

Announcements – 30 Oct 2014

1. Prayer

2. **Exam 2** starts today!
 - a. Late fee on Monday Nov 3, after 2 pm
 - b. Closes on Tuesday Nov 4, 2 pm
 - c. Jerika exam reviews, both in room C295 ESC:
 - i. Wed Oct 29 7 - 8:30 pm (already happened)
 - ii. Thurs Oct 30 5:30 - 7 pm
 - d. Exam covers through angular momentum
 - i. Ch. 5, 6, 7.1-7.3, 8
 - ii. HW 10-17

“Which of the problems from last night's HW assignment would you most like me to discuss in class today?”

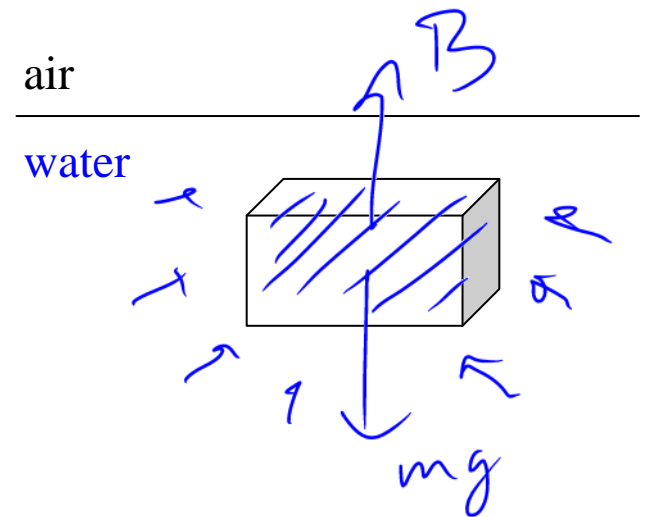
Buoyancy

Water in a thin rectangular plastic bag...

Does the water inside the bag have mass?

Does the water inside the bag have weight?

Why doesn't it accelerate down?



$$\sum F = 0$$

$$B - mg = 0$$

$$B = mg$$

$$B = W_{\text{displaced fluid}}$$

$$P = F/A$$

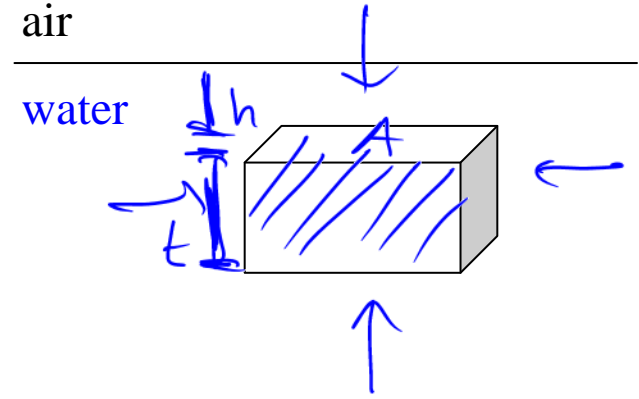
$$F = P \cdot A$$

Buoyancy, view 2

$$P = P_0 + \rho g h$$

$$\rho = m/V$$

Water in a thin rectangular plastic bag...



How much force is pushing downward on top? $(P_0 + \rho g h) A$

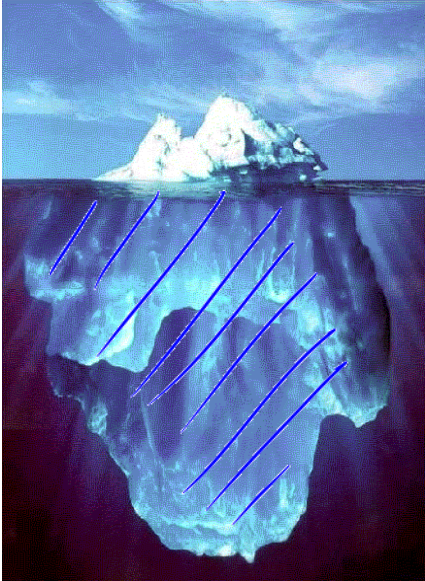
How much force is pushing upward on bottom? $(P_0 + \rho g (h+t)) A$

What's the net force? $(P_0 + \rho g (h+t)) A - (P_0 + \rho g h) A$

$$\begin{aligned} & \cancel{P_0 A} + \cancel{\rho g h A} + \underline{\underline{\rho g t A}} - (\cancel{P_0 A} + \cancel{\rho g h A}) \\ & = \boxed{\rho g V} = m_{\text{fluid}} g \end{aligned}$$

