

Announcements – 11 Sep 2014

1. **A Cappella Auditions!** – Many of the groups in the BYU a cappella club are having a joint audition Tuesday at 7 pm, Varsity Theater. All parts needed, male and female. Prepare 60 seconds of music to sing. They will also do range checks and tonal memory checks.
→ Facebook page: www.facebook.com/acappellaclub

“Which of the problems from last night's HW assignment would you most like me to discuss in class today?”

Adding vectors by components – review

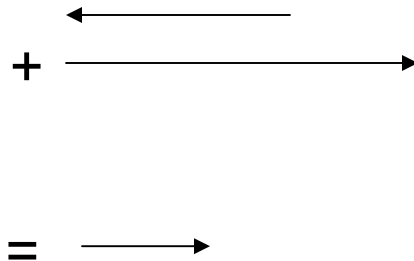
Web demo:

http://phet.colorado.edu/sims/vector-addition/vector-addition_en.html

Relative velocities

From warmup (last time): A man on a treadmill is walking at 1.5 m/s to the left. The treadmill is going at 2 m/s to the right. If you are standing still, it looks like the man is moving:

- a. 0.5 m/s left
- b. 3.5 m/s left
- c. stationary
- d. 0.5 m/s right
- e. 3.5 m/s right



Dr. Colton's "one size fits all" relative velocity equation

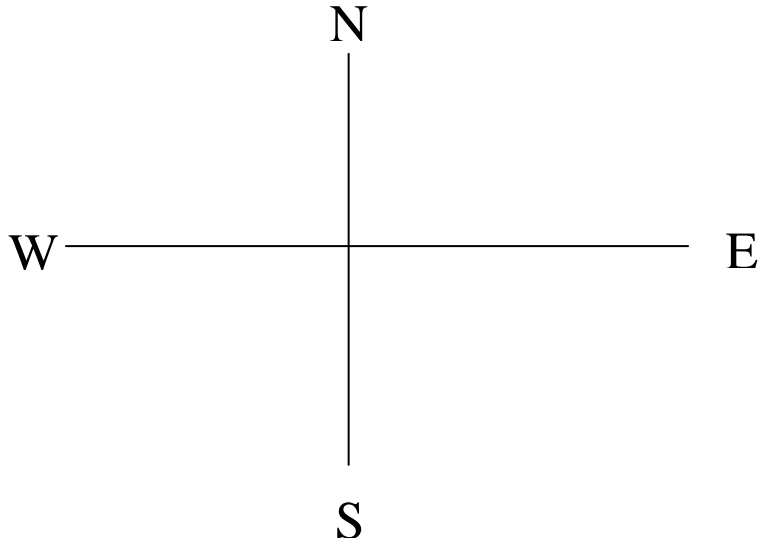
$$\vec{V}_{13} = \vec{V}_{12} + \vec{V}_{23}$$

- Read v_{13} as "velocity of object 1 relative to object 3"
- These are vectors!

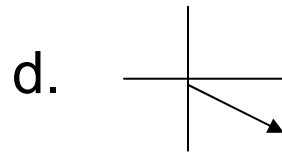
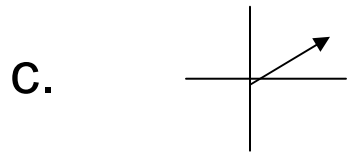
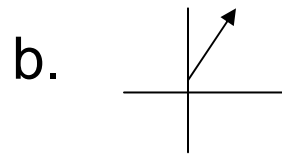
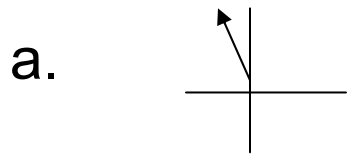
In this case

$$\vec{V}_{man-ground} = \vec{V}_{man-treadmill} + \vec{V}_{treadmill-ground}$$

A jet pointed N at 100 mph airspeed (v of plane w.r.t. air) flies in a 200 mph wind (air w.r.t. ground) going NE.



Clicker quiz: What is the jet's true bearing (velocity with respect to the ground)?



Question: How would you figure out the jet's total velocity (magnitude)?

