Announcements – Oct 20, 2009

1. **Exam 3** starts one week from today
   a. Tuesday will be review session
   b. Exam covers HW 9-14. (HW 14 is due on Tuesday.)
   c. HW 15 not due until the following Wed, Nov 4.

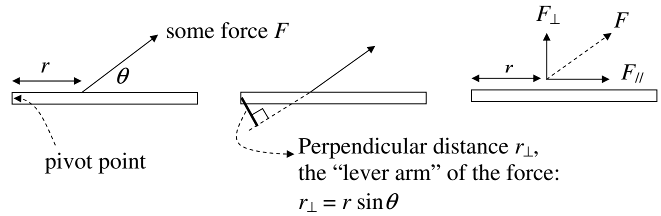
2. **TA-led evening review session**: To overcome limitations of in-class survey, we will use doodle.com. Everyone inputs which times work for them, it totals up things so that everyone can see which times the most numbers of students can make.
   a. I'll send around the survey link today.
   b. Please **vote on times by tomorrow night**. Then I can announce the decision Thursday in class, and I will still have a couple of days to get the room and TA scheduled.

3. **Today's Goal:** complete the connection between linear and angular quantities
   a. Distance $\rightarrow \theta$
   b. Velocity $\rightarrow \omega$
   c. Acceleration $\rightarrow \alpha$
   d. Force $\rightarrow \tau$
   e. Mass → ?? (today)
   f. Energy → ?? (today)
   g. Momentum → ?? (next time)

Review of Torques

Definition of torque: (about a point)

$$\tau_p = r_\perp F = rF_\perp = rF\sin\theta$$



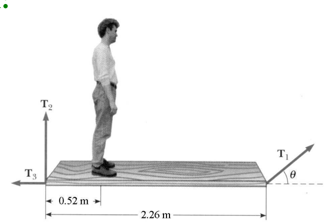
Positive/negative:
Produces a **clockwise** rotation = **negative**
Produces a **counter-clockwise** rotation = **positive**

Equilibrium

$$\sum F = 0$$
$$\sum \tau_p = 0$$

Translation:
- if an object is not speeding up or slowing down, there is no net force on it
- if an object is not speeding up or slowing down its *rotation*, there is no net *torque* on it.

One more equilibrium problem:
A uniform plank of length 2.26 m and mass 10 kg is balanced by three ropes as indicated in the figure, with θ = 35°. A 75 kg person is standing 0.52 m from the left end. Find the tensions in all three ropes.



Answers: 380.3 N, 311.5 N, 614.9 N

Rotational kinetic energy

Clicker quiz: (warmup) Demo…a cart races a ball. Who wins?
a. cart
b. ball
c. tie

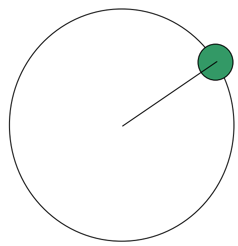
Review: How fast is **cart** going at bottom? (Energy)

How long did it take to get there? (Kinematics)

→ What's different about the ball?

Kinetic energy of a **"point mass"** rotating in a circle:

Write in terms of ω:



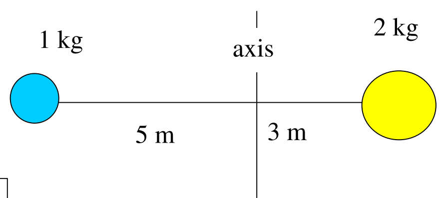
"Moment of inertia"

$$I_{pt\ mass} = mr^2$$ (rotating in a circle)

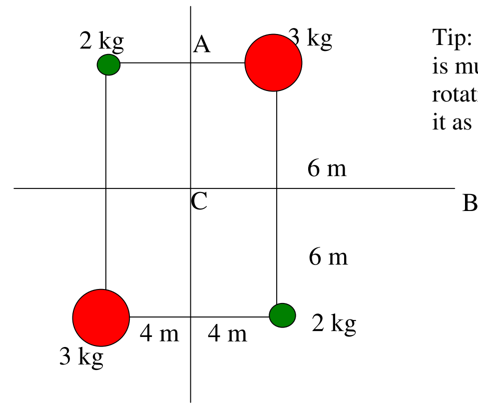
Kinetic energy in terms of I and ω:

$$KE_{rot} = \frac{1}{2} I\omega^2$$

Moment of inertia for two masses? (connected with a rod)



$$I = I_1 + I_2 + \ldots$$



Tip: If size of object is much smaller than rotation radius, treat it as a "point mass"

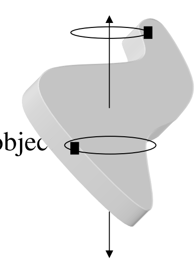
Clicker quiz: Does *I* change when you rotate about axis A vs. axis B?

a. About axis A has larger *I*
b. About axis B has larger *I*
c. They have the same *I*

What about axis C? (C is into the page)

Demo: variable "I-rotator"

Rotating "extended" objects

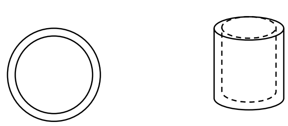


Must add up mr^2 *for each bit of mass* in the object

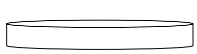
Which bits of mass contribute the most to *I*?

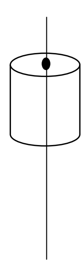
Which of these objects will have the largest I?