Archimedes' Principle

The buoyant force equals the weight of the fluid that the object is displacing at the moment.



$$\begin{aligned} F_{\text{Buoyant}} = B &= m_{\text{displaced fluid}} \times g \\ &= \rho_{\text{fluid}} \underbrace{V_{\text{object}}}_{\text{just the submerged volume}} g \end{aligned}$$

just the
submerged
volume

From warmup

The buoyant force of a submerged object always equals:

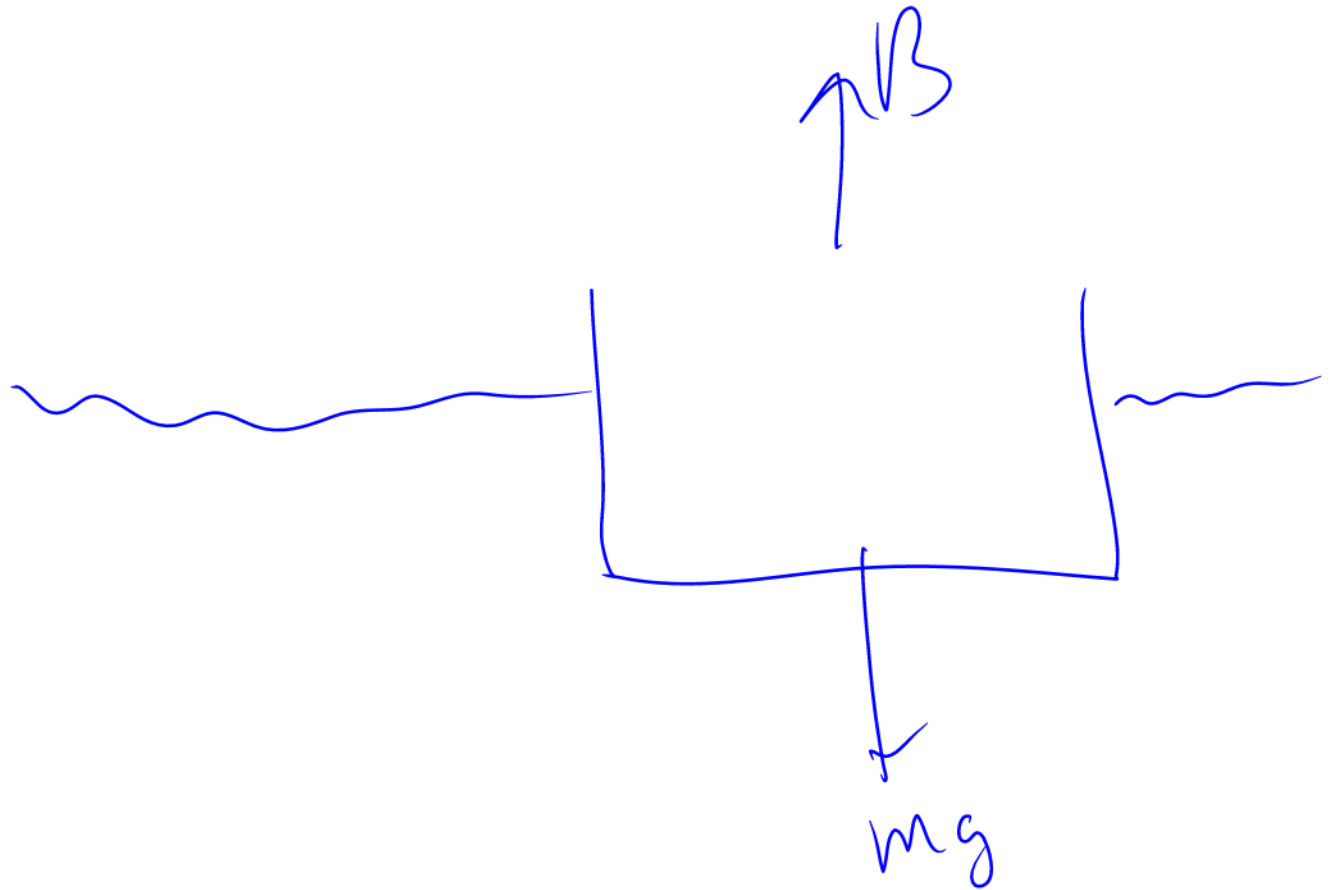
- a. the weight of the object
- b. the net force on the object
- c. the weight of the water that would otherwise occupy the object's space

Demos

- Does a can of soda sink or float?
- Does aluminum foil sink or float?

