity and electrostatic forces)

General definition of  $U$  for a conservative force:

$$\Delta U \stackrel{\text{def}}{=} U_f - U_i \stackrel{\text{def}}{=} -W_{c,i \rightarrow f} \stackrel{\text{def}}{=} - \int_i^f \vec{F}_{c,s} \cdot d\vec{s}$$

Force from potential energy:

$$\vec{F}_s = -\frac{\partial U}{\partial \vec{s}}$$

Change in Internal Energy

$$\Delta U_{\text{int}} \stackrel{\text{def}}{=} U_{\text{int},f} - U_{\text{int},i} \stackrel{\text{def}}{=} -W_{\text{nc},i \rightarrow f} \stackrel{\text{def}}{=} - \int_i^f \vec{F}_{\text{nc},s} \cdot d\vec{s}$$

## Chapter 10 Outline — Rigid-body, Fixed-axis Rotation

### Dynamics:

Equation of Motion:  $\tau_{\text{net}} \stackrel{\text{def}}{=} \Sigma \tau \stackrel{\text{law}}{=} I \alpha$  with  $\tau \stackrel{\text{def}}{=} r F \sin \theta = F d = F r_{\perp} = \tau F_{\perp}$

Kinetic Energy:  $K = \frac{1}{2} I \omega^2$  for a rotating rigid body.  
 $= \frac{1}{2} I \omega^2 + \frac{1}{2} M v_{\text{center}}^2$  for a body rolling without slipping.

### Kinematics:

The angular variables:

angular position  $\theta \stackrel{\text{def}}{=} \frac{s}{r}$  radians, angular displacement  $\Delta \theta$ , angular velocity  $\omega \stackrel{\text{def}}{=} \frac{d\theta}{dt}$ ,  
 and angular acceleration  $\alpha \stackrel{\text{def}}{=} \frac{d\omega}{dt}$

These are mathematically analogous to the corresponding linear variables for one-dimensional motion  $\Delta x$ ,  $v \stackrel{\text{def}}{=} dx/dt$  and  $a \stackrel{\text{def}}{=} dv/dt$ .

Relations between linear and angular variables for angles in radians:  
 ( $r$  is the radius of a particle's circular motion):

$$\Delta s = r \Delta \theta, v = r \omega, a_{\text{tan}} = r \alpha, a_{\text{radial}} = \frac{v^2}{r} = r \omega^2 = v \omega.$$

Relations between angular units:

$$1 \text{ rev} = 2\pi \text{ rad} = 360^\circ.$$

For constant angular velocity,

$$f = \frac{1}{T} = \frac{\omega}{2\pi}, f \text{ in rev/s, } T \text{ in s, } \omega \text{ in rad/s.}$$

For rolling without slipping:

$$v_{\text{center}} = R \omega.$$

### Rotational Inertia:

General Definition:  $I \stackrel{\text{def}}{=} \Sigma \delta m r_{\perp}^2 \stackrel{\text{def}}{=} \int r_{\perp}^2 dm.$

The Parallel-axis theorem:  $I = I_{\text{cm}} + M d^2.$

Specific uniform bodies:

Solid sphere about a diameter:  $I = \frac{2}{5} M R^2$

Solid cylinder about symmetry axis:  $I = \frac{1}{2} M R^2$

Spherical shell about a diameter:  $I = \frac{2}{3} M R^2$

Solid cylinder about centered diameter:  $I = \frac{1}{4} M R^2 + \frac{1}{12} M L^2$

Thin rod, centered perpendicular axis:  $I = \frac{1}{12} M L^2$

Thin cylindrical shell about symmetry axis:  $I = M R^2$

with axis through one end:  $I = \frac{1}{3} M L^2$

Hollow cylinder about symmetry axis:  $I = \frac{1}{2} M (R_1^2 + R_2^2)$

Rectangular plate with perpendicular axis through its center:  $I = \frac{1}{12} M (a^2 + b^2)$

## Chapter 12 Outline — Static Equilibrium; Elasticity

### The two equilibrium conditions:

$$\text{Vector forms: } \Sigma \vec{F}_{\text{ext}} = 0 \quad (1), \quad \Sigma \vec{\tau}_{\text{ext}} = 0 \quad (2)$$

For coplanar forces:  $\Sigma F_{x,\text{ext}} = 0$  (1a),  $\Sigma F_{y,\text{ext}} = 0$  (1b),  $\Sigma \tau_{x,\text{ext}} = 0$  (2a).

