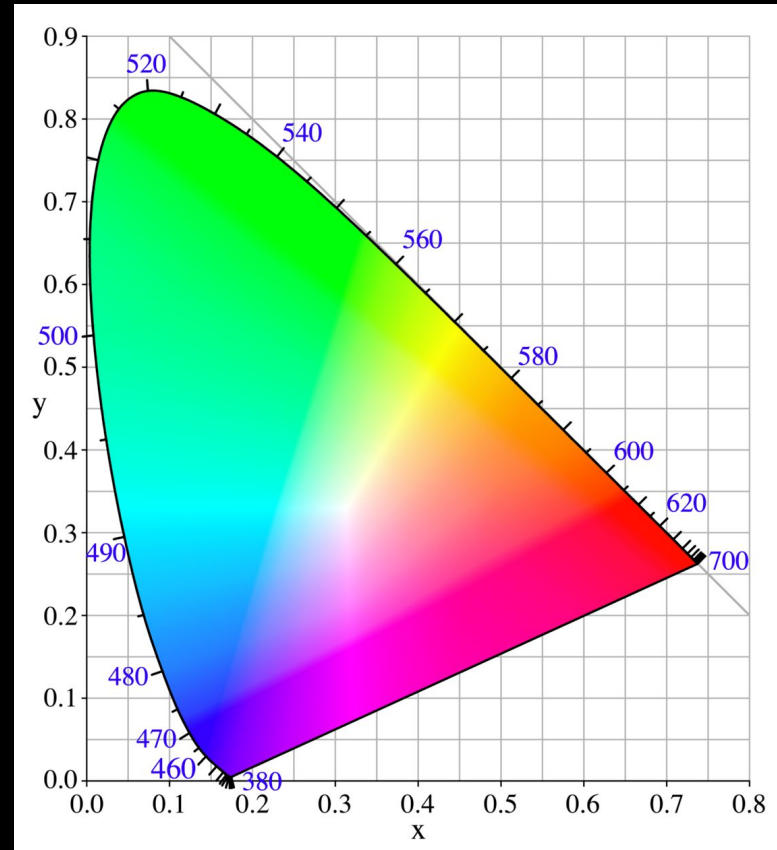


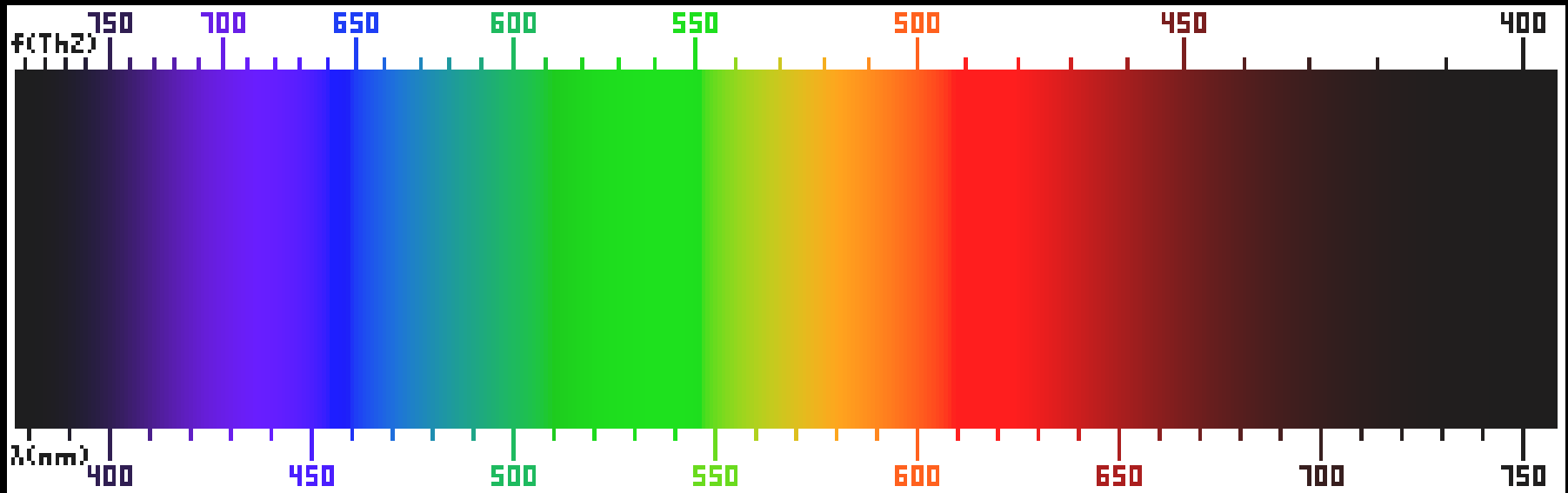
Color! Main Goals:

- Understand this thing:
“Chromaticity diagram”



- Given a spectrum, how to predict what color the spectrum will seem to you

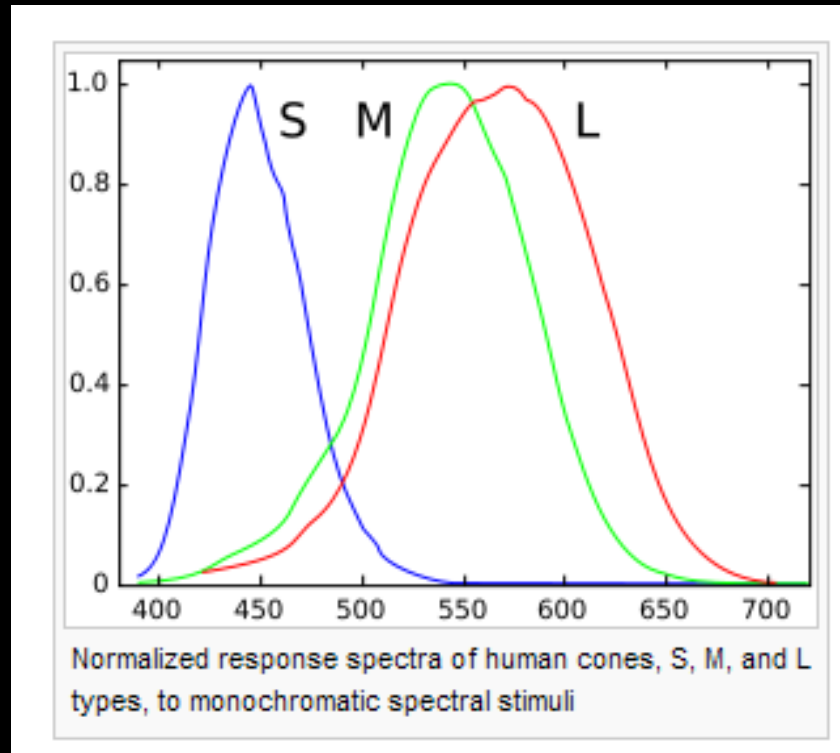
Visible Spectrum



From Wikipedia, “Visible Spectrum”

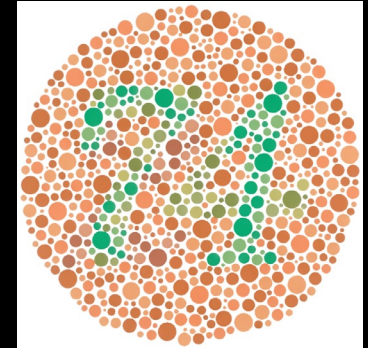
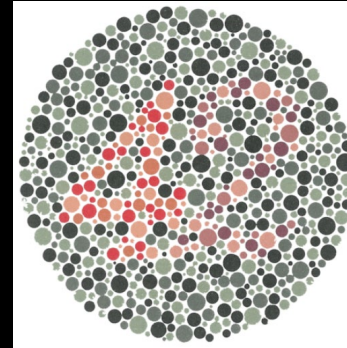
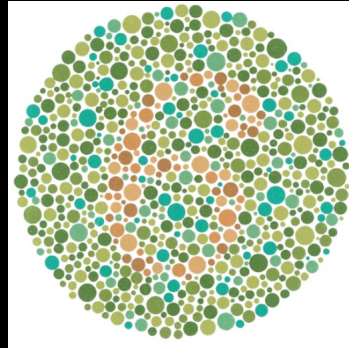
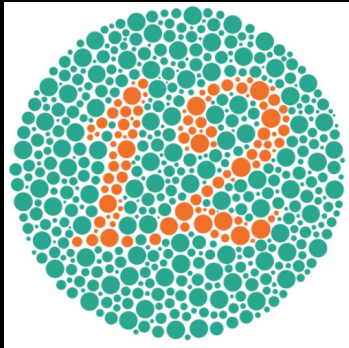
- “All the colors of the rainbow...”
→ Where is brown?? Where is pink?? Where is turquoise??

Cone cells



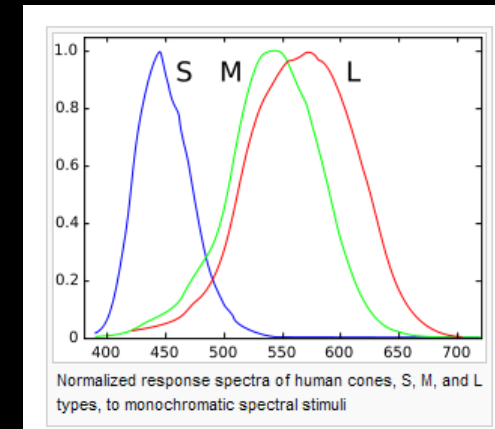
“Short” “Medium” “Long”

Color blindness

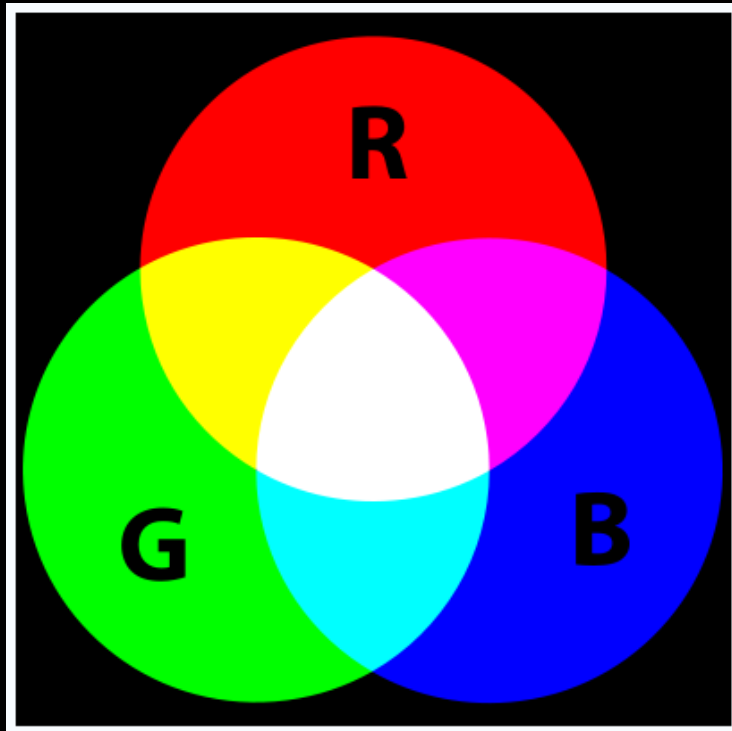


From Wikipedia, “Ishihara test”