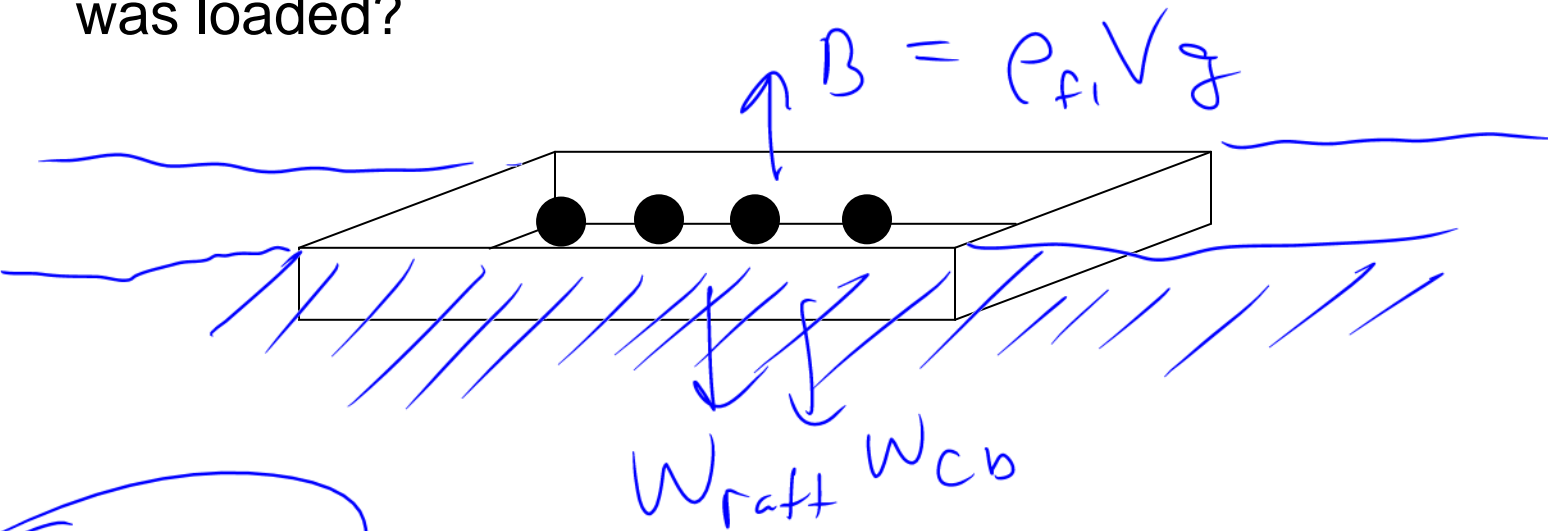
Floating objects

Floating objects will rise out of the water until...



Worked Problem

A raft of wood of size $0.5 \text{ m} \times 6 \text{ m} \times 5 \text{ m}$ weighs $30,000 \text{ N}$. It is loaded with cannon balls until it is (barely) completely submerged. How much weight was loaded?



$$\Sigma F = 0$$

$$B - W_{raft} - W_{cb} = 0$$

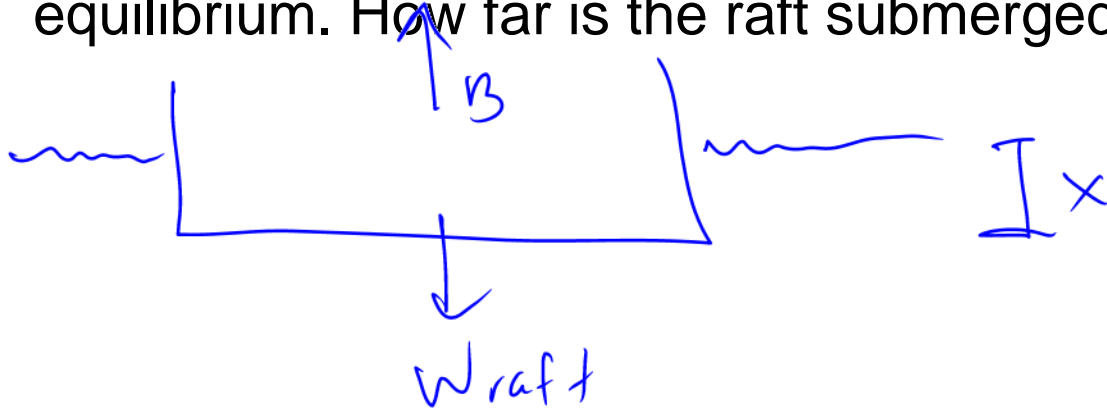
$$\rho_{fl} V g - W_{raft} = W_{cb}$$

$$(1000 \frac{\text{kg}}{\text{m}^3}) (0.5 \text{ m} \times 6 \text{ m} \times 5 \text{ m}) 9.8 \text{ m/s}^2 - 30000 \text{ N} = W_{cb}$$