If (1) and (2) are true for one inertial reference point, they are true for all reference points.

### Center of gravity:

The center of gravity is located at the center of mass if the object is in a uniform gravitational field.

## Chapter 13 Outline — Oscillatory Motion

### Kinematics:

$s(t) \stackrel{\text{def}}{=} A \cos(\Omega t + \phi)$  represents simple harmonic motion.

In words,

( $s$  at time  $t$ ) = (amplitude)  $\cos$ (angular frequency) $t$  + (phase constant)

$$v(t) = ds/dt = -A \Omega \sin(\Omega t + \phi)$$

$$a(t) = dv/dt = d^2s/dt^2 = -A \Omega^2 \cos(\Omega t + \phi) = -\Omega^2 s$$

$$\Omega^2 s^2 + v^2 = \Omega^2 A^2$$

$$\Omega = 2\pi f = 2\pi/T. \quad f \text{ is the frequency, } T \text{ is the period.}$$

### Equation of Motion:

Any equation of either of the forms

$$a = -\Omega^2 s \quad \text{or} \quad \Omega^2 s^2 + v^2 = \Omega^2 A^2,$$

with  $v = ds/dt$  and  $a = dv/dt$ ,

leads to SHM with

$$\Omega^2 = (\text{positive constant}) = (\text{angular frequency})^2.$$

### Spring-block Oscillator:

If  $F_x = -kx$ , the motion is simple harmonic with

$$\Omega = \sqrt{\frac{k}{m}}, \quad T = 2\pi \sqrt{\frac{m}{k}} \quad \text{and} \quad f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}.$$

The total energy is  $E = \frac{1}{2} k A^2.$

The potential energy is  $U = \frac{1}{2} k x^2 = \frac{1}{2} k A^2 \cos^2(\Omega t + \phi)$

The kinetic energy is  $K = \frac{1}{2} m v^2 = \frac{1}{2} k A^2 \sin^2(\Omega t + \phi)$

### The generality of SHM.

Almost all small departures from stable equilibrium exhibit SHM.

## Chapter 11 — Angular Momentum; Rolling

### Conservation of angular momentum:

$$\vec{L}_j \stackrel{\text{law}}{=} \vec{L}_i \quad \text{or} \quad \Delta \vec{L} \stackrel{\text{law}}{=} 0 \quad \text{or} \quad \frac{d\vec{L}}{dt} \stackrel{\text{law}}{=} 0$$

for an isolated system. ( $\vec{\tau}_{\text{ext}} = 0$ )

For any component  $z$ ,

$$L_{zj} \stackrel{\text{law}}{=} L_{zi} \quad \text{if} \quad \tau_z = 0.$$

### 2nd law of motion:

With  $\vec{\tau} \stackrel{\text{def}}{=} \vec{r} \times \vec{F}$ ,

$$\text{particle: } \frac{d\vec{L}}{dt} \stackrel{\text{law}}{=} \Sigma \vec{\tau} \quad \text{or} \quad \Delta \vec{L} \stackrel{\text{law}}{=} \Sigma \int \vec{\tau} dt$$

$$\text{system: } \frac{d\vec{L}}{dt} \stackrel{\text{law}}{=} \Sigma \vec{\tau}_{\text{ext}} \quad \text{or} \quad \Delta \vec{L} \stackrel{\text{law}}{=} \Sigma \int \vec{\tau}_{\text{ext}} dt$$

The integral forms of these equations are the angular impulse-momentum theorems.

### Definition of angular momentum:

$$\vec{L} \stackrel{\text{def}}{=} \vec{r} \times \vec{p} \stackrel{\text{def}}{=} \vec{r} \times m \vec{v} \quad \text{for a particle}$$

$$\vec{L} \stackrel{\text{def}}{=} \Sigma \vec{L}_k = (\vec{R} \times \vec{P}) + \vec{L}_{\text{cm}} = (\vec{R} \times M \vec{V}) + \vec{L}_{\text{cm}} \quad \text{for a system}$$

$$\vec{L} = I \vec{\omega} \quad \text{for a rigid body rotating about a principal axis.}$$

### Rolling:

For a symmetric object rolling without slipping:

$$v_{\text{center}} = R \omega \quad \text{and} \quad K = \frac{1}{2} I_{\text{cm}} \omega^2 + \frac{1}{2} M v_{\text{cm}}^2.$$

### The vector product $\vec{A} \times \vec{B}$ :

$$\text{If } \vec{A} \times \vec{B} = \vec{C}, \quad \vec{C} \stackrel{\text{def}}{=} |\vec{C}| \stackrel{\text{def}}{=} AB \sin \theta = AB_{\perp} = A_{\perp} B$$

$\vec{C}$  is perpendicular to  $\vec{A}$  and  $\vec{B}$

in the direction given by the right-hand rule.