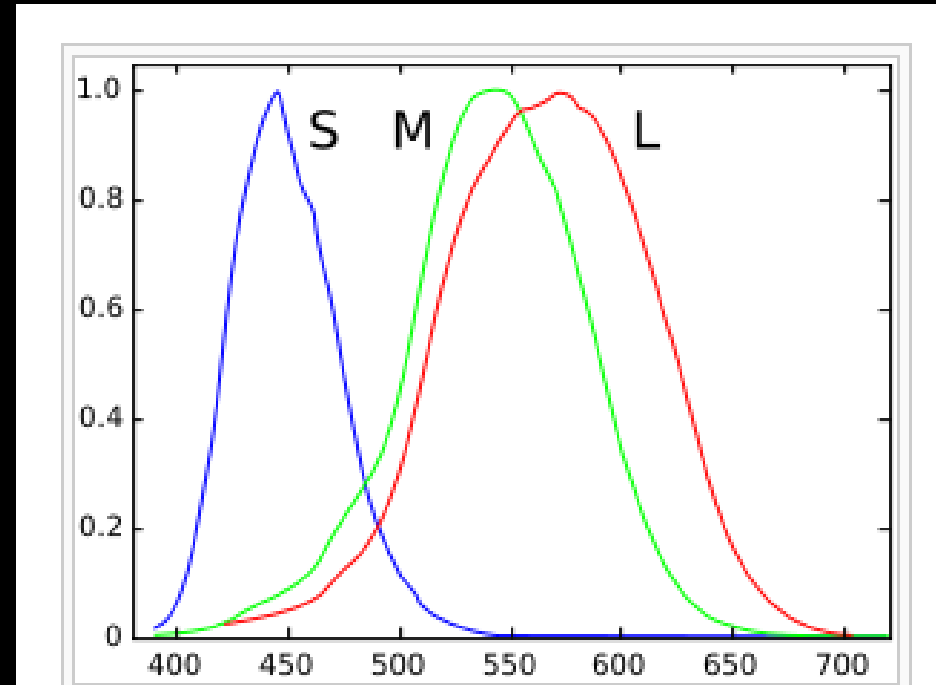
Name	Cause	Prevalence
tritanopia	lacks S cones	<1% of males and females
tritanomaly	S cones mutated	~0.01% of males and females
deutanopia	lacks M cones	~1% of males
deutanomaly, standard “red-green color blindness”	M cones mutated	~5% of European males; far fewer females
protanopia	lacks L cones	~1% of males
protanomaly	L cones mutated	~3% of European males; far fewer females
achromatopsia	total color blindness	0.003% of males and females (1 in 33,333)



Primary Colors



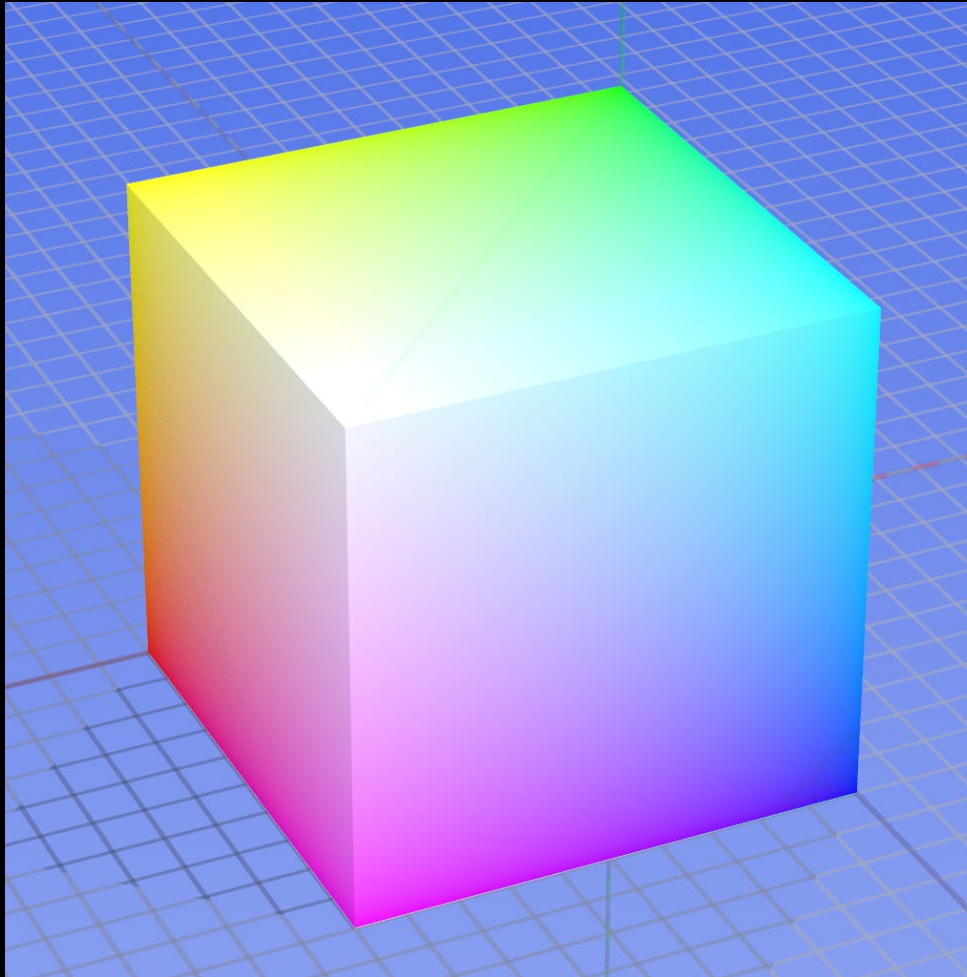
From Wikipedia,
“RGB Color Model”



Cone cell response

- How the primary song *should* go
- “Additive color mixing”
- (Pigments: “subtractive color mixing”)

Components of R, G, B: Plot in 3D “color space”

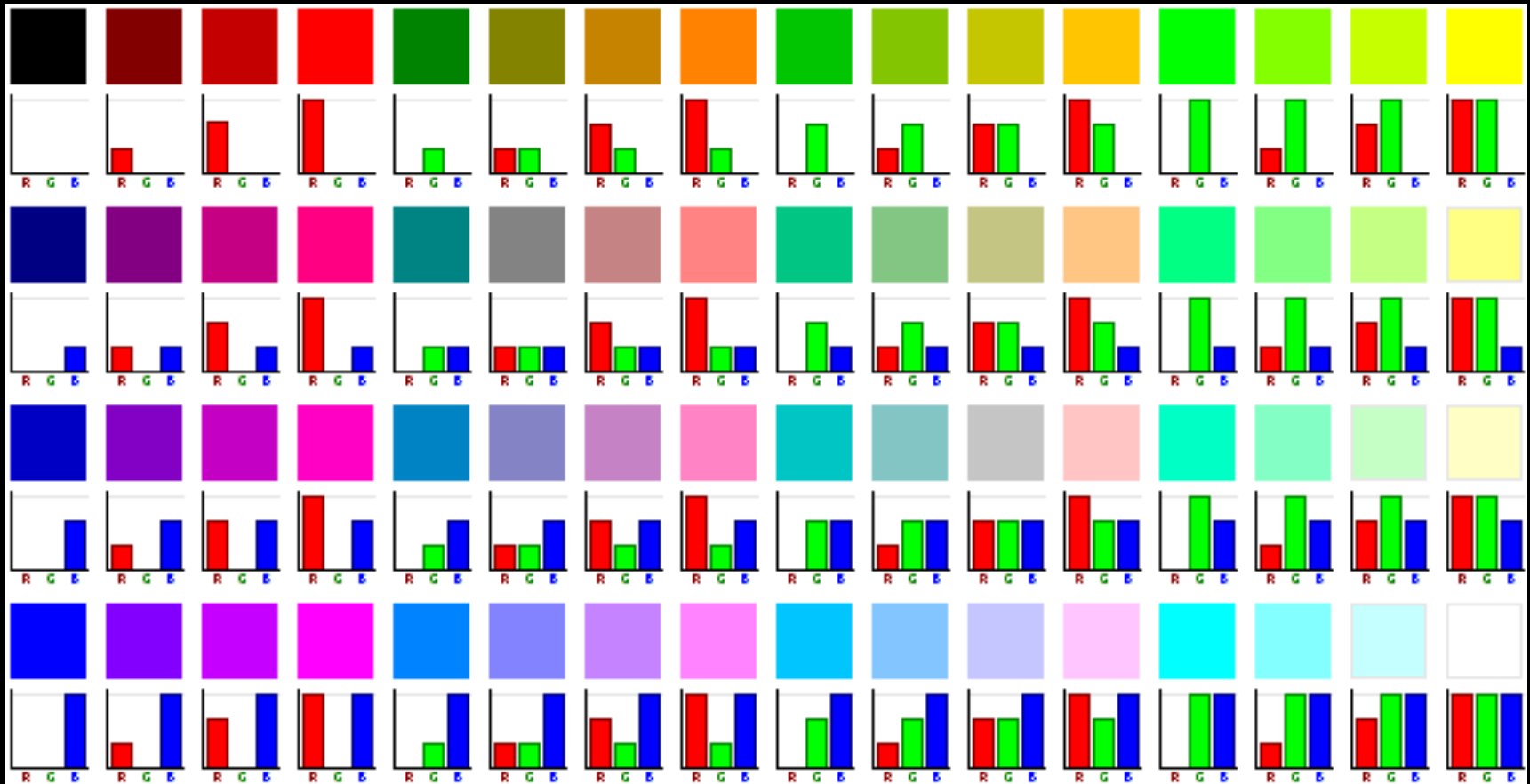


From Wikipedia,
“RGB Color Model”
(old version)

Viewing slices of the cube:

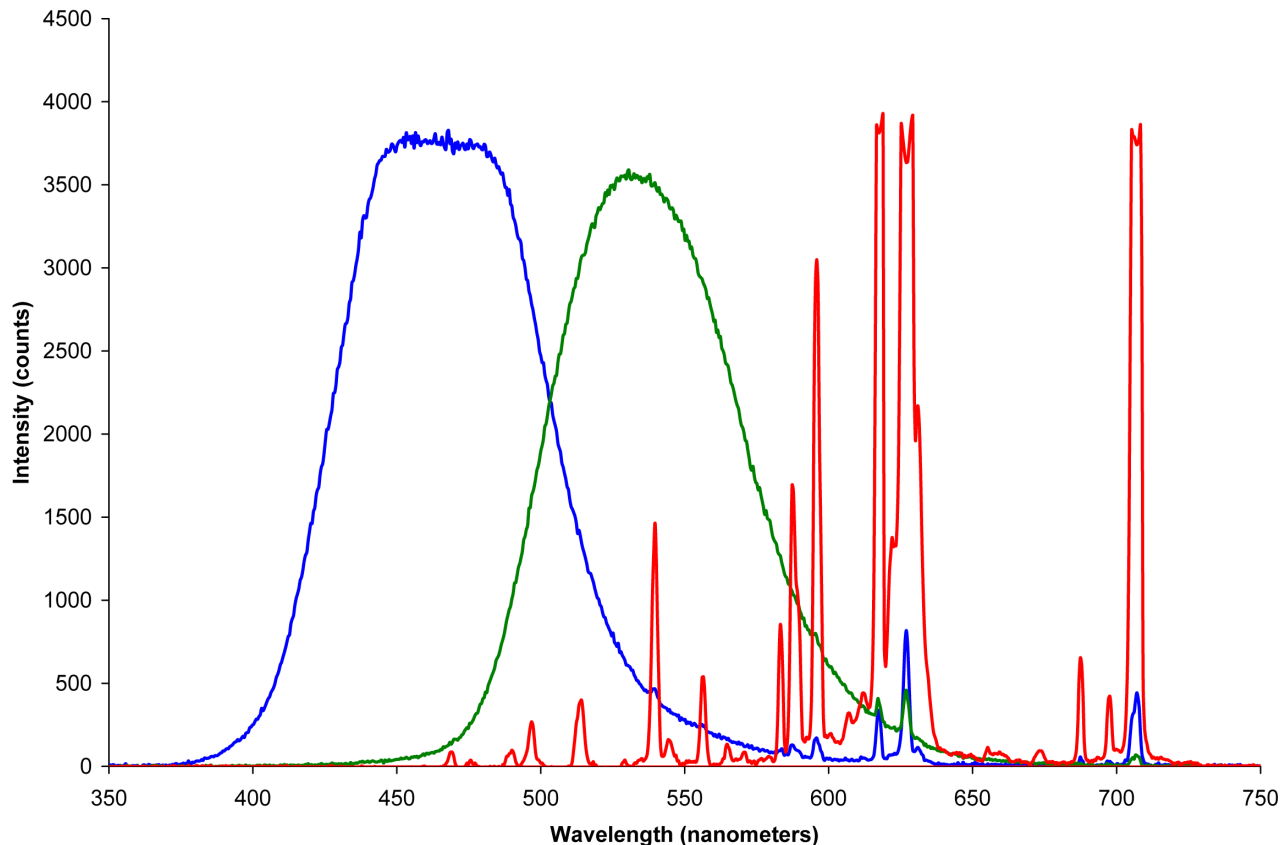
<https://programmingdesignsystems.com/color/color-models-and-color-spaces/index.html>

Components of R, G, B



From Wikipedia,
“RGB Color Model”
(old version)

How to Display Colors



The **emission spectra** of the three **phosphors** that define the **additive primary colors** of a **CRT** color video display. Other electronic color display technologies (**LCD**, **Plasma display**, **OLED**) have analogous sets of primaries with different emission spectra.

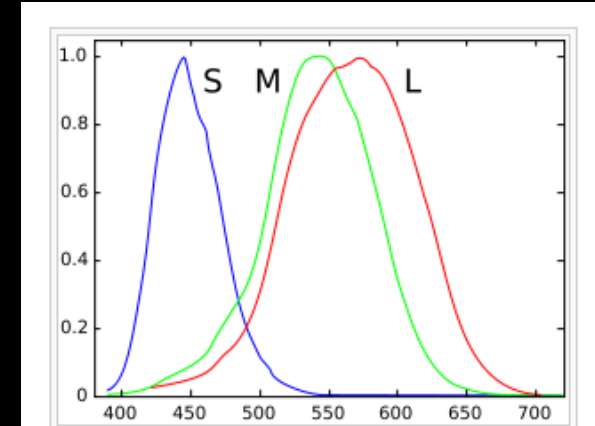
From Wikipedia, "Primary Color"

1920's Color Matching Experiments

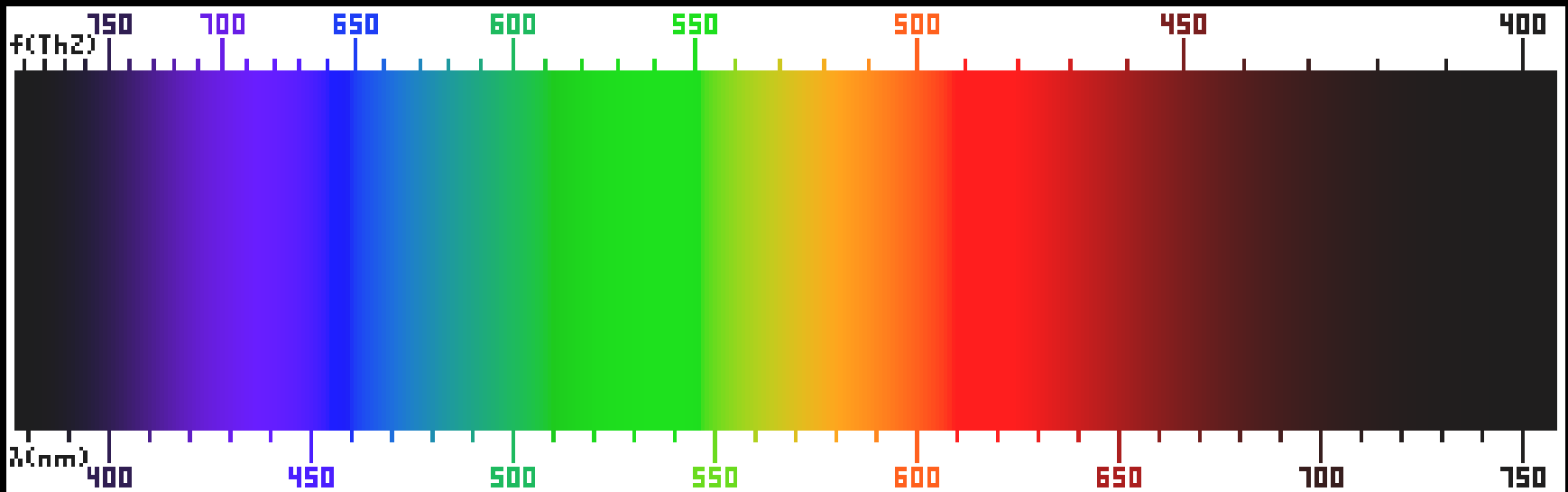
Using combinations of these three:

- Narrow red source at 700 nm
- Narrow green source at 546.1 nm
- Narrow blue source at 435.8 nm

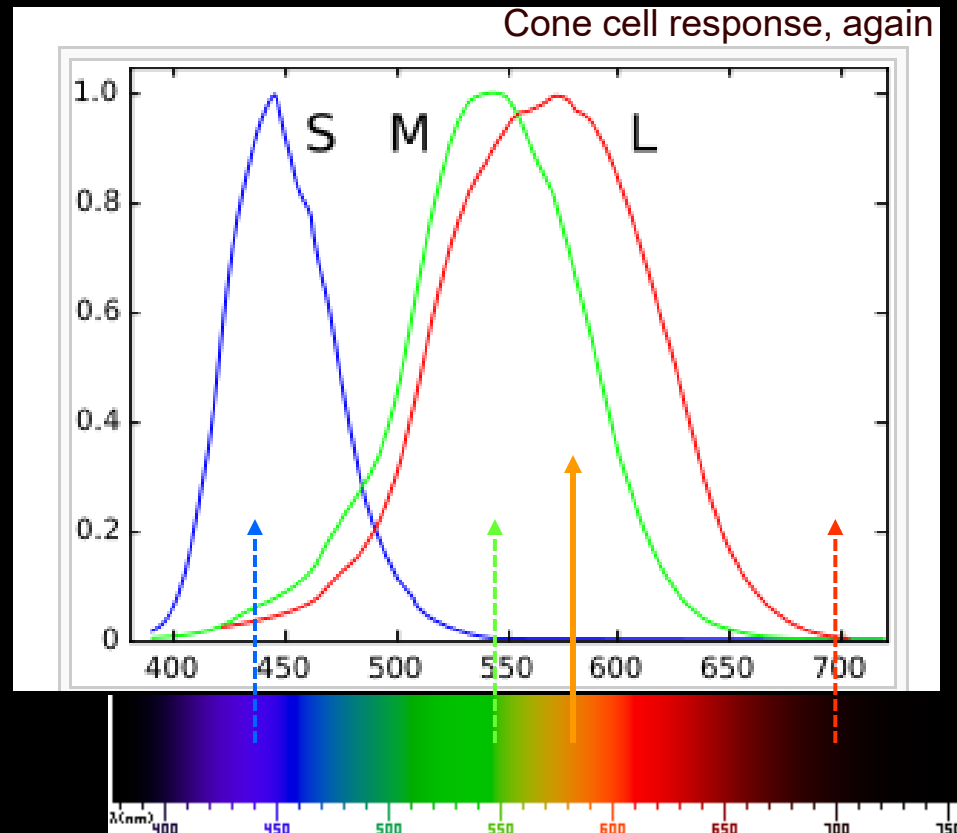
How much of each is required to match the wavelengths in the visible spectrum (“pure colors”)?