Answer: $117,000 \text{ N}$

$$\boxed{117000 \text{ N} = W_{cb}}$$

Additional part: the balls are unloaded, and the raft now sits at equilibrium. How far is the raft submerged?



$$\sum F = 0$$

$$B = W_{\text{raft}}$$

$$\rho_{\text{fl}} V_{\text{obj}} g = W_{\text{raft}}$$

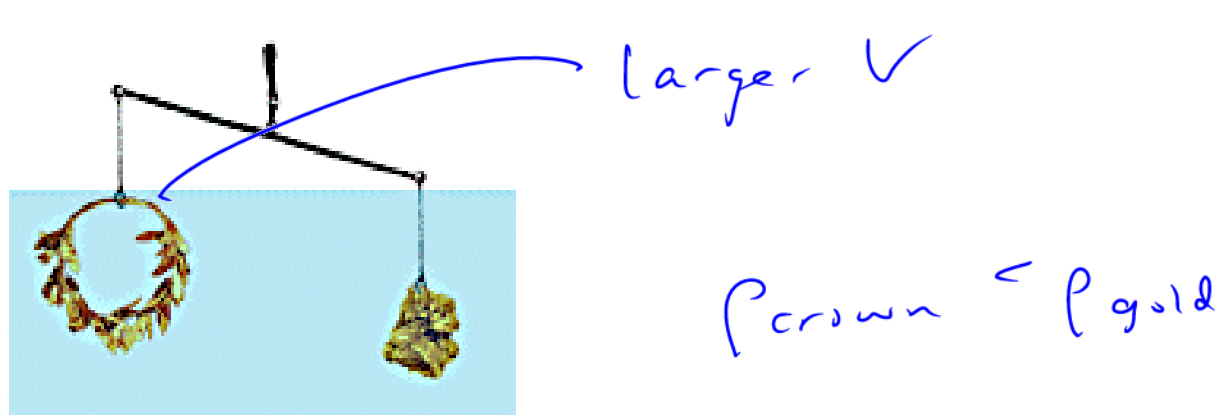
$$\left(1000 \frac{\text{kg}}{\text{m}^3}\right) (x \cdot 6 \text{ m} \cdot 5 \text{ m}) (9.8 \text{ m/s}^2) = 30000 \text{ N}$$

$$x = \frac{30000}{1000 \cdot 30 \cdot 9.8} = \boxed{0.102 \text{ m}}$$

Answer: 10.2 cm

Archimedes: "Eureka"

$$B = \rho_{\text{fluid}} V_{\text{obj}} g$$



Archimedes was charged with determining if a crown was pure gold. One method he may have used: he balanced the crown with pure gold outside water. After immersing, the balance tipped as shown.