In rectangular components,

$$\vec{A} \times \vec{B} \stackrel{\text{def}}{=} \begin{pmatrix} (A_y B_z - A_z B_y) \hat{i} \\ +(A_x B_z - A_z B_x) \hat{j} \\ +(A_x B_y - A_y B_x) \hat{k} \end{pmatrix} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix}$$

$$= -\vec{B} \times \vec{A}$$

## Chapter 14 Outline — The Law of Gravity

### A. The Law of Universal Gravitation

$$\vec{F}_{21} \stackrel{\text{law}}{=} \left( G \frac{m_1 m_2}{r^2} \right) (-\hat{r}_{12}), \quad G = 6.672 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2} \approx \frac{2}{3} \times 10^{-10} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}$$

Valid for points and uniform external spheres.

3<sup>rd</sup> Law := TRUE

Always attractive

Gravitational forces are vectors.

Superposition

### B. Geophysical Consequences

$g$  of the earth

motion of planets and satellites (Kepler's laws)

rotational motion of double star systems

structure of the large-scale universe.

### C. Gravitational Potential Energy

$$U_g \stackrel{\text{law}}{=} - \frac{G m_1 m_2}{r}$$

Examples: Free fall, Escape from the earth, Planets and satellites

Superposition

### D. The Gravitational Field

$$\vec{g} \stackrel{\text{def}}{=} \frac{\vec{F}_g}{m}$$

### E. The Principle of Equivalence

$$m_{\text{gravitational}} = m_{\text{inertial}}; \quad 1 \text{ part in } 10^{11}.$$

### Conversion Factors

#### Mass

$$1 \text{ kg} = 1000 \text{ g}$$
$$1 \text{ u} = 1.66 \times 10^{-27} \text{ kg}$$

#### Length

$$1 \text{ m} = 100 \text{ cm} = 3.28 \text{ ft}$$
$$1 \text{ mi} = 1.61 \text{ km} = 5280 \text{ ft}$$

#### Time

$$1 \text{ day} = 86,400 \text{ s}$$
$$1 \text{ year} = 3.16 \times 10^7 \text{ s}$$

#### Speed

$$60 \text{ mi/h} = 88 \text{ ft/s} \approx 26.8 \text{ m/s}$$
$$100 \text{ km/h} = 27.77 \text{ m/s} \approx 62.1 \text{ mi/h}$$

#### Angle

$$1 \text{ rev} = 360^\circ = 2\pi \text{ rad}$$

#### Force

$$1 \text{ N} = 0.225 \text{ pound}$$
$$1 \text{ pound} = 4.45 \text{ N}$$

#### Energy

$$1 \text{ eV} = 1.60 \times 10^{-19} \text{ J}$$
$$1 \text{ kcal} = 10^3 \text{ cal} = 4.19 \text{ kJ}$$
$$1 \text{ kW}\cdot\text{h} = 3.6 \times 10^6 \text{ J} = 3.6 \text{ MJ}$$

### Physical Constants

speed of light	$c$	$3.00 \times 10^8 \text{ m/s}$
gravitational constant	$G$	$\frac{2}{3} \times 10^{-10} \text{ N}\cdot\text{m}^2/\text{kg}^2$

#### For Earth:

free-fall acceleration	$g$	$9.80 \text{ m/s}^2$
mass	$M_E$	$5.98 \times 10^{24} \text{ kg}$
mean radius	$R_E$	$6370 \text{ km}$

### Metric Prefixes

<i>prefix</i>	<i>symbol</i>	<i>factor</i>
tera-	T	$10^{12}$
giga-	G	$10^9$
mega-	M	$10^6$
kilo-	k	$10^3$
milli-	m	$10^{-3}$
micro-	$\mu$	$10^{-6}$
nano-	n	$10^{-9}$
pico-	p	$10^{-12}$