Cone cell response, again



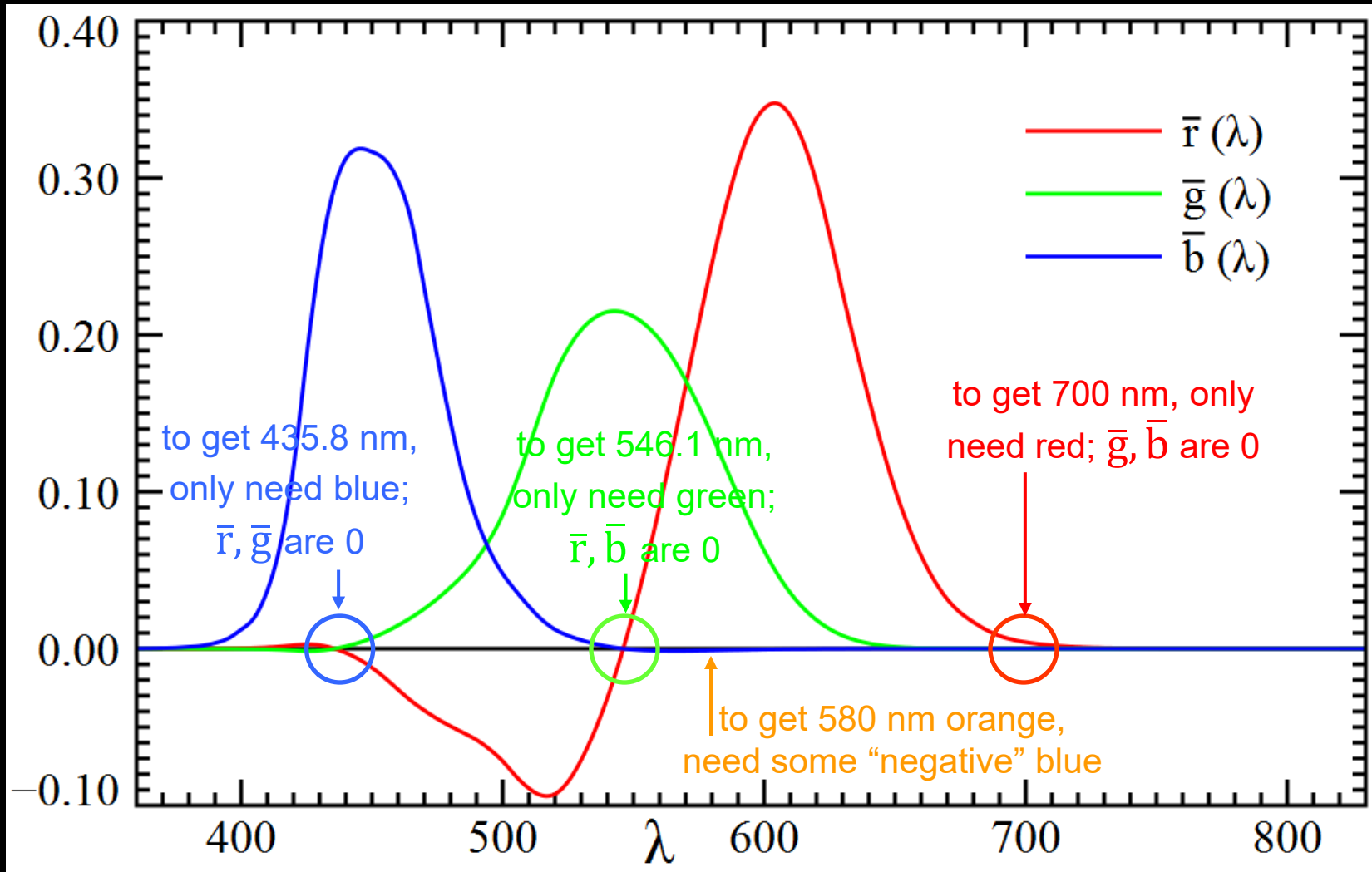
A Concern



- Say you want to mix the dashed lines to look the same as 580 nm orange line.
- You may start by turning up the red light. But soon you also need to turn up the green light. However...
 - Green light will excite some S! (a small amount, but nonzero)
 - 580 nm alone will never excite S! Therefore 580 nm cannot be matched.
 - You need some “negative blue” to counteract

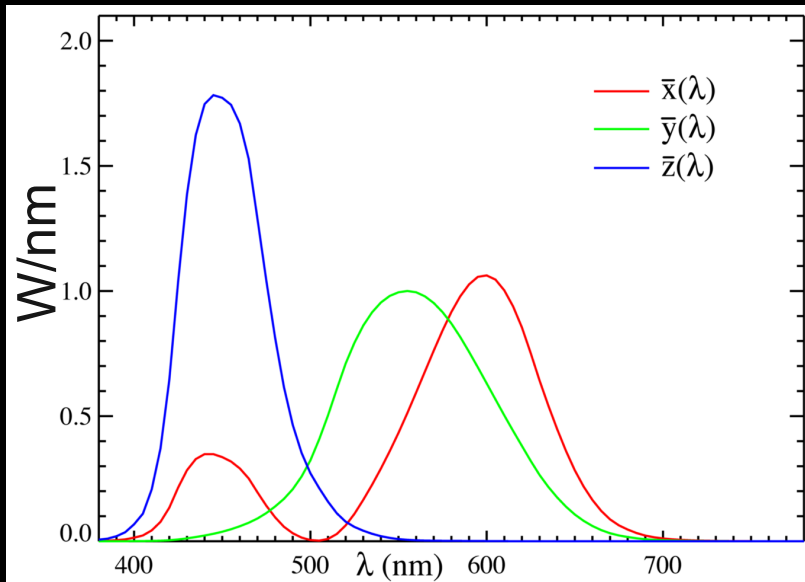
Results: \bar{r} , \bar{g} , \bar{b} functions

red source = 700 nm green source = 546.1 nm blue source at 435.8 nm



From Wikipedia, "1931 Color Space" (also in P&W)

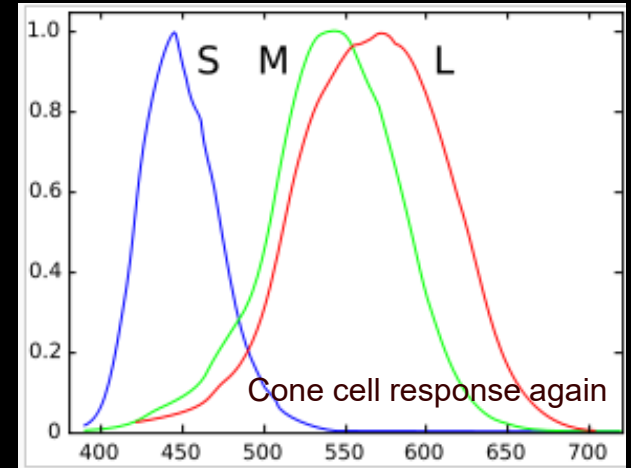
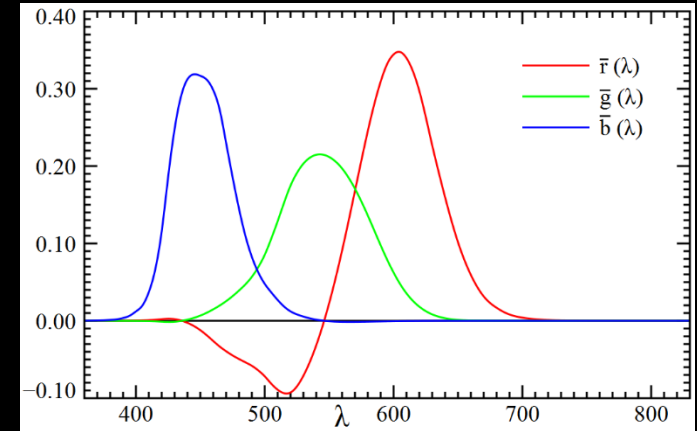
Better!! \bar{x} , \bar{y} , \bar{z} functions



From Wikipedia, "CIE 1931 Color Space"
(Very Important, but not in Peatross & Ware)

\bar{x} , \bar{y} , \bar{z} properties

- all are positive
- \bar{z} = close to S cones, close to \bar{b}
- \bar{y} = matches intensity response of eye, close to M cones. Normalized to 1.
- \bar{x} = chosen so that white is equal parts of all three



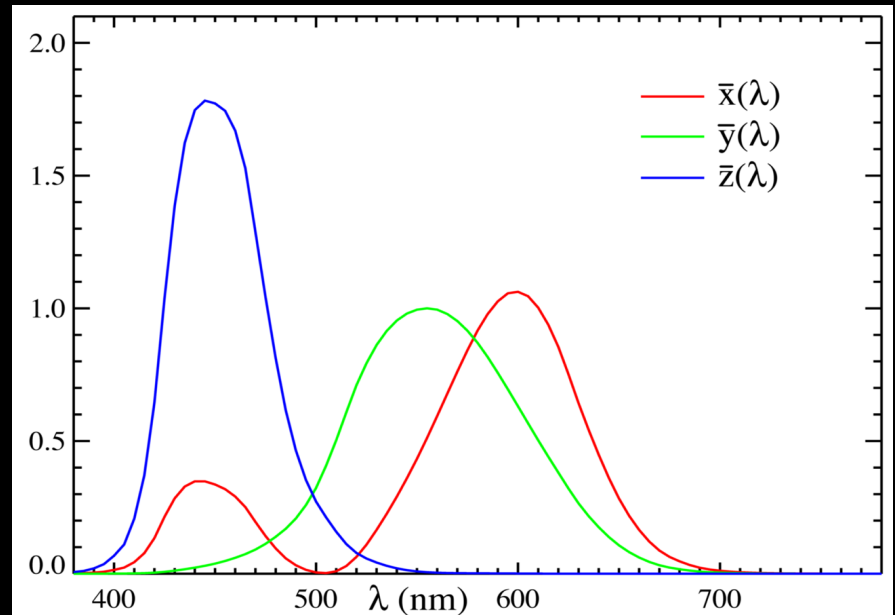
Projections

- Given a spectrum $I(\lambda)$, how much \bar{x} , \bar{y} , and \bar{z} does it have?

