

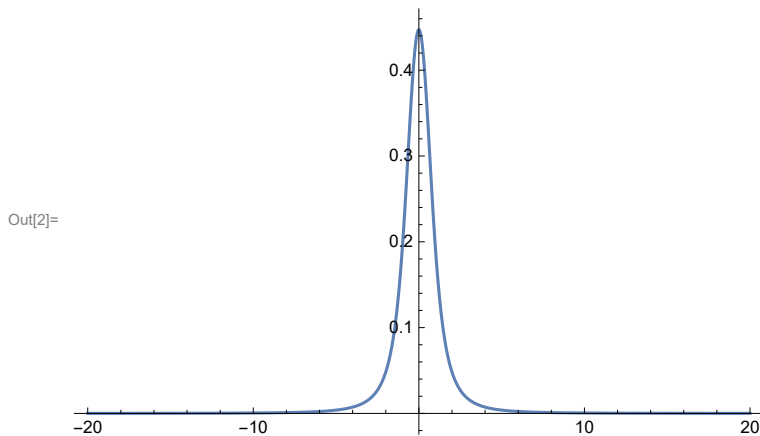
■ Field of a magnetized cylinder (or equivalently, a finite solenoid)

In[1]:= (* exact formula, setting $\mu_0 = 1$ and $R = 1$ *)

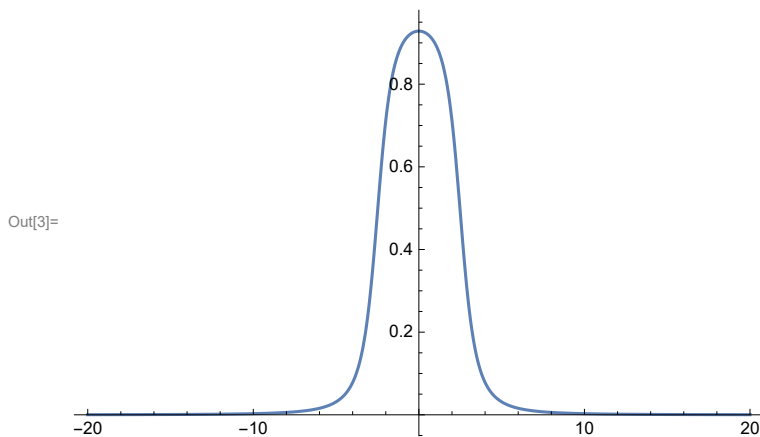
$$b[z_, L_] = 1/2 ((z + L/2) / \text{Sqrt}[1 + (z + L/2)^2] - (z - L/2) / \text{Sqrt}[1 + (z - L/2)^2])$$

$$\text{Out[1]} = \frac{1}{2} \left(-\frac{-\frac{L}{2} + z}{\sqrt{1 + \left(-\frac{L}{2} + z\right)^2}} + \frac{\frac{L}{2} + z}{\sqrt{1 + \left(\frac{L}{2} + z\right)^2}} \right)$$

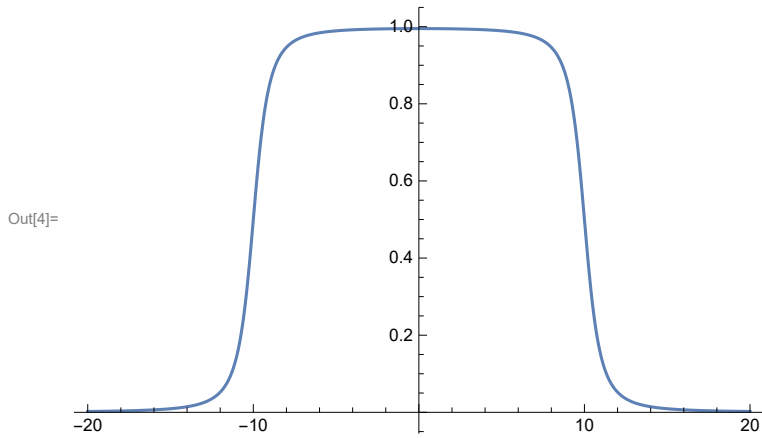
In[2]:= **Plot**[b[z, 1], {z, -20, 20}, PlotRange → All] (* length = 1 x radius *)