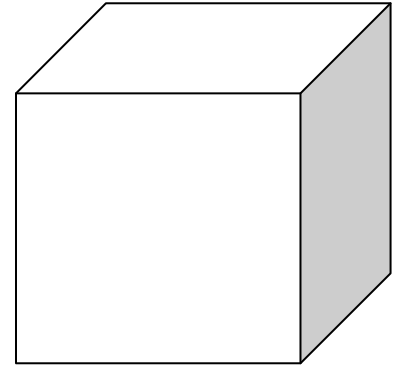
Clicker quiz: The crown has density

- a. more than gold
- b. less than gold
- c. same as than gold

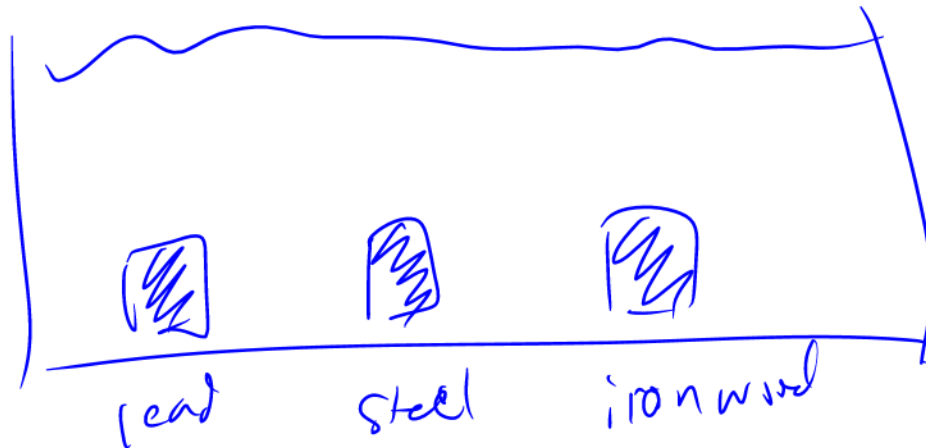
$$B = \rho_f V_{\text{obj}} g$$

Clicker quiz

Three cubes of the same size and shape are put in water. They sink. One is lead, one is steel and one is a dense wood (ironwood). $\rho_{\text{lead}} > \rho_{\text{steel}} > \rho_{\text{ironwood}}$. The buoyant force is greatest on the _____ cube



- a. lead
- b. steel
- c. wood
- d. same buoyant force

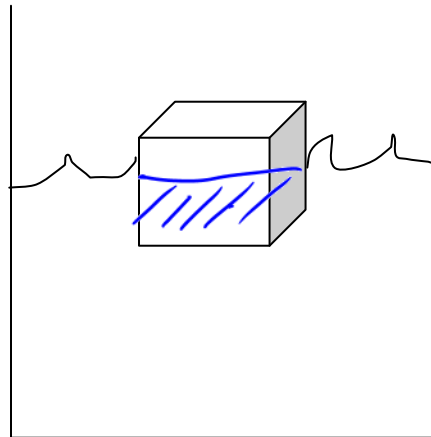
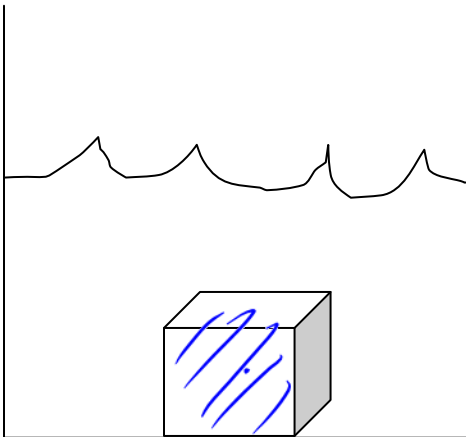


$$B = \rho_{\text{fl}} V_{\text{obj}} g$$

Clicker quiz

Two cubes of the same size and shape are made out of wood. The ironwood cube **sinks**, but the walnut cube **floats**. The bouyant force is greatest on the _____ cube

- a. ironwood
- b. walnut
- c. same bouyant force



Moving fluids

Disclaimer: **viscosity exists** → *Viscosity is friction in fluids*

Friction causes a loss in pressure along the tube as fluid flows.

Friction effects depend on radius:

bigger effects if radius is smaller

Friction effects depend on length:

bigger effects if length is longer

The power of viscosity (watch on your own):

http://www.youtube.com/watch?v=W3YZ5veN_Bg

That being said, we'll now ignore all viscosity effects...

...assume "frictionless fluids" unless otherwise stated

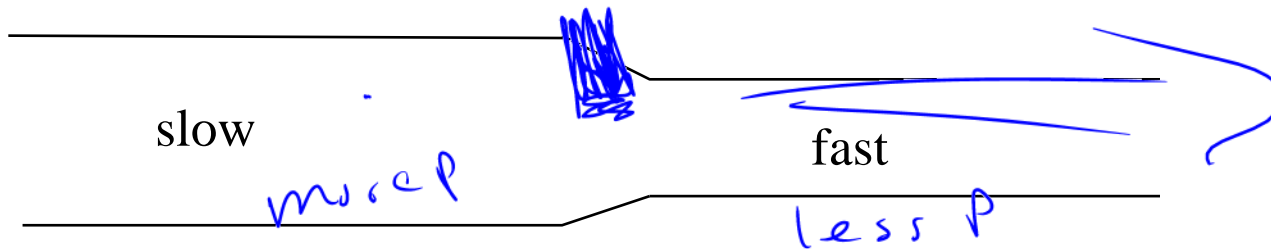
Bernoulli effect

The pressure in a fluid changes with the speed of the fluid.

Demo

Bernoulli effect in glass tube with varying diameter

→ why does the speed change?



Result of demo: Where is pressure the largest?

Disclaimer 1: This pressure change is **on top** of pressure lost from viscosity effects.