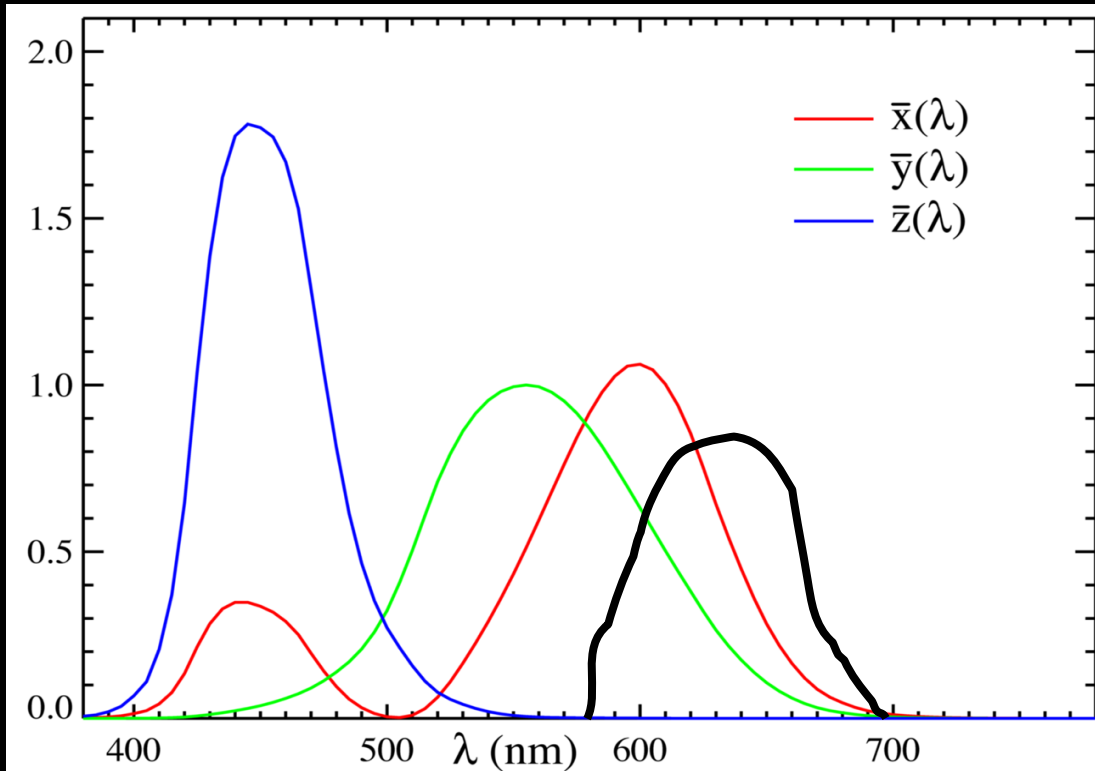
$$X = \int I(\lambda) \bar{x}(\lambda) d\lambda$$

$$Y = \int I(\lambda) \bar{y}(\lambda) d\lambda$$

$$Z = \int I(\lambda) \bar{z}(\lambda) d\lambda$$



Worked Example, Like P2.13



Note 1: the functions were changed in 2006. For HW problem, use functions given on <https://optics.byu.edu/resources> (link provided in textbook)

Note 2: as explained in my instructions for P2.13, "luminous power" (in lumens)
 $= 683 \times \int I(\lambda) \bar{y}(\lambda) d\lambda$
 $= 683 \times Y$

- $X = \sim 15$
- $Y = \sim 12$
- $Z = 0$

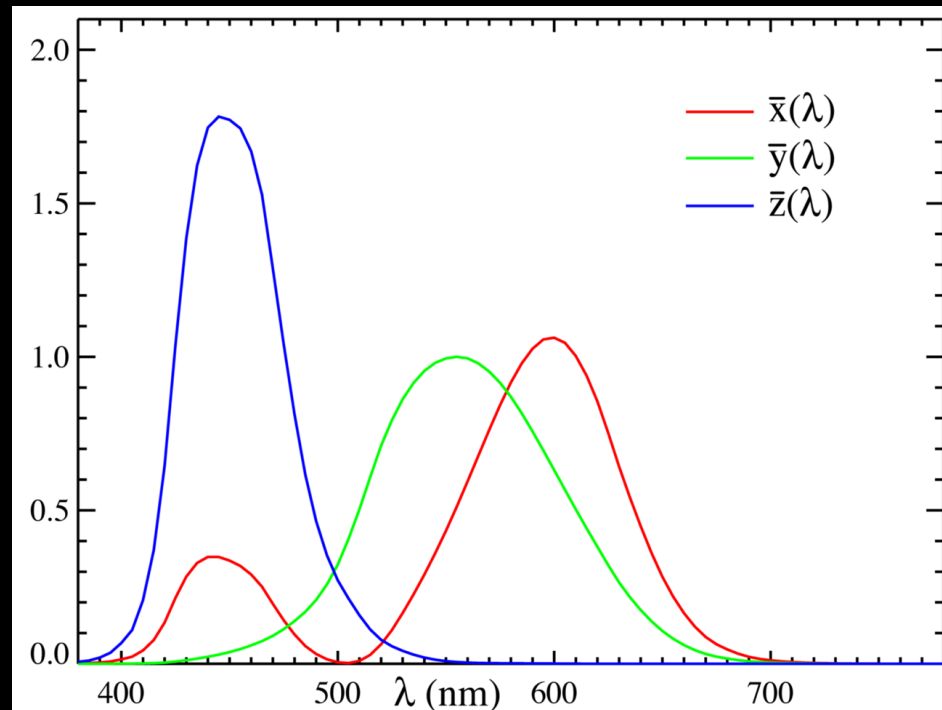
Normalize so they add up to 1 ("color" should not depend on overall intensity)

- $x = 15/27 = 0.56$
- $y = 12/27 = 0.44$
- $z = 1 - x - y = 0$

These are the chromaticity coordinates!!

Another Worked Example

- What is (x, y) for a delta function at 560 nm?



My estimates:

$X = 0.59$

$Y = 0.98$

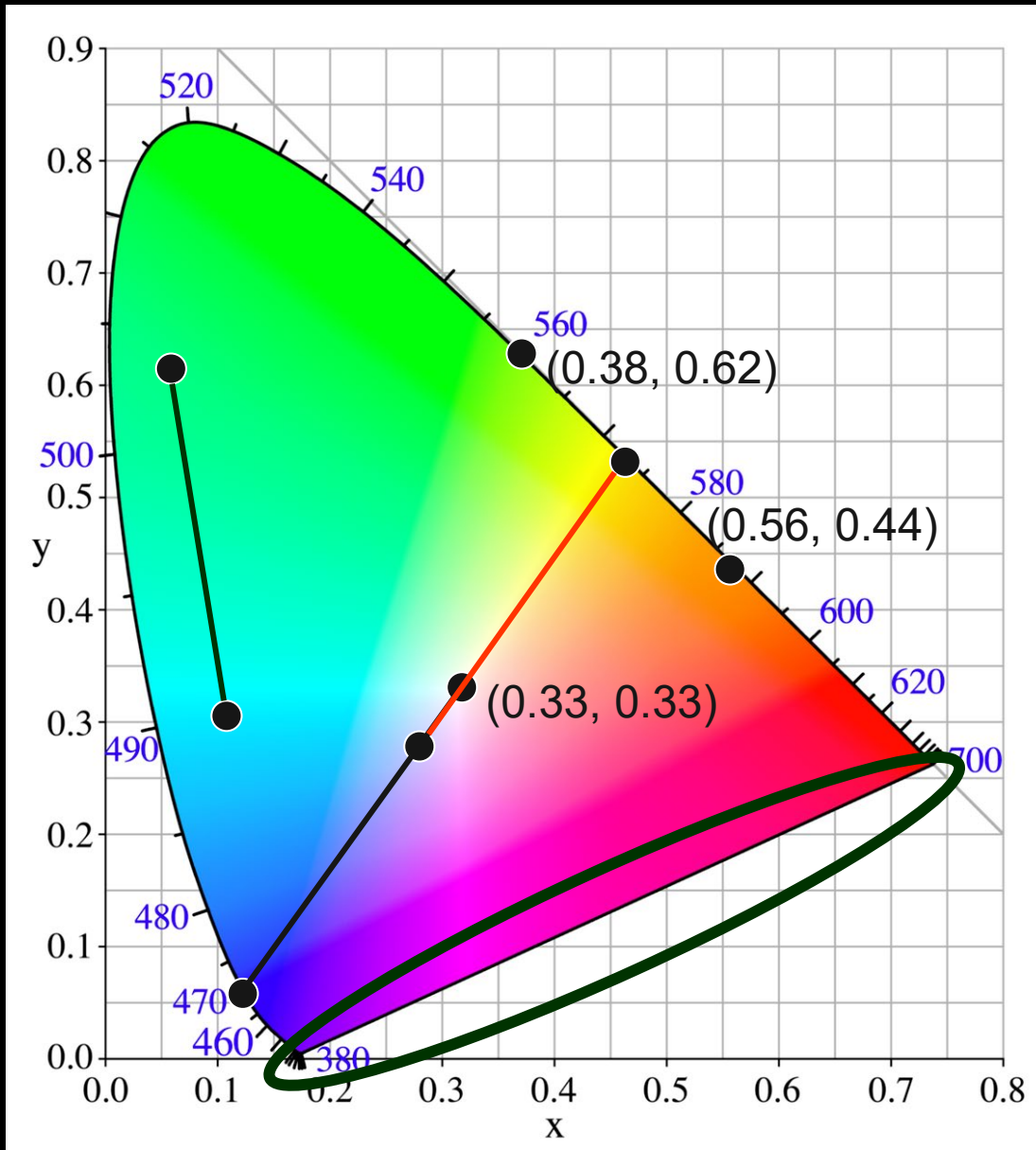
$Z = 0$

$x = 0.38$

$y = 0.62$

Do that for every wavelength \rightarrow the “locus” curve

Chromaticity Diagram



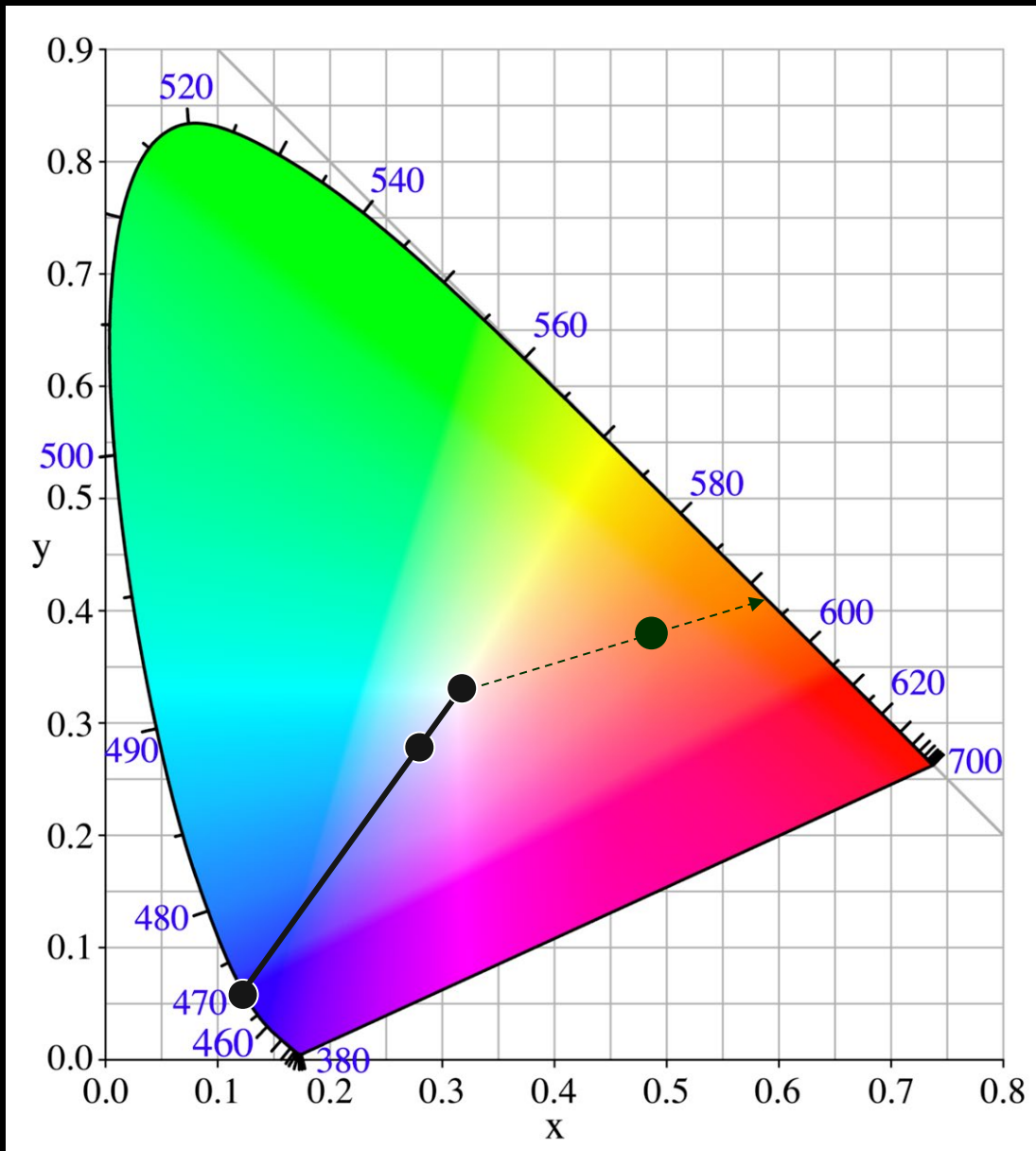
Things to observe

- Example 2: 560 nm = (0.38, 0.62)
- The locus curve
- Example 1: (0.56, 0.44)
- The white point = (0.33, 0.33)
- "Line of purples"

Linear effects

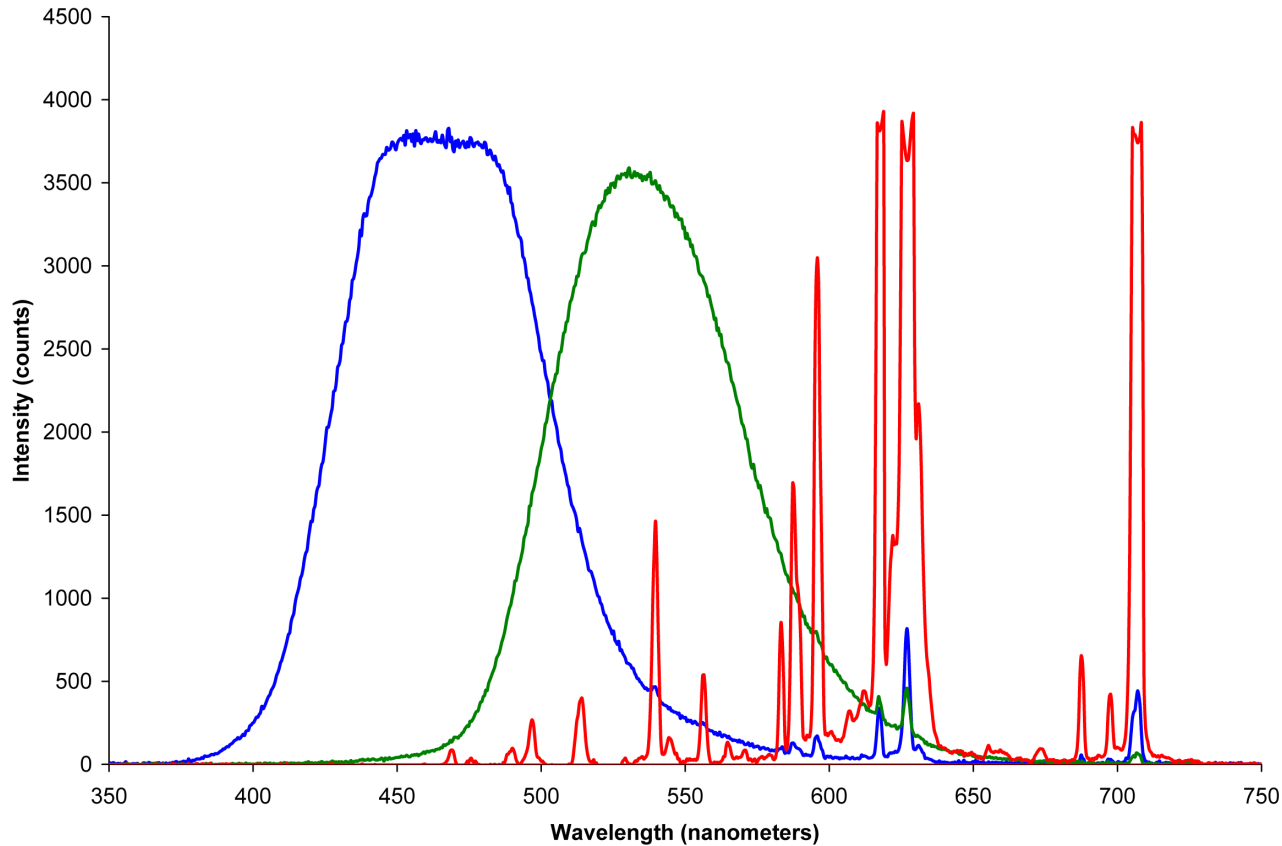
- Color mixing along line connecting two points
- "Hue": pure wavelength which can mix with white to get the point. Example: 470 nm
- "Complementary color": color that can mix with the point to get white. Example: $\lambda_c = 573$ nm

Chromaticity Diagram



- Saturation: How close is the point to its hue?
 - Example 1: 18%
 - Example 2: 65%
- Brightness
 - Overall intensity, Not on this diagram

Remember this?

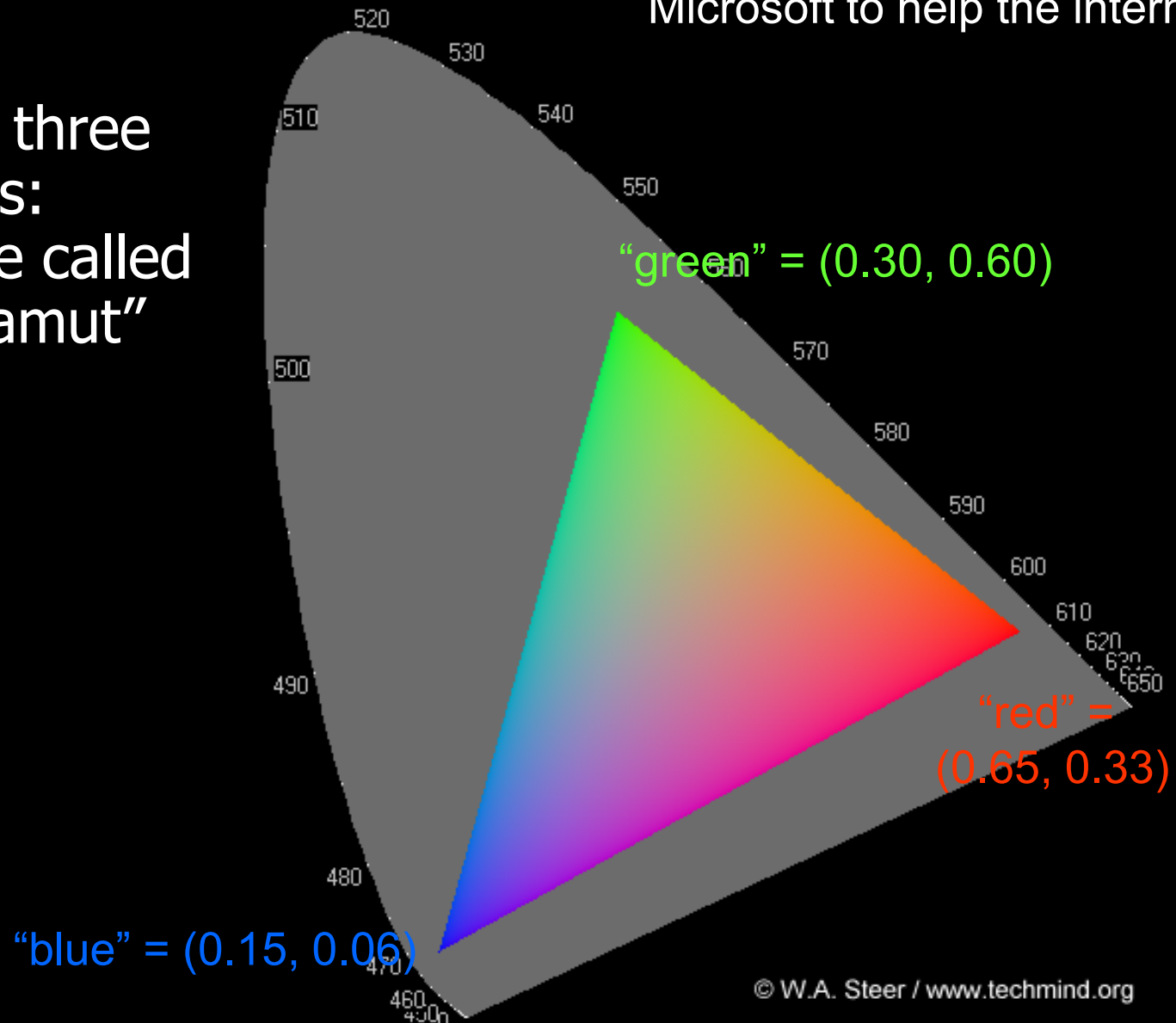


The **emission spectra** of the three **phosphors** that define the **additive primary colors** of a **CRT** color video display. Other electronic color display technologies (**LCD**, **Plasma display**, **OLED**) have analogous sets of primaries with different emission spectra.