In[3]:= **Plot**[b[z, 5], {z, -20, 20}, PlotRange → All] (* length = 5 x radius *)



In[4]:= `Plot[b[z, 20], {z, -20, 20}, PlotRange -> All] (* length = 20 x radius *)`

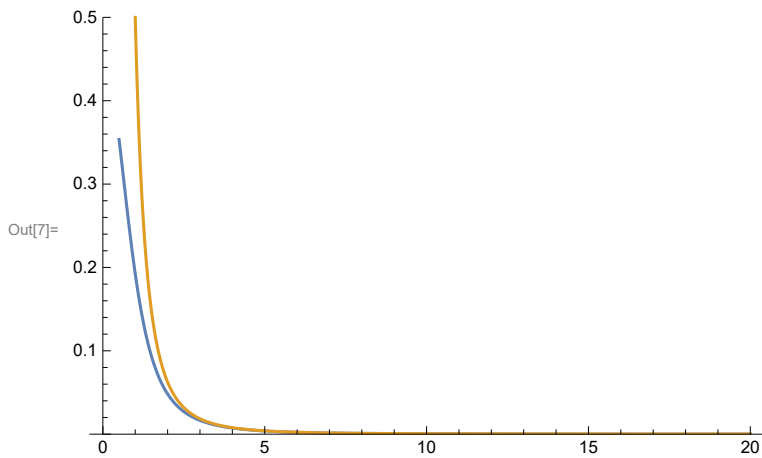


In[5]:= `(* approximate formula, setting mu0 = 1 and R = 1 *)`
`bapprox[z_, L_] = L / (2 z^3)`

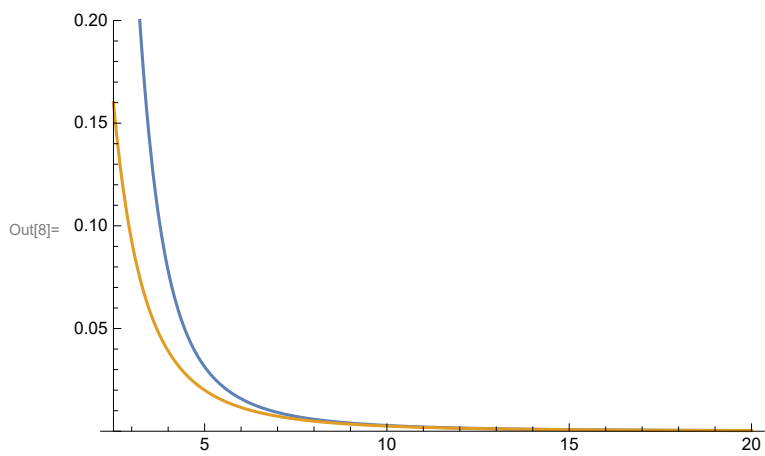
Out[5]=
$$\frac{L}{2 z^3}$$

In[6]:= `(* Some plots of field outside the cylinder, exact and also approximate dipole field *)`

In[7]:= `Plot[{b[z, 1], bapprox[z, 1]}, {z, 0.5, 20}, PlotRange -> {0, .5}]`
`(* length = 1 x radius *)`



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In[8]:= Plot[{b[z, 5], bapprox[z, 5]}, {z, 2.5, 20}, PlotRange -> {0, .2}]  
(* length = 5 x radius *)
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In[9]:= Plot[{b[z, 20], bapprox[z, 20]}, {z, 10, 50}, PlotRange -> {0, .012}]  
(* length = 20 x radius *)
```