Disclaimer 2: What this *doesn't* mean (i.e. must compare speed in same overall flow)

Detour: fluid speeds

Volume flow rate: m^3/sec past any point

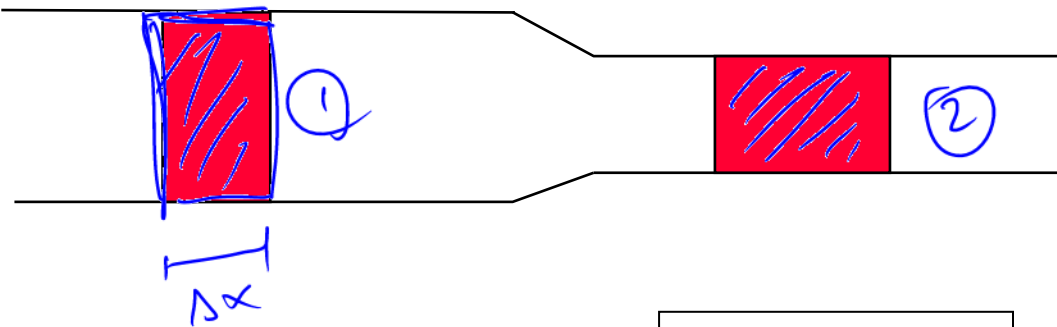
$$\underline{VFR} = \frac{\Delta \text{Volume}}{\Delta t} = \frac{\text{Area} \Delta x}{\Delta t} = A \cdot v$$

Assume:

- No viscosity (friction)
- • Incompressible (constant density) – *not true for gases*
- No turbulence

Then...

Conservation of Mass → Conservation of Volume Flow



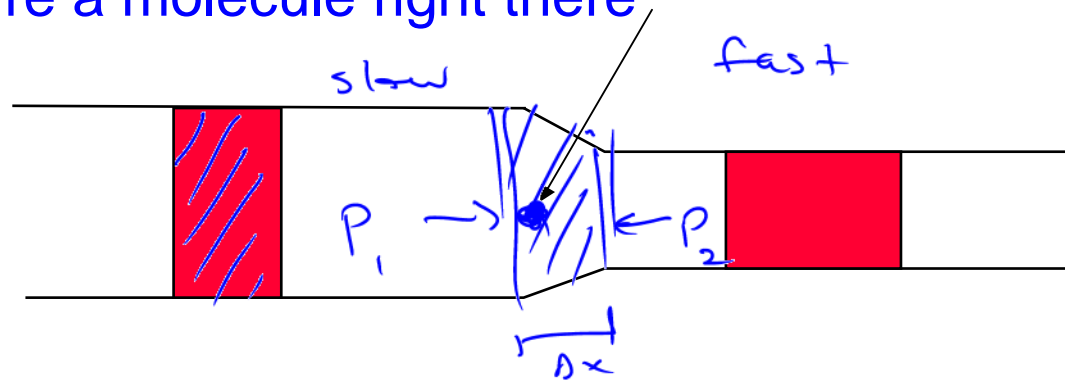
“Garden Hose Equation”:

$$A_1 v_1 = A_2 v_2$$

Book: “Equation of Continuity”

Why does the pressure depend on speed?

View #1: If you're a molecule right there



in what direction is the net force?

$$P_1 > P_2$$

$$F_{net} = \underline{P_1 A} - \underline{P_2 A}$$

$$W = F \cdot d$$



View #2: Energy & work, per volume

$$E_{\text{bef}} + W = E_{\text{aft}}$$

$$\frac{1}{2} m v_1^2 + m g h_1 + \underbrace{(P_1 A)^{\Delta x} - (P_2 A)^{\Delta x}}_{+ P_2 A \Delta x} = \frac{1}{2} m v_2^2 + m g h_2$$

divide by V

$$\frac{1}{2} \rho v_1^2 + \rho g h_1 + \overset{\text{pressure}}{P_1} = \frac{1}{2} \rho v_2^2 + \rho g h_2 + P_2$$

ρ
density

if same height

$$P_1 + \frac{1}{2} \rho v_1^2 = P_2 + \frac{1}{2} \rho v_2^2$$

\downarrow lower
 \uparrow if faster

“Bernoulli’s equation”

$$P_1 + \frac{1}{2} \rho v_1^2 + \rho g h_1 = P_2 + \frac{1}{2} \rho v_2^2 + \rho g h_2$$

Another blueprint!

From warmup: In the reading assignment for today, Ralph noticed two different equations labeled "Bernoulli's Equation". One said,

$$\underline{P_1 + \frac{1}{2} \rho v_1^2 + \rho g h_1} = \underline{P_2 + \frac{1}{2} \rho v_2^2 + \rho g h_2};$$

the other said, $\underline{P + \frac{1}{2} \rho v^2 + \rho g h} = C$.