Hoop/cylindrical shell

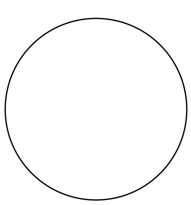


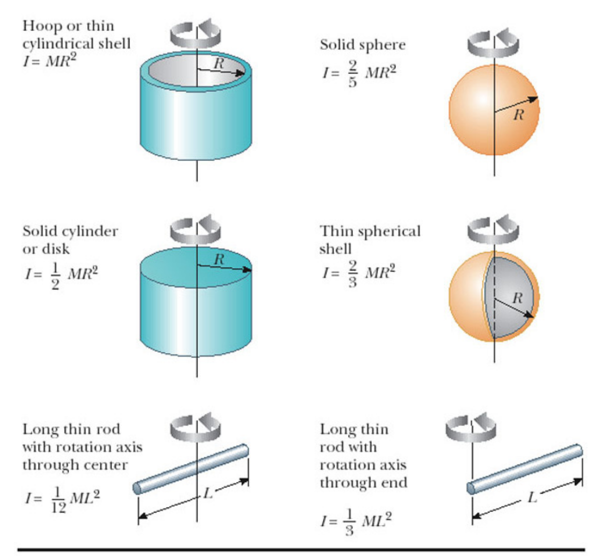
Solid disk/cylinder





Solid sphere





From warmup. Moment of inertia is biggest for:

a. compact objects
b. objects that are spread out
c. neither; doesn't depend on shape

Demo: Long & short "I-bars"

Clicker quiz: Which kind of rolling object will be moving the <u>fastest</u> at the bottom of an incline?

a. Hoop
b. Solid disk
c. Sphere
d. They will all tie
e. Can tell; it depends on size and mass

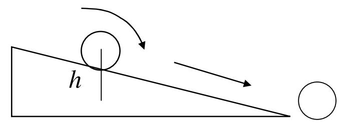
→ Which object will get there first?

Demo: racing objects down incline

Clicker quiz: If they continued on, which would go the farthest up a hill on the other side?

a. Hoop
b. Solid disk
c. Sphere
d. All the same height at the end

Worked Problem: An object with moment of inertia I rolls down a height h without slipping. Find the speed at bottom.



Answer: $v = \sqrt{\dfrac{2gh}{1+I/mR^2}}$

Newton's second law for rotation

$$\boxed{\sum \tau_p = I\alpha}$$

still also have $\sum \vec{F} = m\vec{a}$

… but acceleration of what?

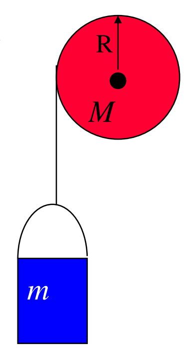
From warmup. Angular acceleration will definitely increase if:

a. torque is decreased and momentum of inertia is decreased
b. torque is decreased and momentum of inertia is increased
c. torque is increased and momentum of inertia is decreased
d. torque is increased and momentum of inertia is increased

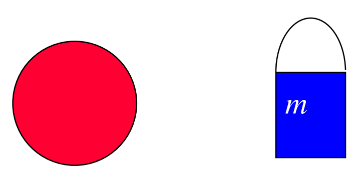
From warmup. Ralph heard his instructor say **"Moment of inertia plays the same role in rotational motion that mass does in linear motion."** This confuses him. What does it mean?

Answer from the class:

Worked problem: A falling mass starts a cylinder rotating (<u>not</u> a "massless pulley"). What is the acceleration of m?



Start with FBDs:



Write equations…

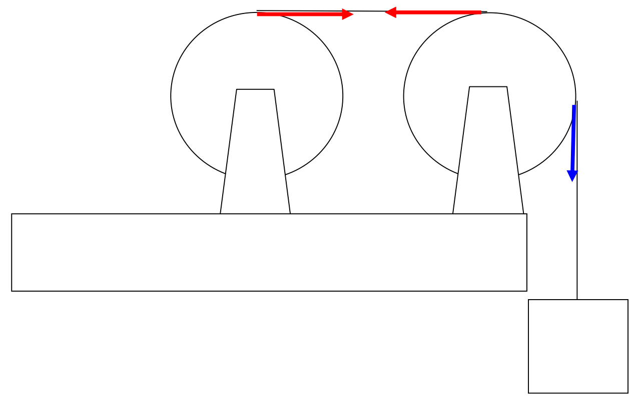
Cylinder

Pail

Make a connection between α and *a*:

Alternate method:

Answer: $a = \frac{m}{m + M/2} g$



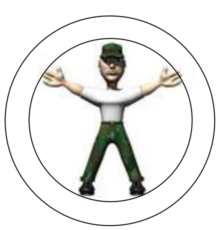
Clicker quiz: The left disk has a rope wrapped around its edge and the rope passes over a second disk. The two disks are identical and their **mass is significant**. As the system accelerates there is no slipping of the rope on either wheel; both wheels accelerate at the same rate. The tension in the rope is

a. Largest between the disks
b. Largest above the mass
c. The same in both places.

What's the difference with our old "massless pulleys"?

Clicker quiz: Mary and Fred are rolling a large tire down a hill. Mary says it will go faster if Fred gets inside the tire as shown and rolls down with it. Fred's not sure. What do you think?

a. It will go faster
b. It will go slower
c. It will take the same time



Let's do the experiment!