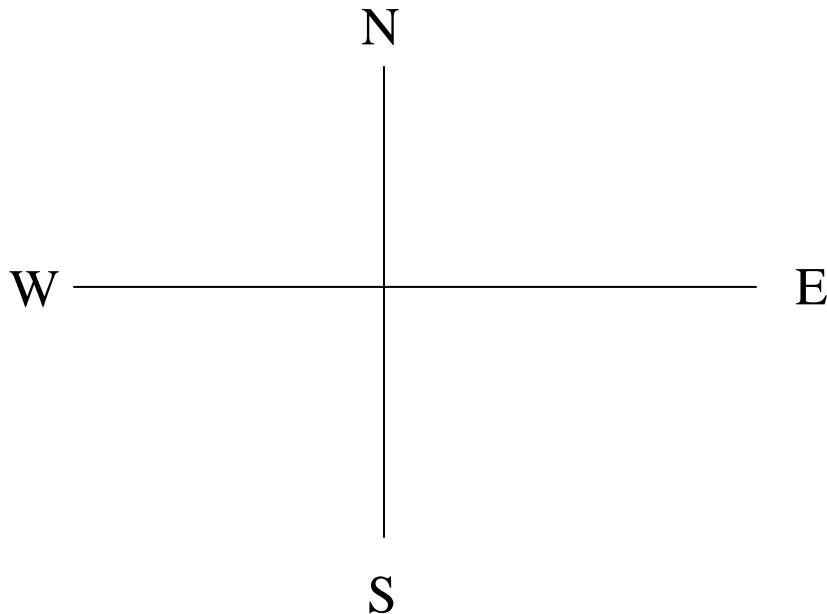
Clicker quiz

A captain wants her boat to sail exactly **E** on a map, with a speed relative to the *earth* of 10 mph. What direction should she point her boat if there is a 5 mph current to the **N**?

- a. a little bit north of east
- b. a little bit east of north
- c. a little bit south of east
- d. a little bit east of south

Hint: Start with an approximate picture

$$\mathbf{V}_{\text{boat-earth}} = \mathbf{V}_{\text{boat-water}} + \mathbf{V}_{\text{water-earth}}$$



Worked Problem

How fast will the boat have to go, and what's the exact heading?

Answer: 11.18 m/s, 26.6° south of east

Demo: Cart & ball

Clicker quiz: What will happen?

- A. Ball will land in front of cart
- B. Ball will land in back of cart
- C. Ball will land in cart

Demo: “Shooter & dropper” (2 balls: one shot & one dropped)

Clicker quiz: What will happen?

- A. Dropped ball will land first
- B. Shot ball will first
- C. Two balls will land at same time

2D Motion: Basic Concept

Motions in perpendicular directions are **independent**

From warmup

Which geometrical shape does a 2D projectile follow?

- a. line
- b. circle
- c. ellipse
- d. parabola
- e. hyperbola

Why is that?



<http://en.wikipedia.org/wiki/Parabola>



<http://www.aapt.org/Programs/contests/pc08.cfm>

Dr. Stokes' flash animation: baseball velocity components

http://stokes.byu.edu/teaching_resources/baseball_flash.html

Equations

x-direction

$$v_x = v_{0x} + a_x t$$

$$x = x_0 + v_{0x} t + \frac{1}{2} a_x t^2$$

$$v_{fx}^2 = v_{0x}^2 + 2a_x \Delta x$$

y-direction

$$v_y = v_{0y} + a_y t$$

$$y = y_0 + v_{0y} t + \frac{1}{2} a_y t^2$$

$$v_{fy}^2 = v_{0y}^2 + 2a_y \Delta y$$

2-D Projectile motion:

projectile: an
object in free fall

$$a_x = 0$$

$$a_y = -g$$

$$(-9.8 \text{ m/s}^2)$$

Warmup Questions

I throw a ball at an upward angle across a flat field. Neglecting air resistance, at what part of its path does the ball have its *minimum* speed?

- a. right before it hits the ground
- b. halfway to the top
- c. at the top of its path
- d. right after it leaves my hand
- e. There's not enough information to say

I throw a ball at an upward angle across a flat field. Neglecting air resistance, at what part of its path does the ball have its *maximum* speed?

- a. right before it hits the ground
- b. halfway to the top
- c. at the top of its path
- d. right after it leaves my hand
- e. There's not enough information to say

Clicker Quizzes

Sally and Bob each throw a rock horizontally from a cliff. Sally throws her rock hard. Bob throws his more easily.

Q1: Which spends the longest time falling?

- a. Sally's
- b. Bob's
- c. same

Q2: Which rock is going fastest (vector magnitude) just before it hits the ground?

- a. Sally's
- b. Bob's
- c. same

Question

Sally throws a rock horizontally from a cliff. Bob throws his at an angle above horizontal. They throw at the same speed. Whose hits first?

Demo: Monkey gun

Clicker quiz: What will happen?