He wants to know how they can both be the same equation when they look so different. And what does C stand for, anyway? What can you tell him?

“Think-pair-share”

- Think about it for a bit
- Talk to your neighbor, find out if he/she thinks the same as you
- Be prepared to share your answer with the class if called on

Clicker: I am now ready to share my answer if randomly selected.

a. Yes

Note: you are allowed to "pass" if you would really not answer.

Review

From warmup: Water flows from a pipe with large diameter into a pipe with smaller diameter. The speed of the water in the small tube is _____ the speed in the large tube.

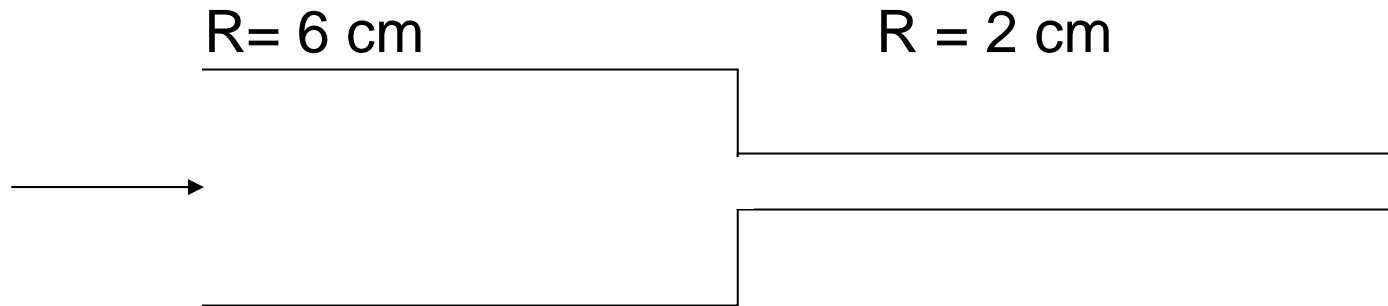
- a. greater than
- b. less than
- c. equal to

From warmup: Same situation. The pressure in the small tube is _____ the pressure in the large tube.

- a. greater than
- b. less than
- c. equal to

Worked Problem

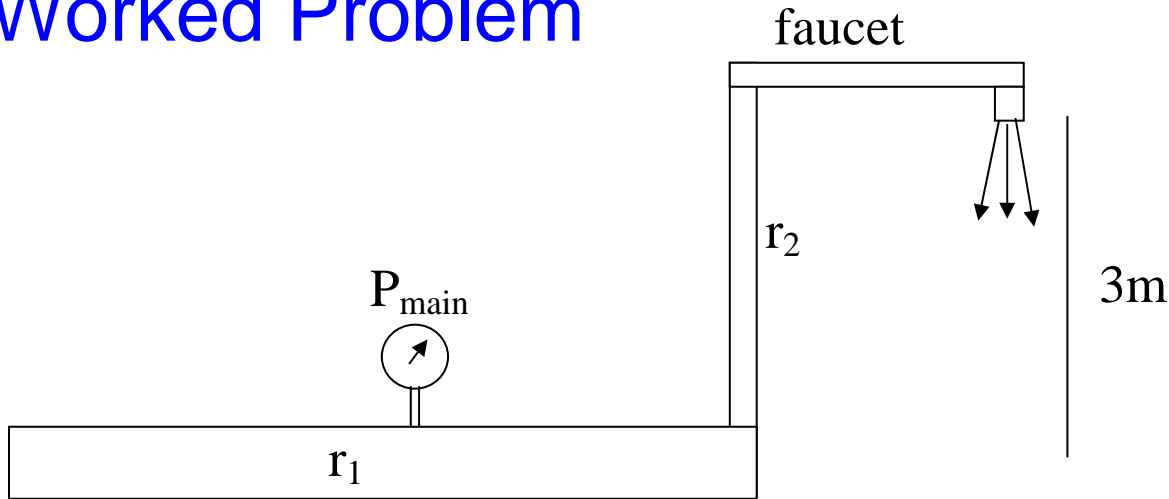
Water flows from the big pipe into the little pipe. Ignore any friction or height change.



If the speed on the left is 1 m/s , what's the speed on the right?

Answer: 0.111 m/s

Worked Problem



The faucet of radius $r_2 = 2$ cm puts water out at 15 liters/minute. The pressure at the opening of the faucet is about 1 atm. The water main ($r_1 = 6$ cm), is 3 meters below the faucet

- What is the speed of the water in the narrow pipe?
- What is the pressure in the water main?