sRGB: three specific color sources

Standard created in 1996 by HP and Microsoft to help the internet

- Mixing three sources:
triangle called the “gamut”

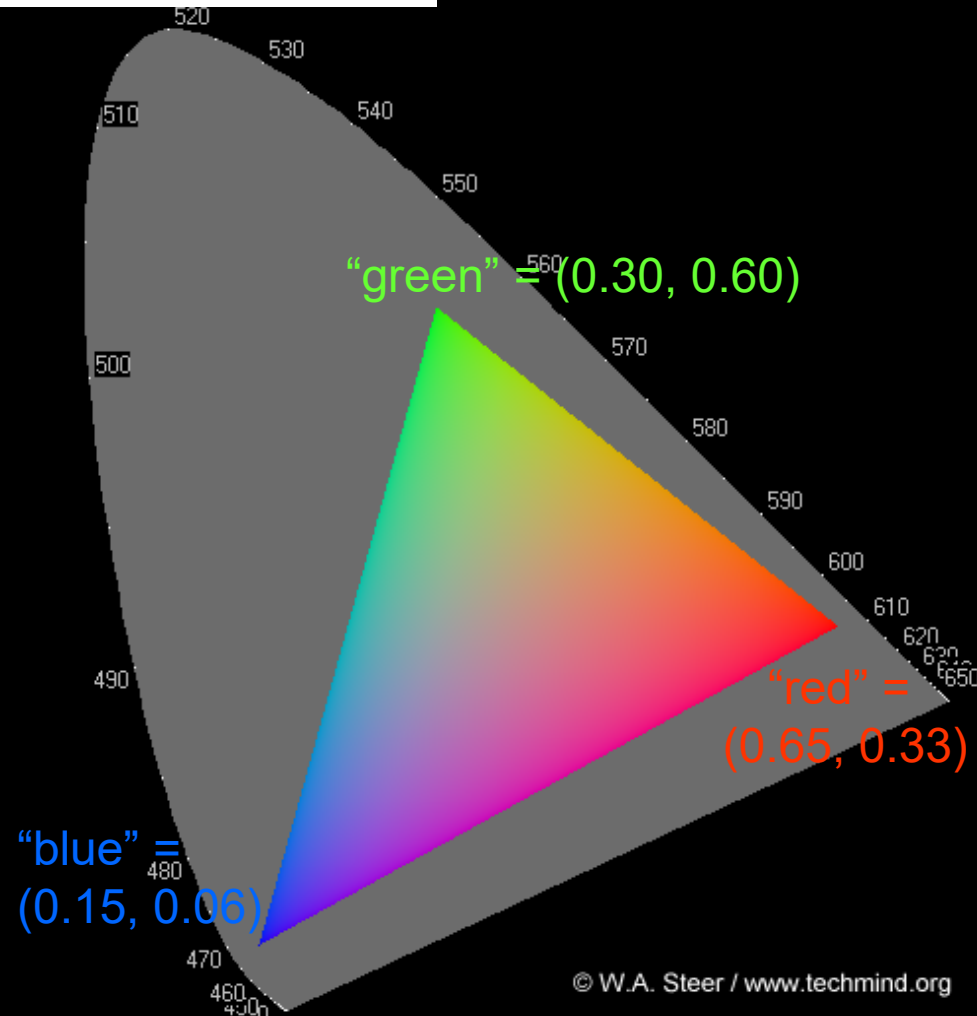


XYZ to sRGB

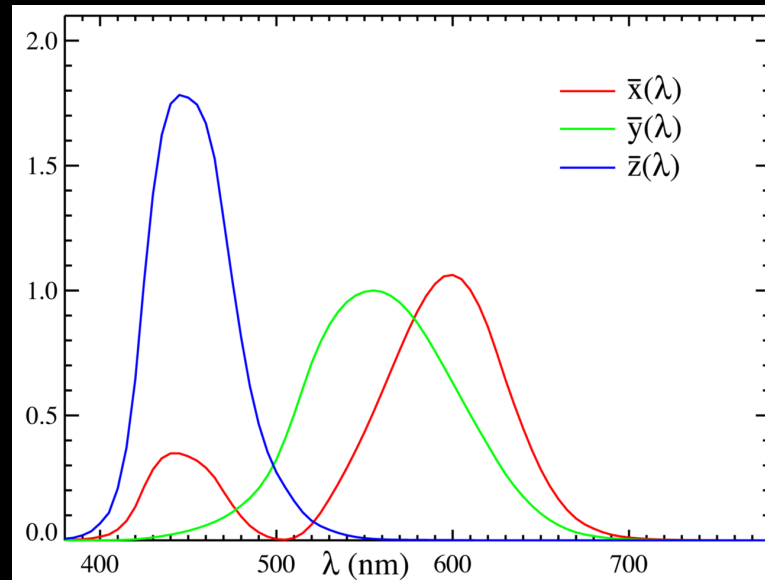
$$\begin{bmatrix} \tilde{R} \\ \tilde{G} \\ \tilde{B} \end{bmatrix} = \begin{bmatrix} 3.2406 & -1.5372 & -0.4986 \\ -0.9689 & 1.8758 & 0.0415 \\ 0.0557 & -0.2040 & 1.0570 \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \end{bmatrix}$$

From P&W P2.14

- Step 1: linear transformation
- Step 2: apply nonlinear function because eyes respond logarithmically (given in P2.14)
- Normalize R,G,B values to be integers from 0 to 255
 - a. $256 \times 256 \times 256 = 16,777,216$ possible colors



- Reminder: what was Y?



- all are positive
- \bar{z} = close to S cones, close to \bar{b}
- \bar{y} = matches intensity response of eye, close to M cones
- \bar{x} = chosen so that white is equal parts of all three

$XYZ \leftrightarrow xyY$ Transformations

$$\begin{bmatrix} x \\ y \\ Y \end{bmatrix} = \begin{bmatrix} \frac{X}{X+Y+Z} \\ \frac{Y}{X+Y+Z} \\ Y \end{bmatrix}$$

$$\begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} \frac{x}{y} Y \\ Y \\ \frac{1-x-y}{y} Y \end{bmatrix}$$

"Hue, brightness, saturation"

- Hue – use RGB values to turn locus into a hexagon, then written as 0 to 360°
- Saturation called "chroma", as before
- Brightness from Y, scaled as 0 to 1

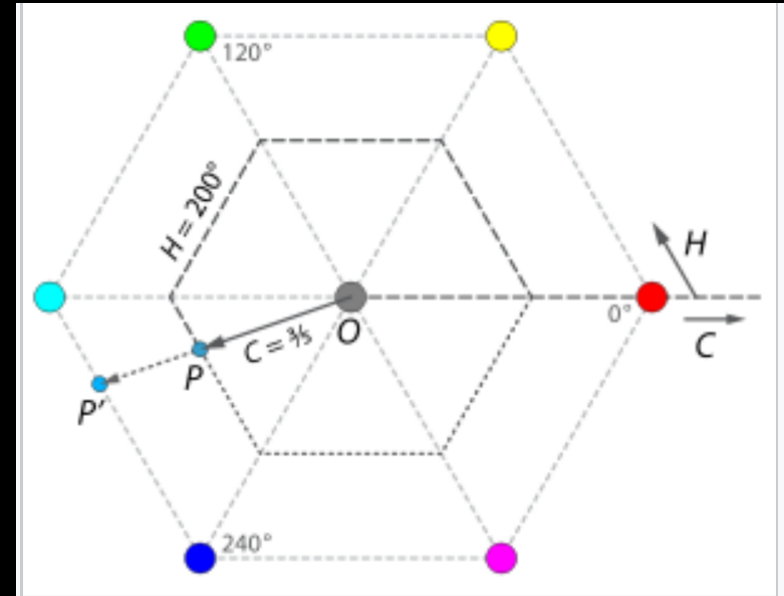
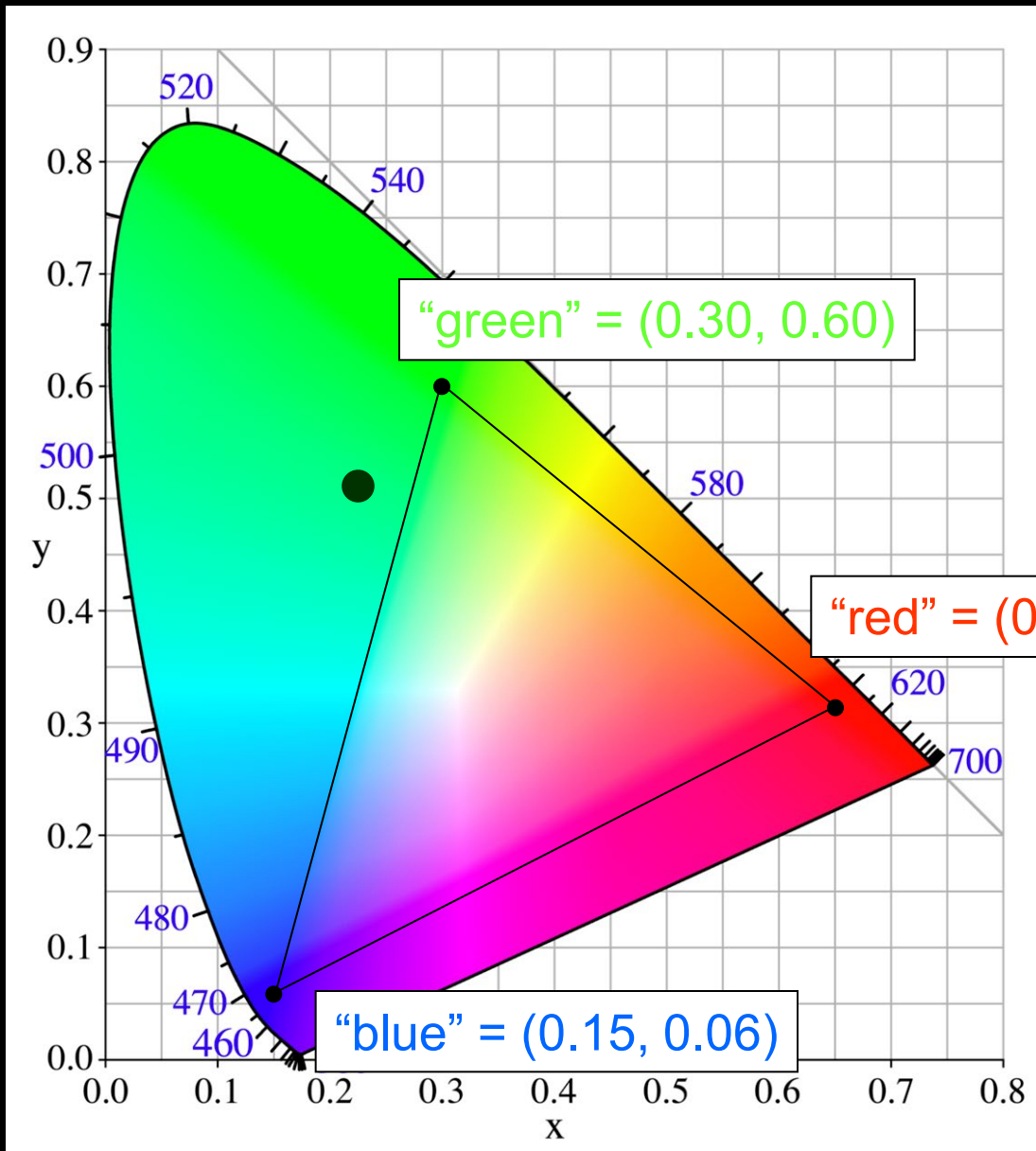