- A. Bullet will pass over monkey
- B. Bullet will pass under monkey
- C. Bullet will hit monkey

Warmup question

A ball is thrown upwards at an angle. Ralph thought that since the ball is still moving upwards for a while after it is thrown, it must have some upwards acceleration in the air after it leaves my hand that continues to propel the ball. I told him "No, that's not quite what is happening." Can you help Ralph understand what *is* happening?

“Think-pair-share”

- Think about it for a bit
- Talk to your neighbor, find out if he/she thinks the same as you
- Be prepared to share your answer with the class if called on

Clicker: I am now ready to share my answer if randomly selected.

a. Yes

Note: you are allowed to "pass" if you would really not answer.

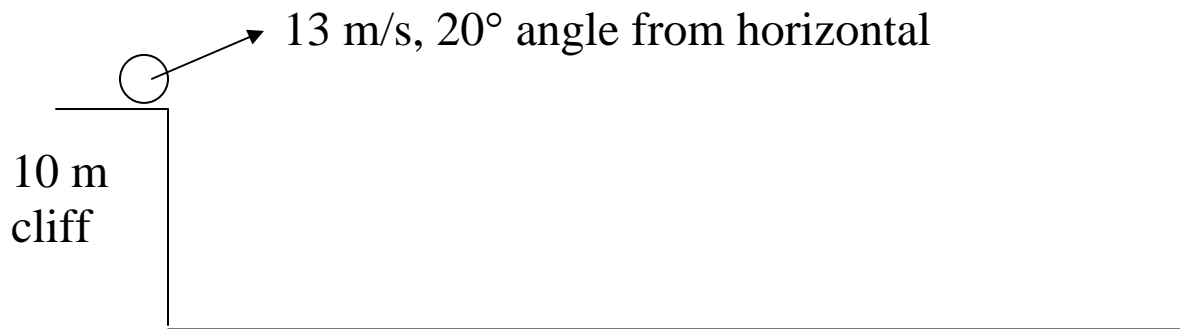
Range problems

Usually use the **y-equations** to figure out the **time** it takes

→ Then use the **x-equations** to figure out **how far** it has traveled in that time

Exception: Sometimes the nature of the problem means the x-equations determine the time it takes—for example, if the projectile runs into a wall

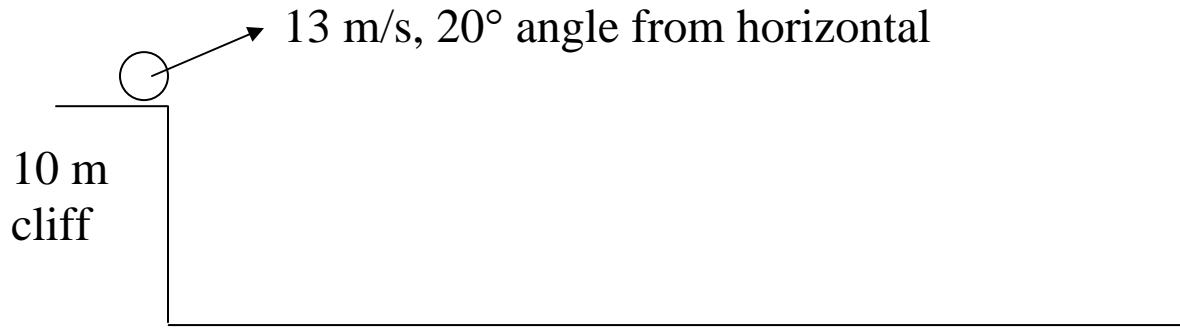
Worked Problem: Where does the ball hit? How fast is it going then?



Step 1: find the time

Answer: $t = 1.9526 \text{ s}$

Worked Problem, cont.: Where does the ball hit? How fast is it going then?



Step 2: use the time

Answers: $t = 1.9526$ s, $x = 23.85$ m, $v_{fx} = 12.22$ m/s, $v_{fy} = 14.69$ m/s, $v_{f,tot} = 19.10$ m/s

Worked Problem

A rifle at the same height as a very large target tries to hit the center, 400 m away. The rifle is shot at 8° above the horizontal. The initial velocity of the bullet is 200 m/s. How far above/below the center does the bullet hit?

Answers: $t = 2.02$ s, $y = 36.23$ m

Maximum range

Warmup question: Neglecting air resistance, at what angle should you throw a ball on a flat field in order to get the maximum range? (also neglecting height of person)

- a. 30°
- b. 45°
- c. 60°
- d. It depends on the initial speed

Caveats...