Answers: 0.199 m/s, 1.304×10^5 Pa

The Bernoulli effect – what good is it?

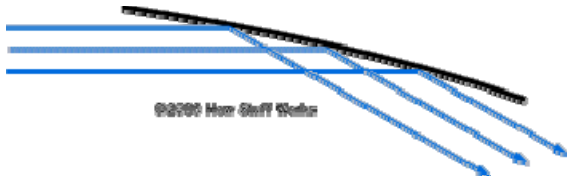
Demos: Blowing on paper, Ball over blower, Venturi blower, funnel, metal plate and wood cylinder

Video: Elder Nelson, April 1997 General Conference (1:58 - 3:45)

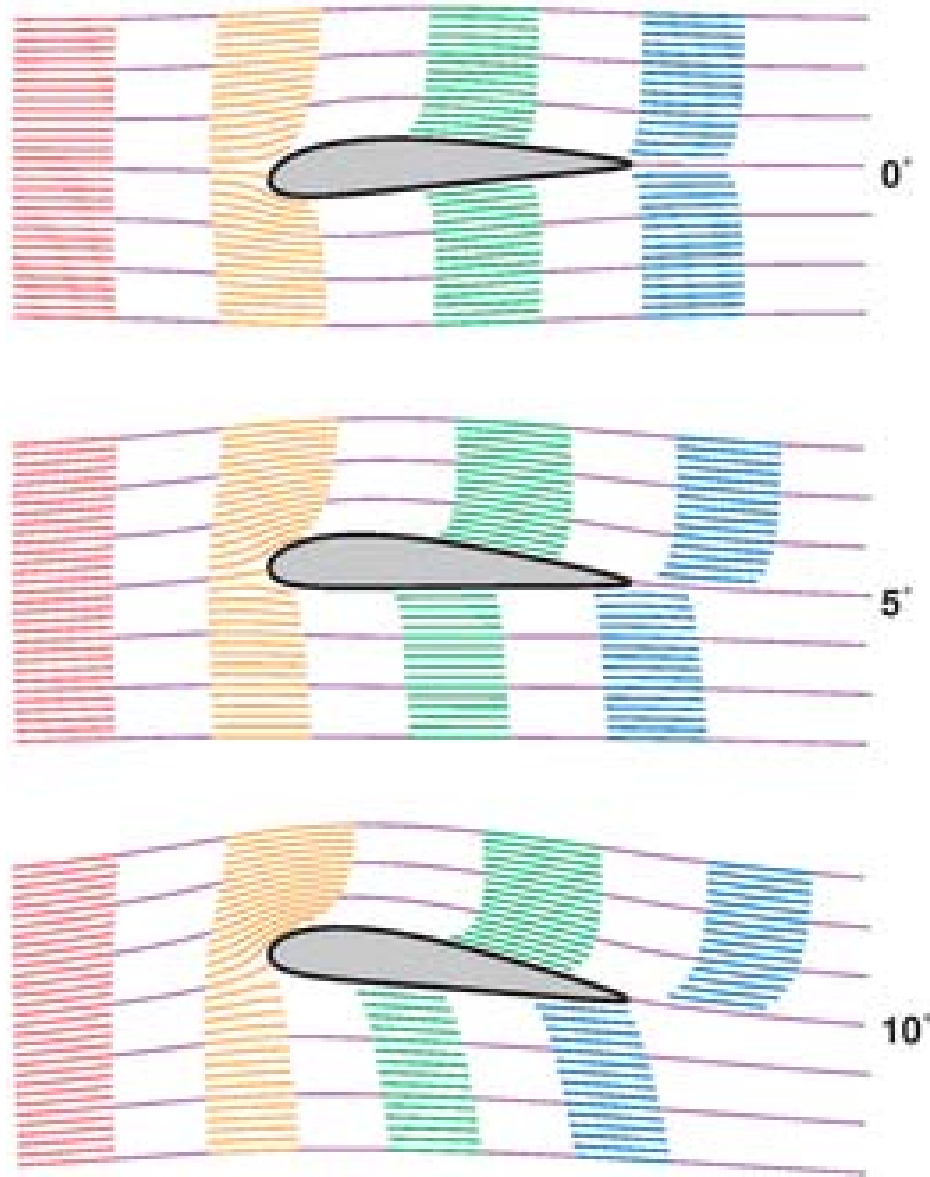
Airplane wings, and sails, and other “airfoils” (even racecars!)



Principle 1: air deflection, aka “put hand out the window” effect



Principle 2: Bernoulli



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