

The Four Complicated Integral Formulas

- “Huygens-Fresnel diffraction formula”

$$E(x, y, z) = -\frac{i}{\lambda} \iint_{\text{aperture}} E(x', y', 0) \frac{e^{ikR}}{R} dx' dy' \quad (10.1)$$

- “The Fresnel-Kirchhoff diffraction formula”

$$E(x, y, z) = -\frac{i}{\lambda} \iint_{\text{aperture}} E(x', y', z=0) \frac{e^{ikR}}{R} \left[\frac{1 + \cos(\mathbf{R}, \hat{\mathbf{z}})}{2} \right] dx' dy' \quad (10.10)$$

- “The Fresnel approximation”

$$E(x, y, z) \cong -\frac{ie^{ikz} e^{i\frac{k}{2z}(x^2+y^2)}}{\lambda z} \iint_{\text{aperture}} E(x', y', 0) e^{i\frac{k}{2z}(x'^2+y'^2)} e^{-i\frac{k}{z}(xx'+yy')} dx' dy' \quad (10.13)$$

- “The Fraunhofer approximation”

$$E(x, y, z) \cong -\frac{ie^{ikz} e^{i\frac{k}{2z}(x^2+y^2)}}{\lambda z} \iint_{\text{aperture}} E(x', y', 0) e^{-i\frac{k}{z}(xx'+yy')} dx' dy' \quad (10.19)$$