Fig. 9. Both hue and chroma are defined based on the projection of the RGB cube onto a hexagon in the "chromaticity plane". Chroma is the relative size of the hexagon passing through a point, and hue is how far around that hexagon's edge the point lies.

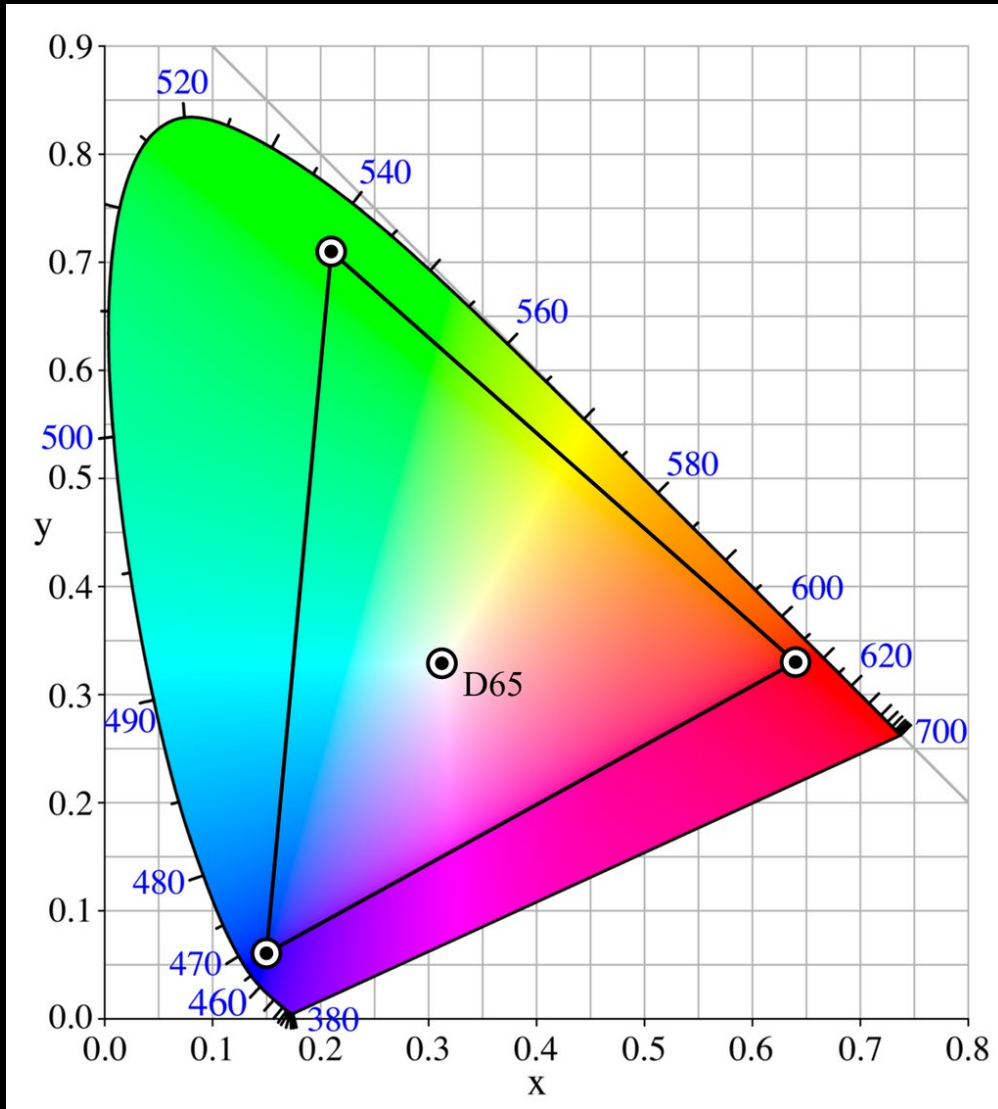
From Wikipedia
"HSL and HSV"

sRGB gamut, again



- How would you get this color using sRGB?
- What would be the ideal set of three light sources for your monitor to give you as many colors as possible in the gamut?

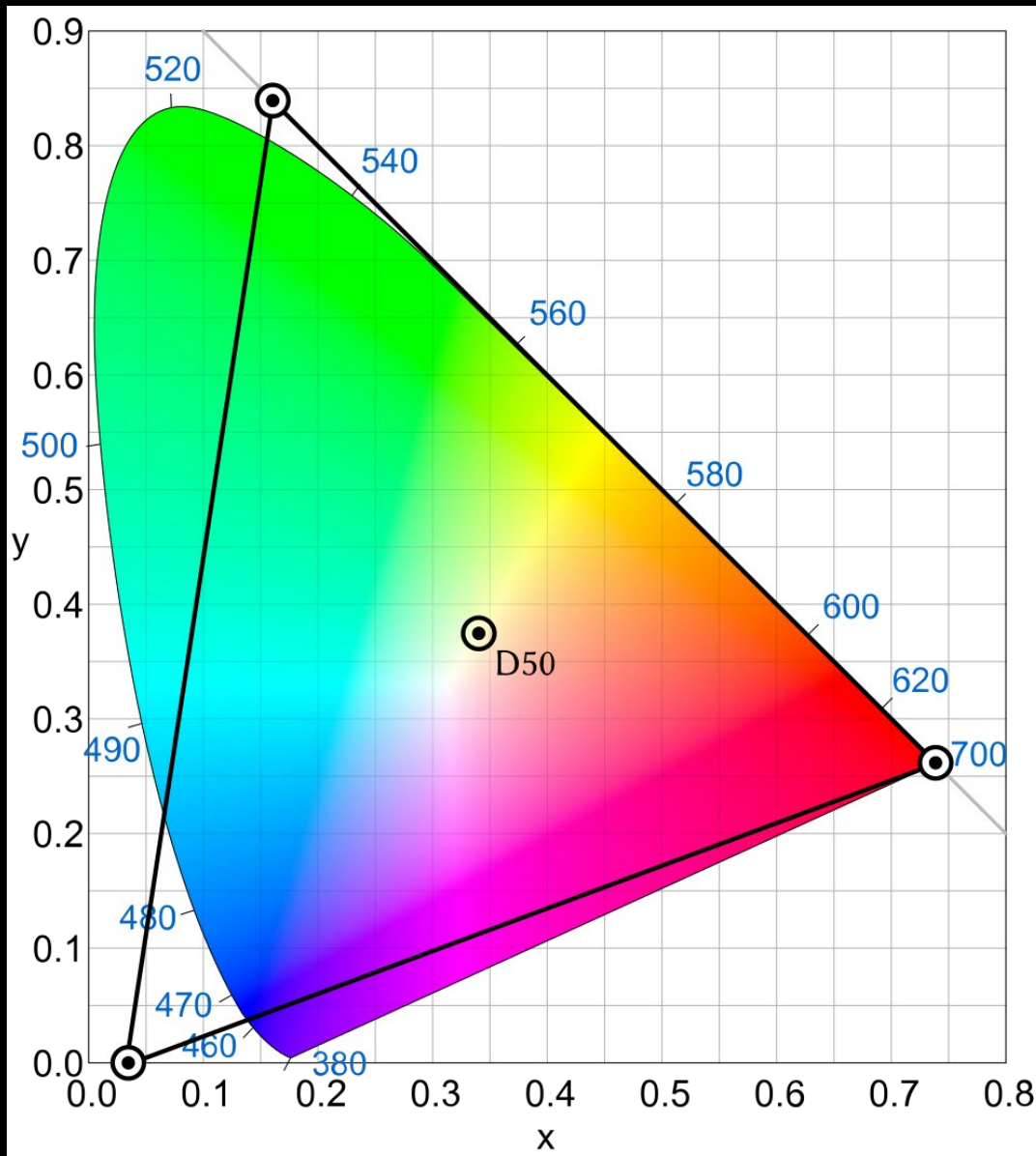
Adobe RGB



- Better than sRGB?
- Only if your camera/display/ printer are all calibrated for it
- Not for use on internet
- Also: there's a wider range of possible colors, but the difference between individual colors is bigger than in sRGB (still $256 \times 256 \times 256$)

From Wikipedia,
“Adobe RGB color space”

ProPhoto RGB



“One of the downsides to this color space is that approximately 13% of the representable colors are imaginary colors that do not exist and are not visible colors.”

From Wikipedia,
“ProPhoto RGB color space”

Summary

- Three types of cones: short, medium, long
- Three dimensional color space: RGB
- “Color matching functions”: \bar{r} , \bar{g} , \bar{b}
- Alternate functions: \bar{x} , \bar{y} , \bar{z}
 - \bar{y} = overall response
 - \bar{z} is basically \bar{b}
 - \bar{x} makes white light have equal parts
- Projections of spectrum: X,Y,Z values
- Normalized X,Y,Z values: x,y,z
- Chromaticity coordinates: x,y
- Chromaticity diagram
 - Locus, gamut, linear effects, complementary colors, etc.
- Other ways to specify coordinate in 3d space:
 - x,y,Y; hue, saturation, Y; hue, brightness, saturation;
 - sRGB coordinates; other color spaces

